Algorithms

Robert Sedgewick | Kevin Wayne

FOURTH EDITION

Robert Sedgewick | Kevin Wayne
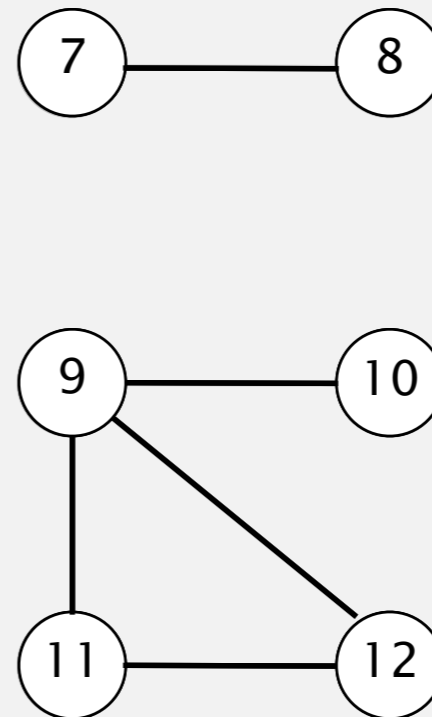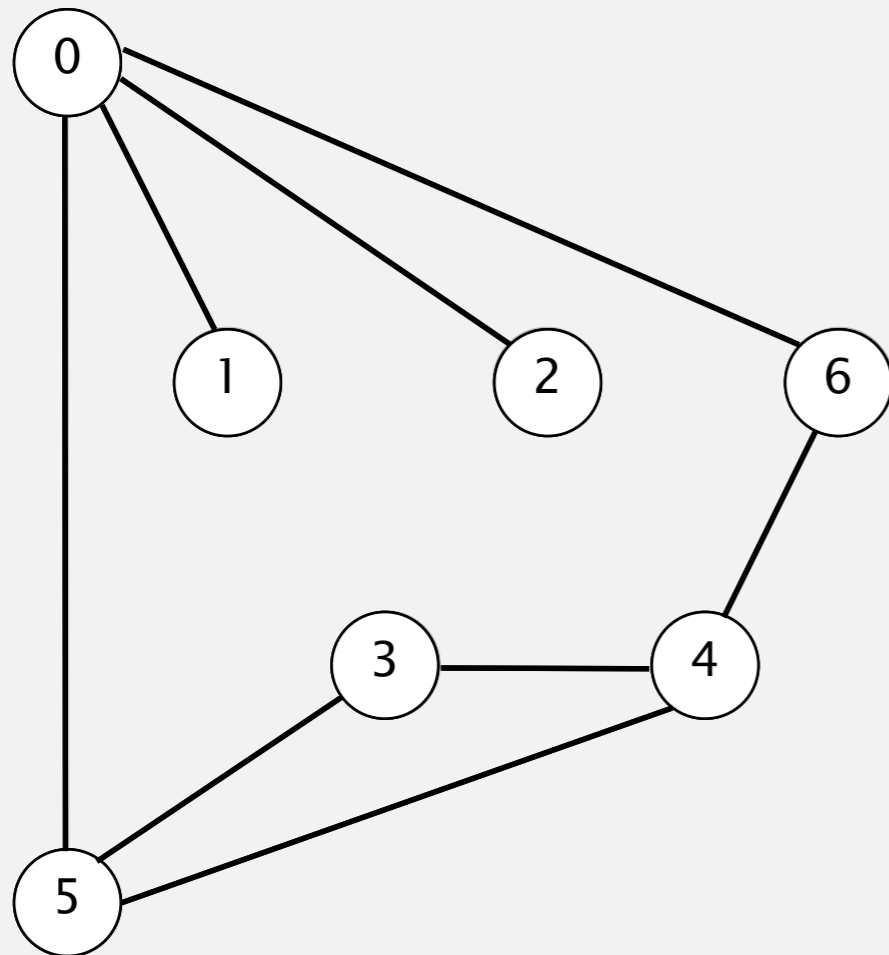
http://algs4.cs.princeton.edu

4.1 Connected Components Demo

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
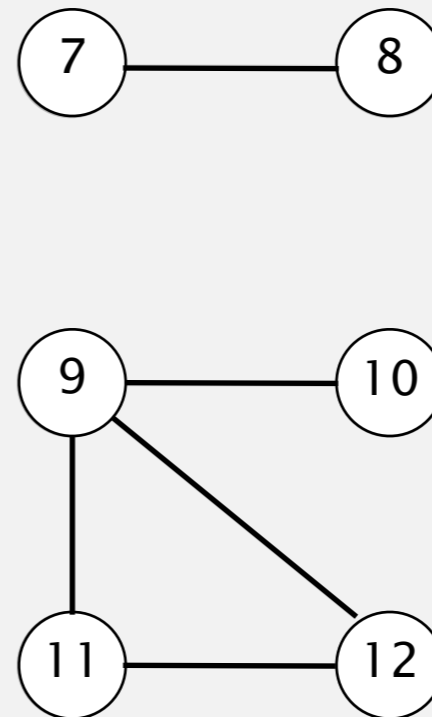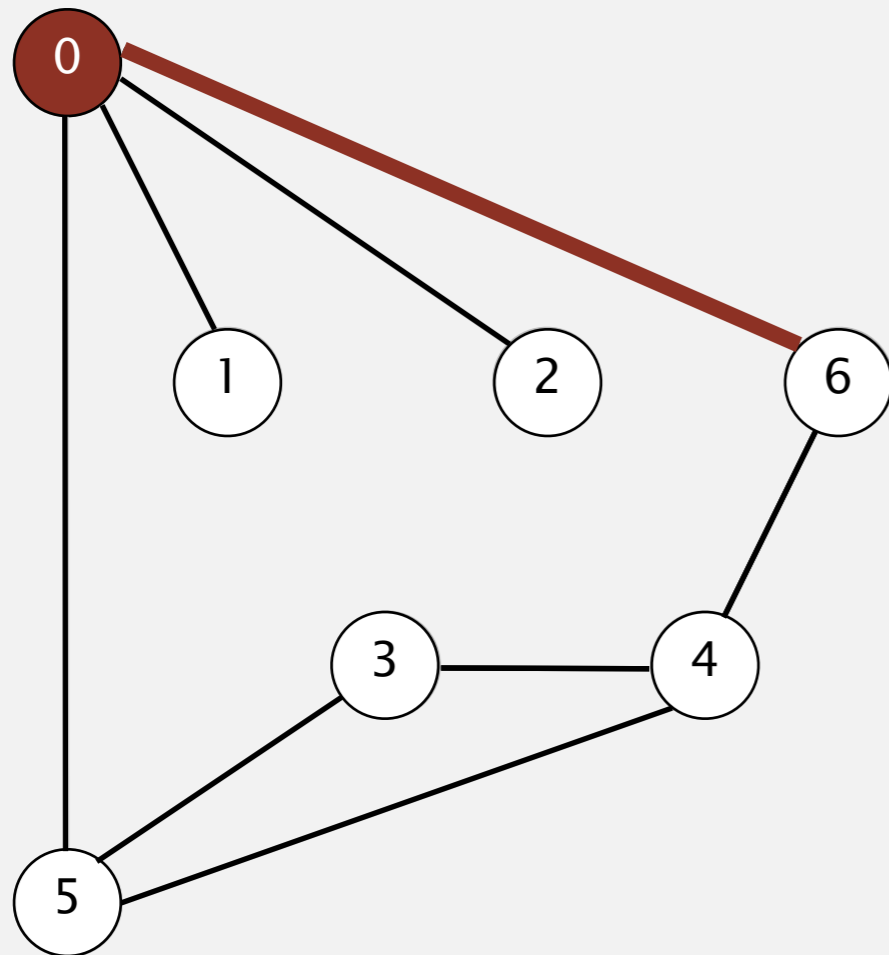- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	F	–
1	F	–
2	F	–
3	F	–
4	F	–
5	F	–
6	F	–
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

graph G

Connected components demo

To visit a vertex v :

- Mark vertex v as visited.
- Recursively visit all unmarked vertices adjacent to v.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	F	–
4	F	–
5	F	–
6	F	–
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 0

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
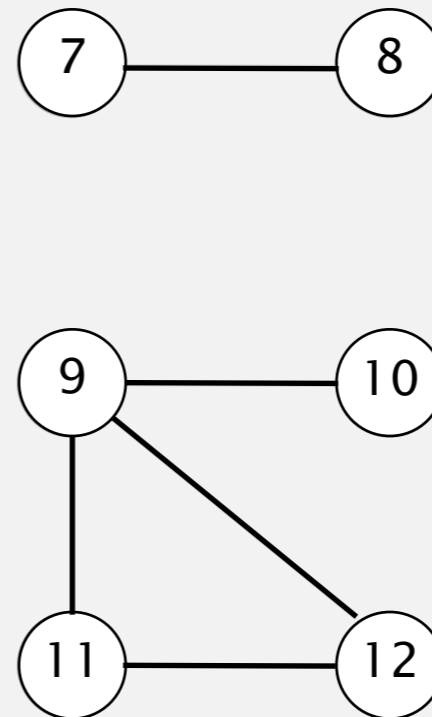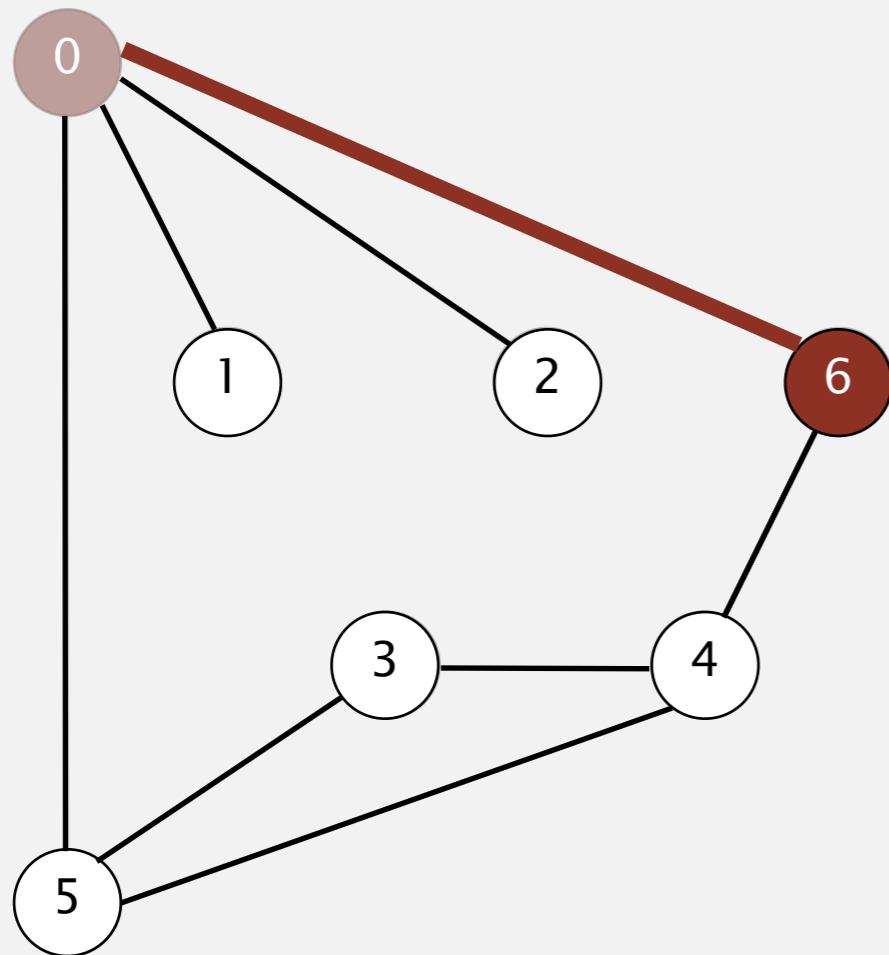
- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	F	–
4	F	–
5	F	–
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 6

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
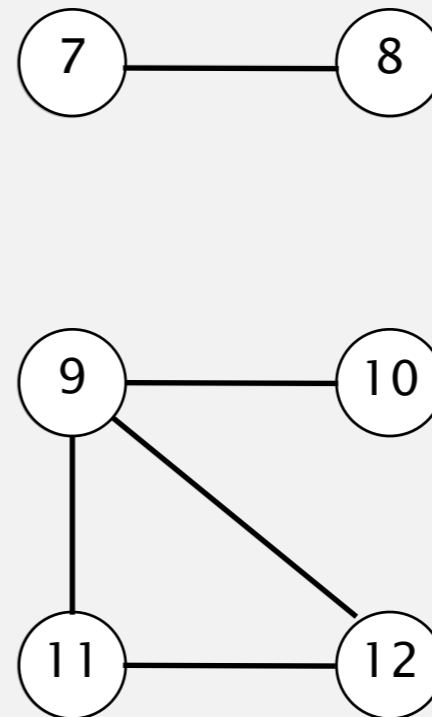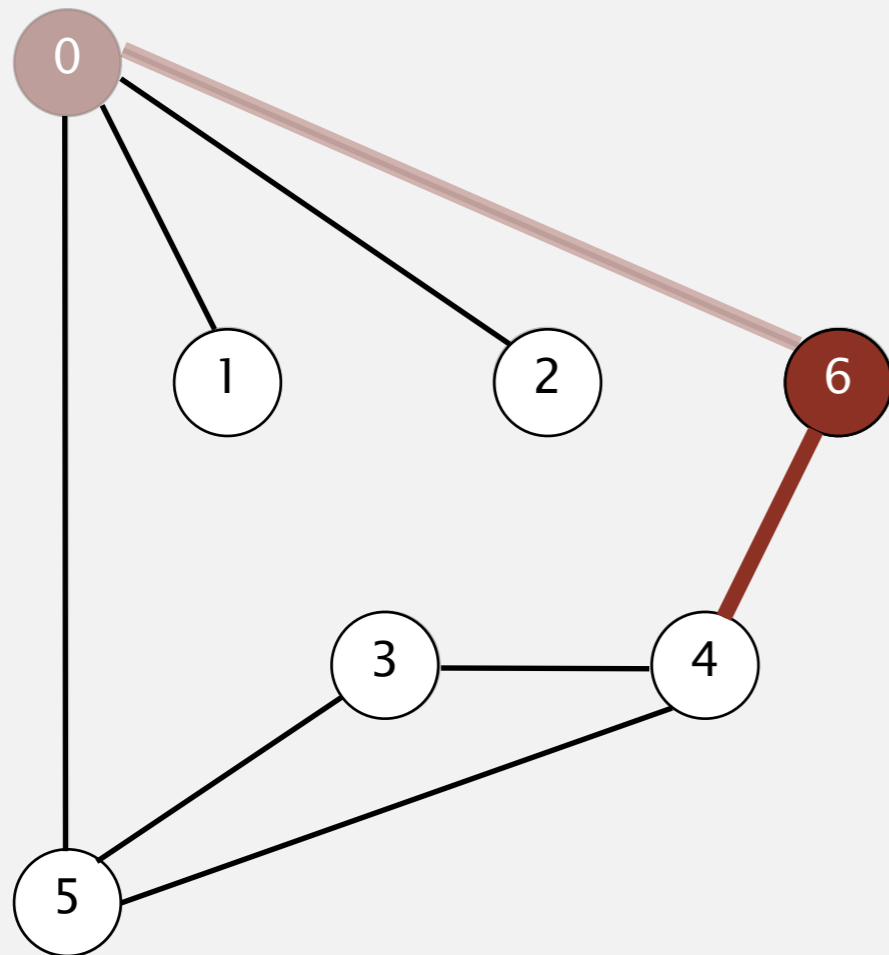- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	F	–
4	F	–
5	F	–
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 6

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
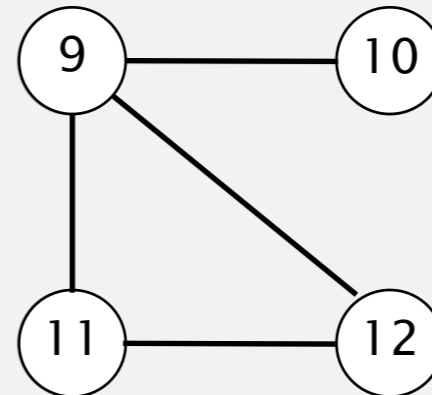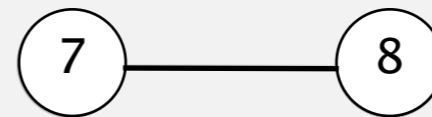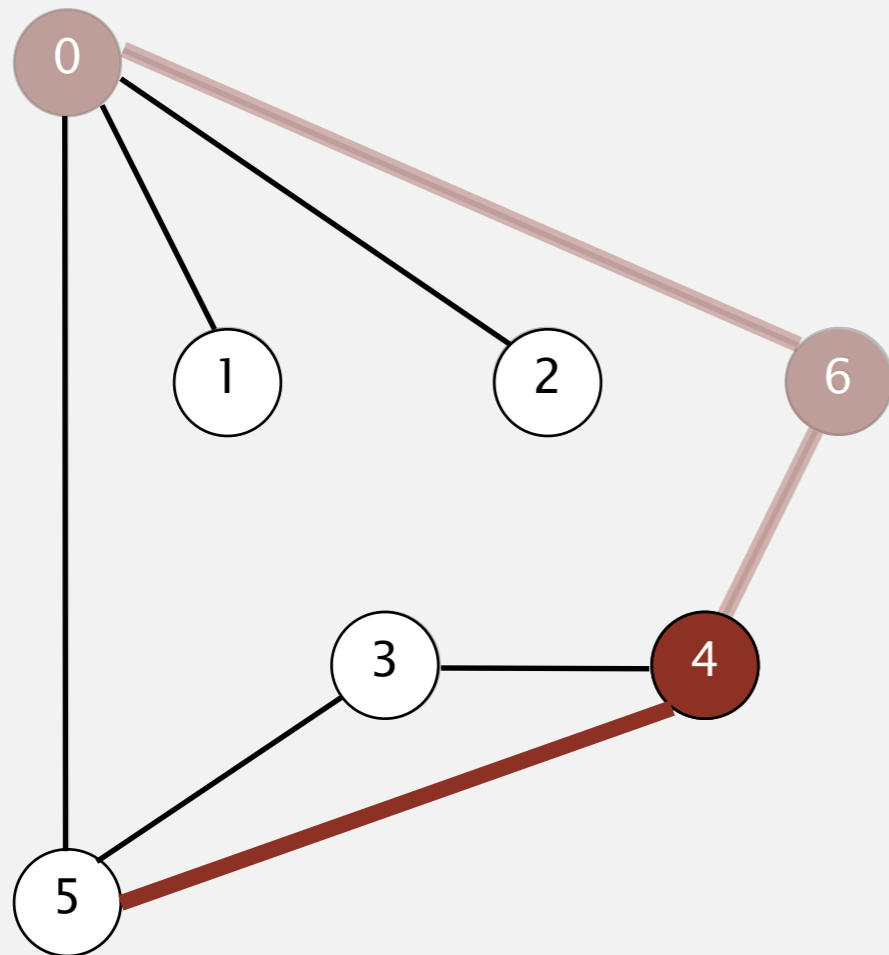
- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	F	–
4	T	0
5	F	–
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 4

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
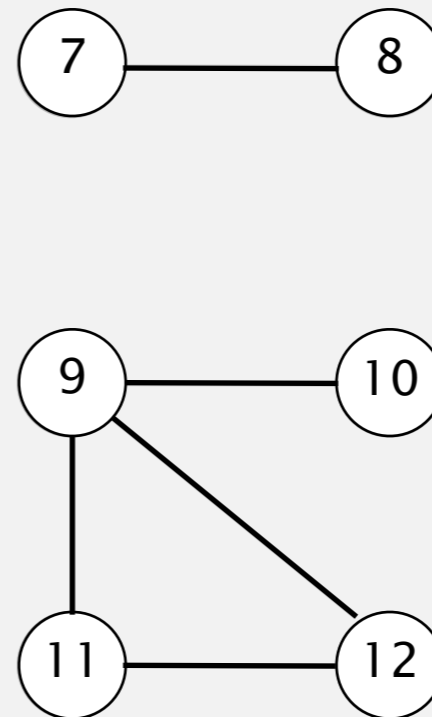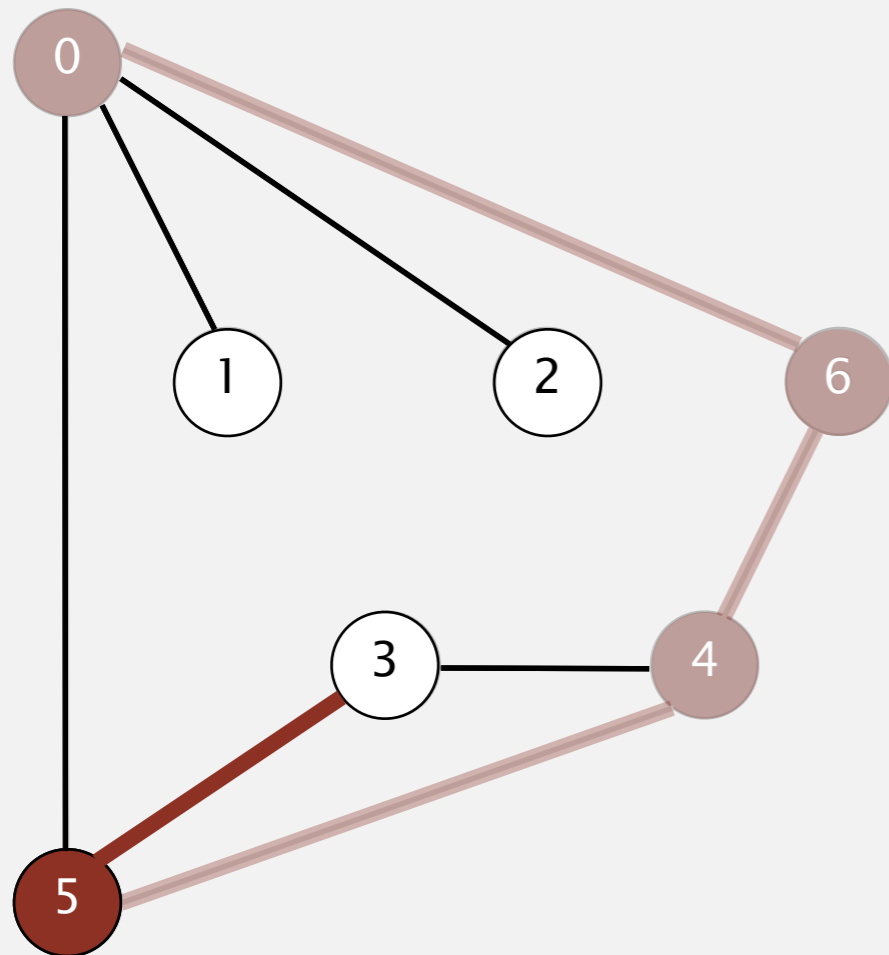
- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	F	–
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 5

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
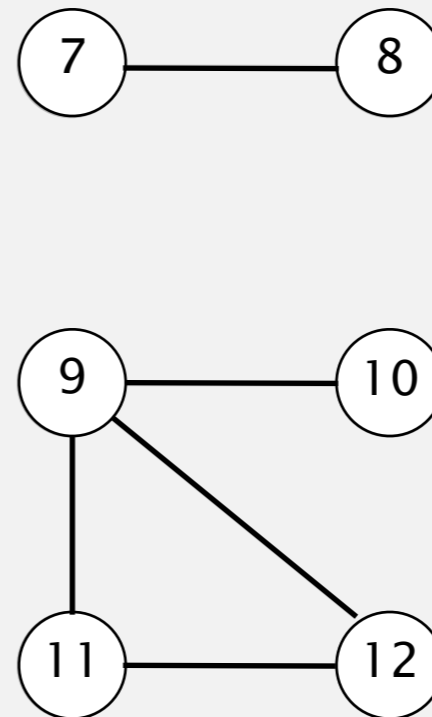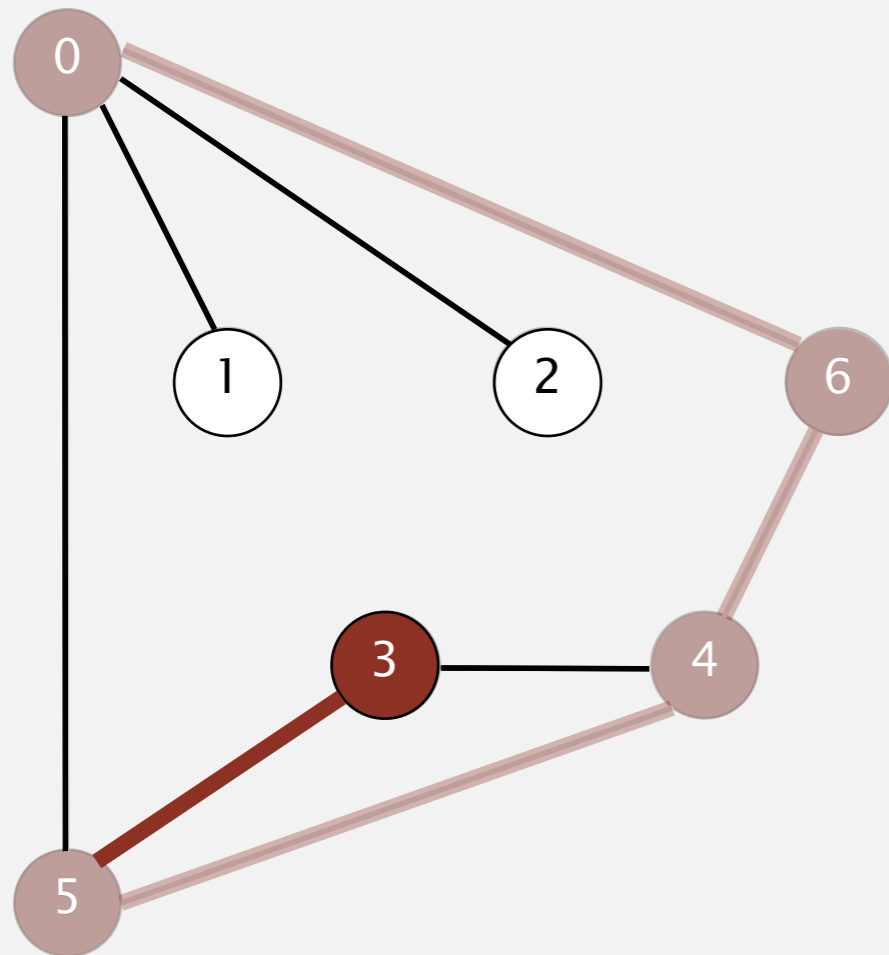
- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 3

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
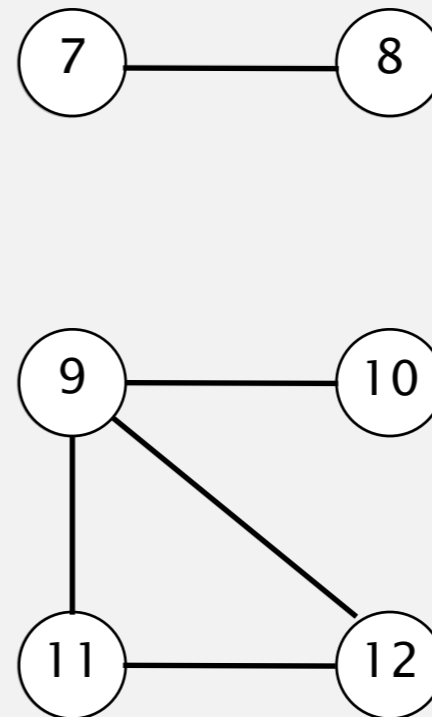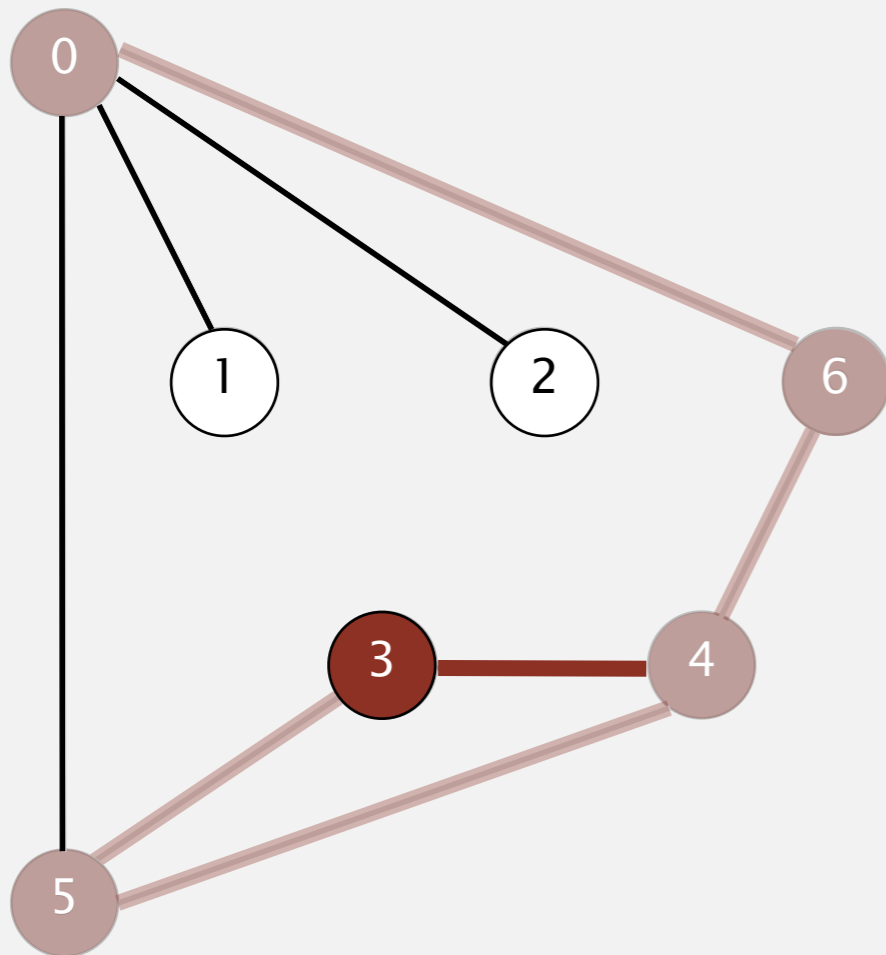- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 3

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
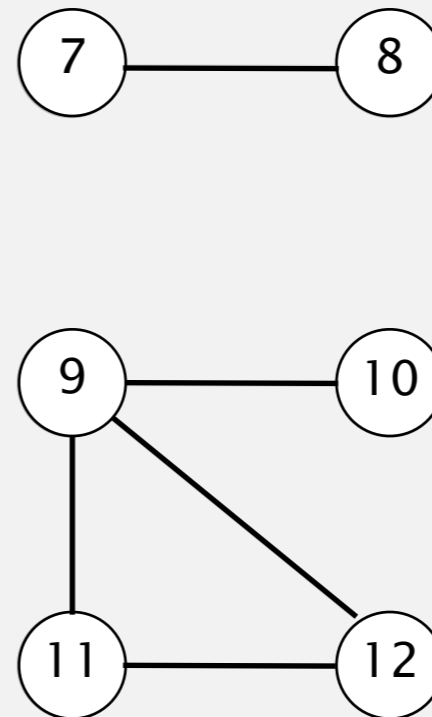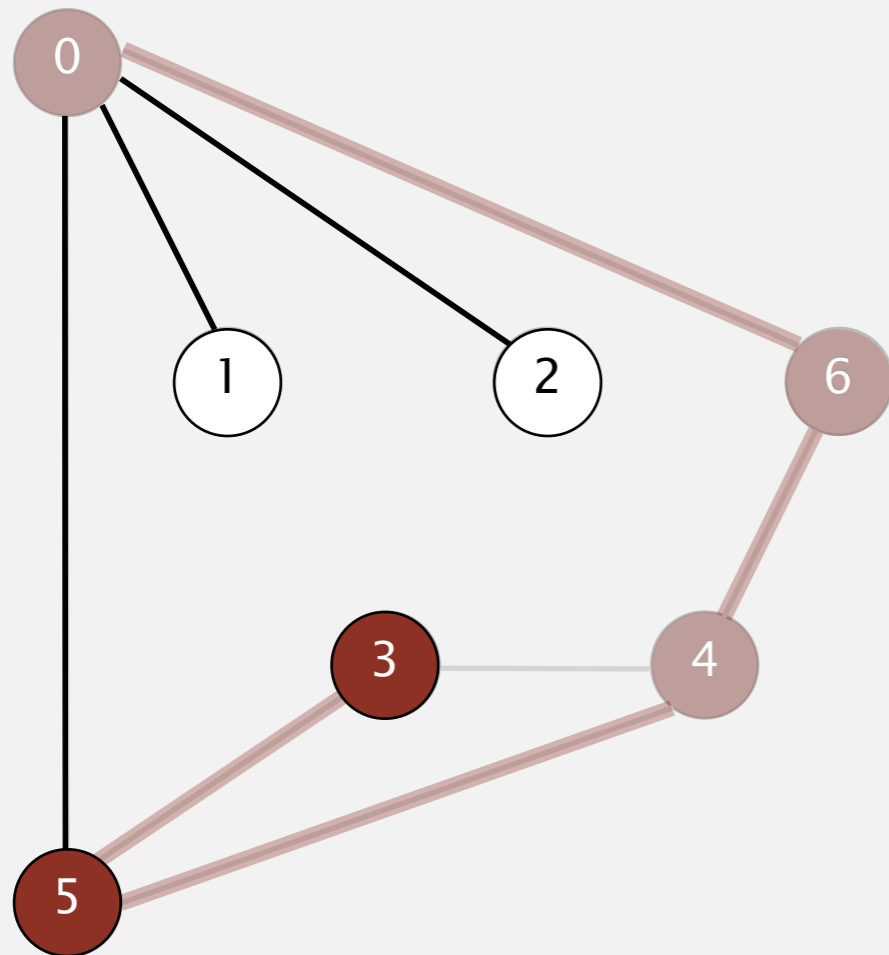
- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

3 done

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.

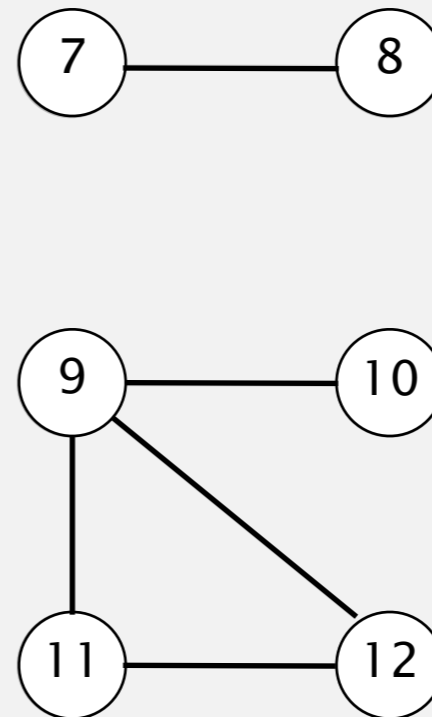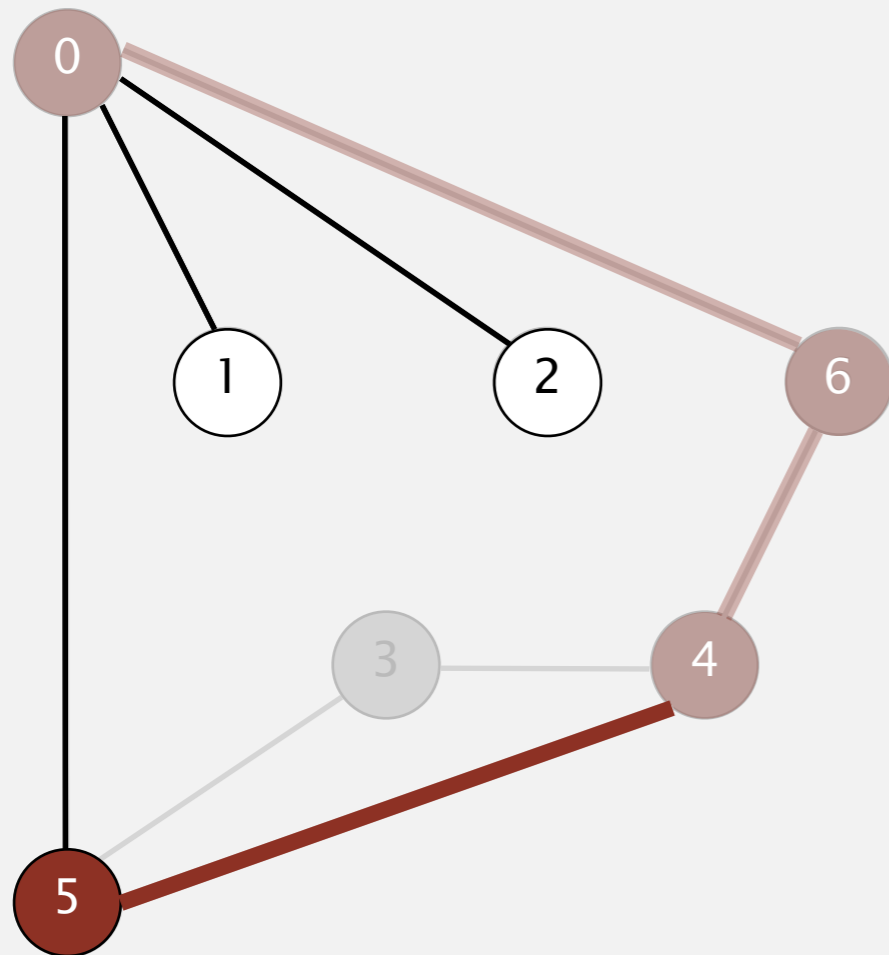- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 5

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
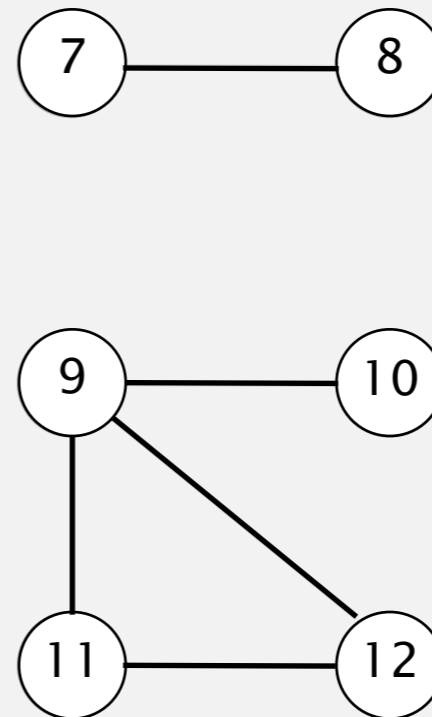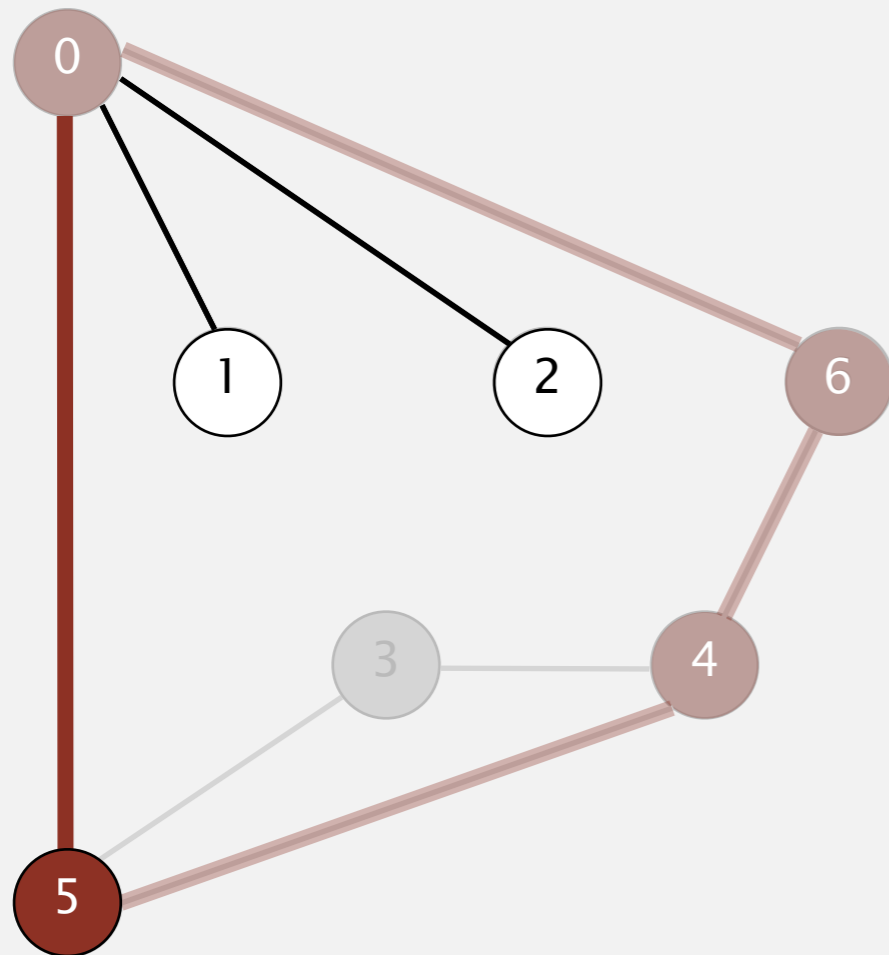
- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 5

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
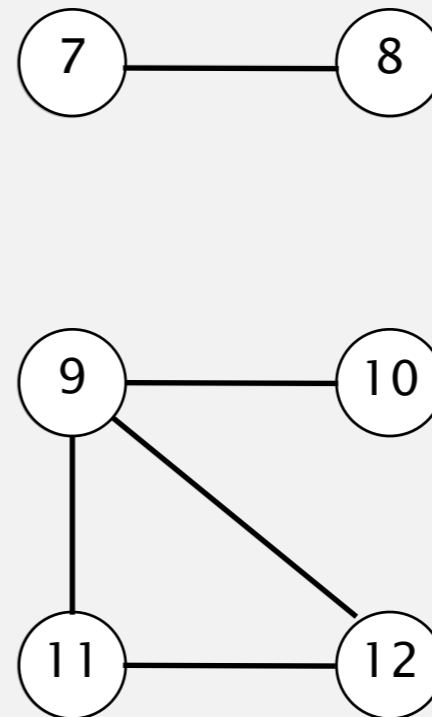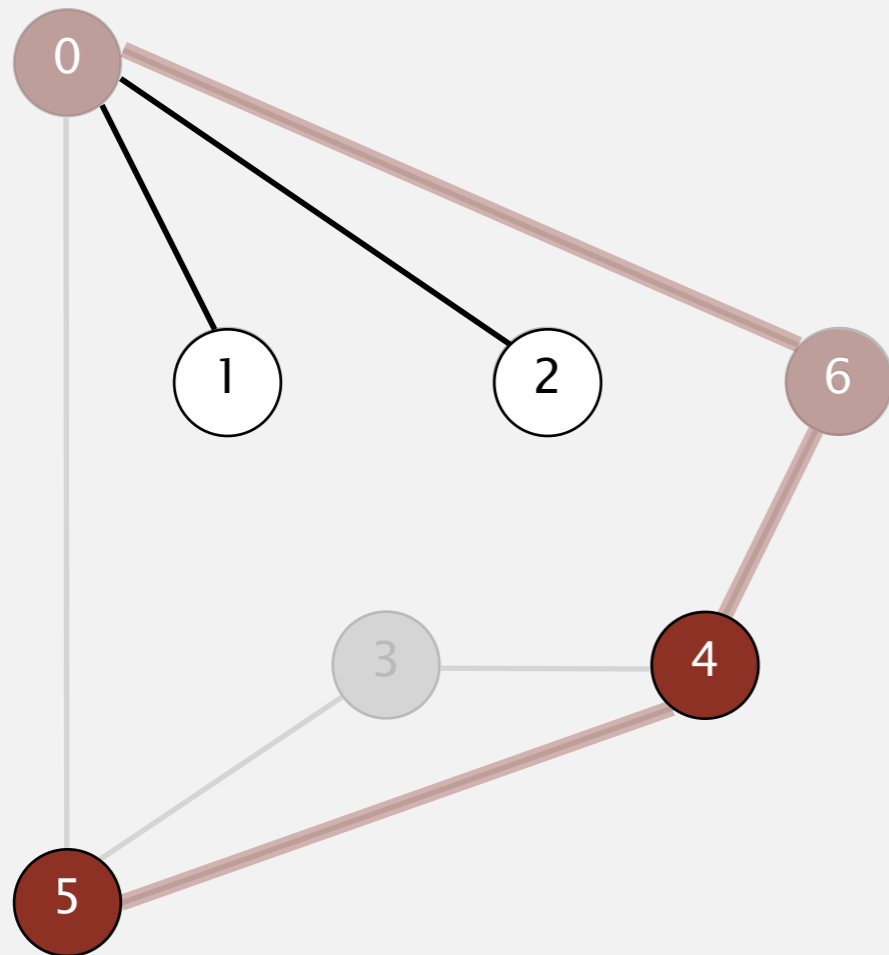- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

5 done

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
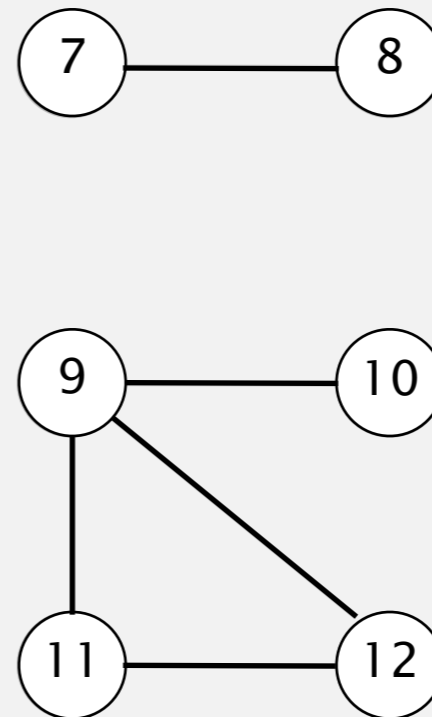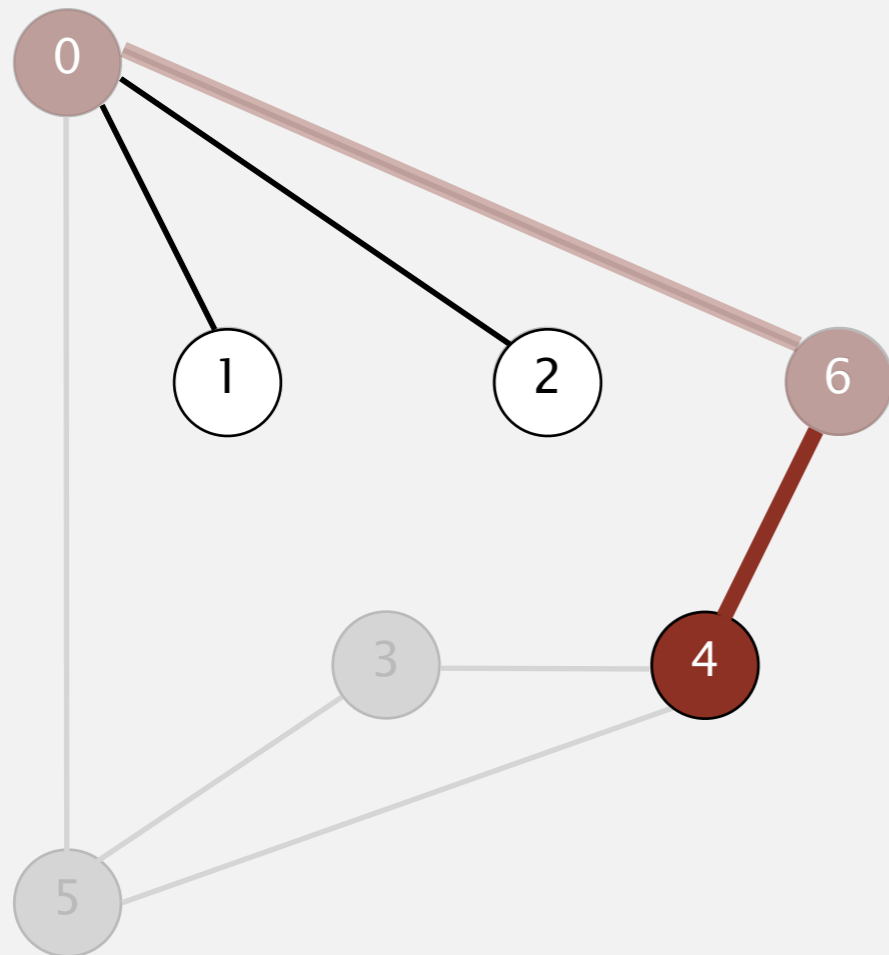- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 4

14

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
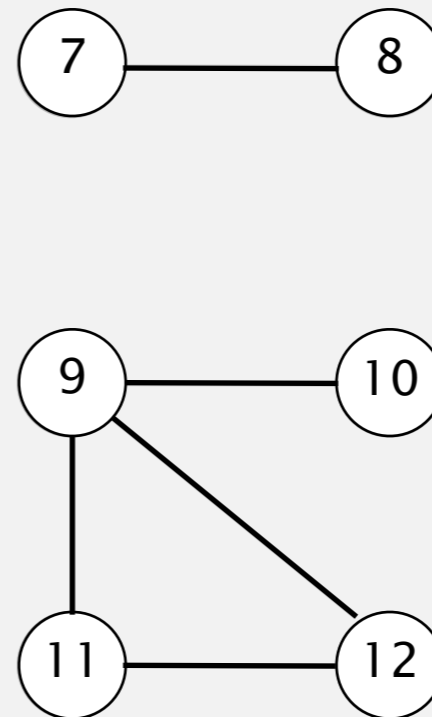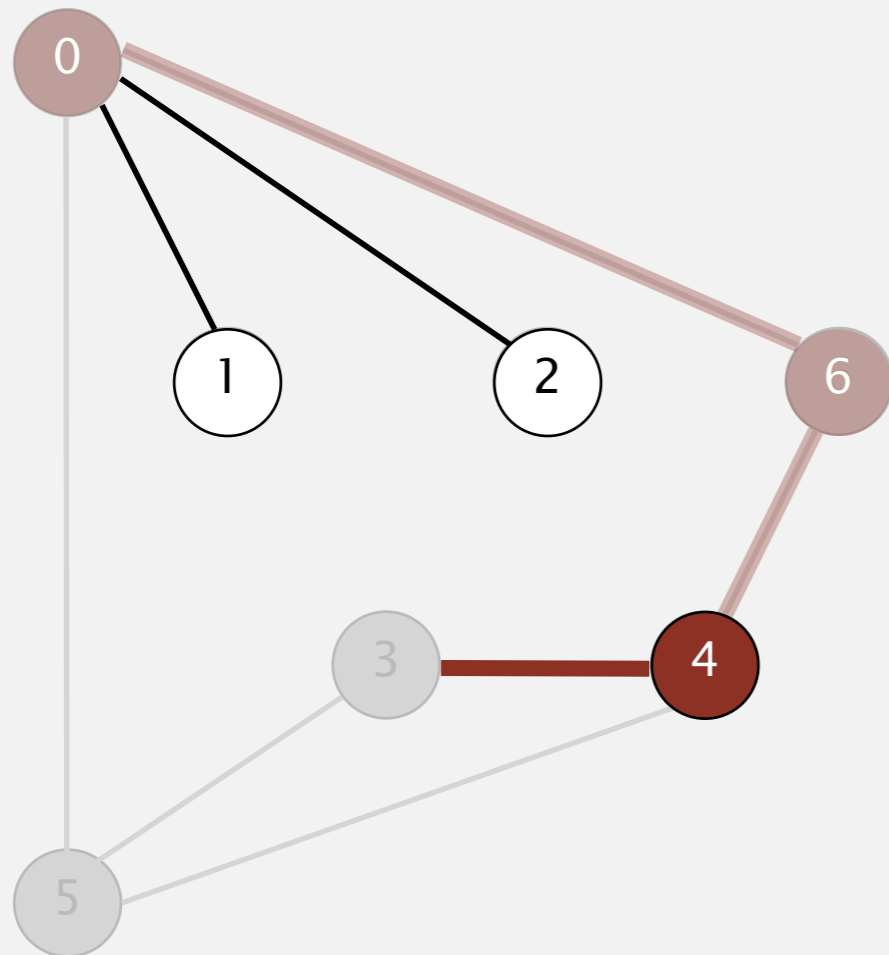
- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 4

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
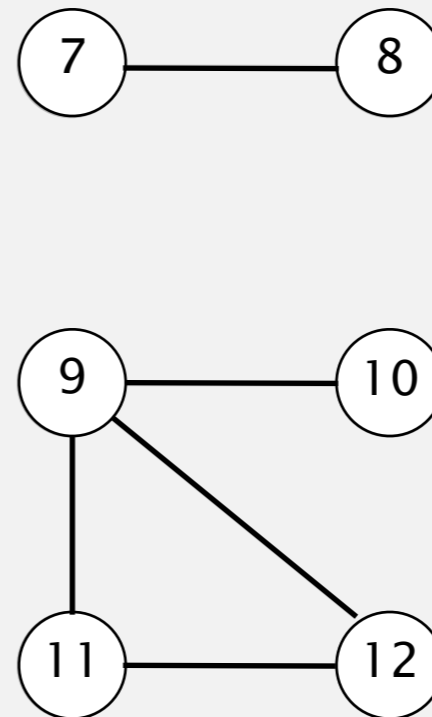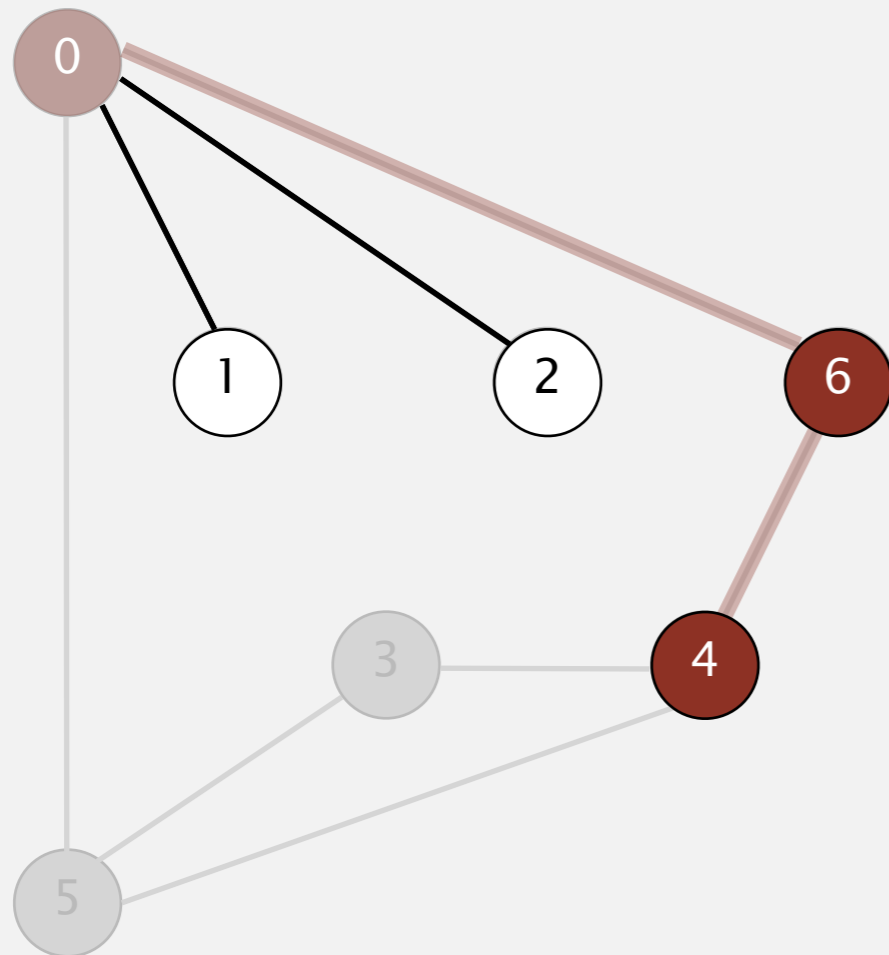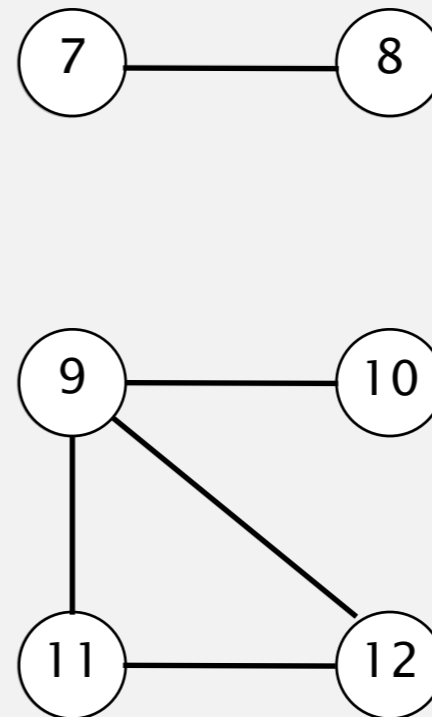
- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

4 done

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.

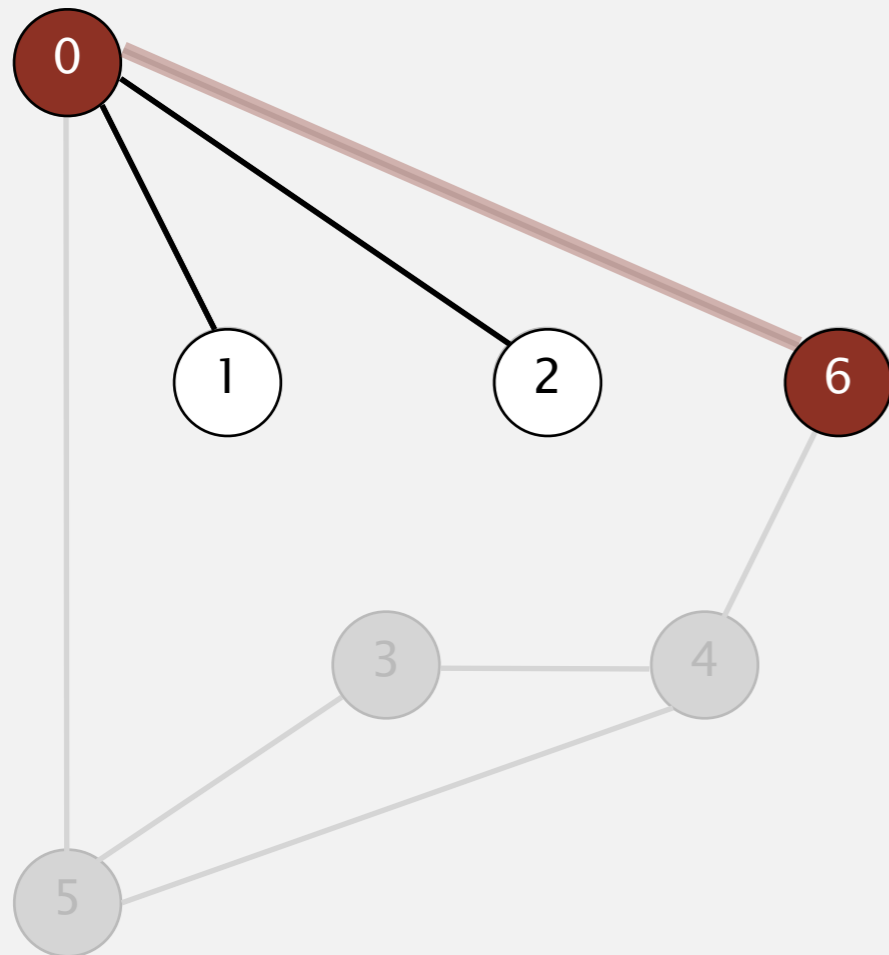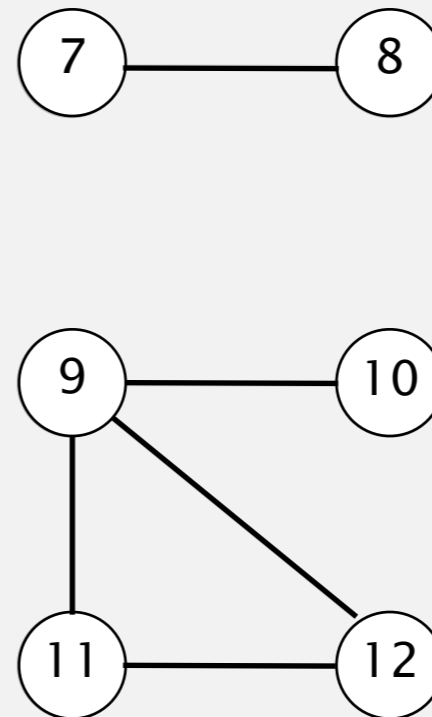- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

6 done

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
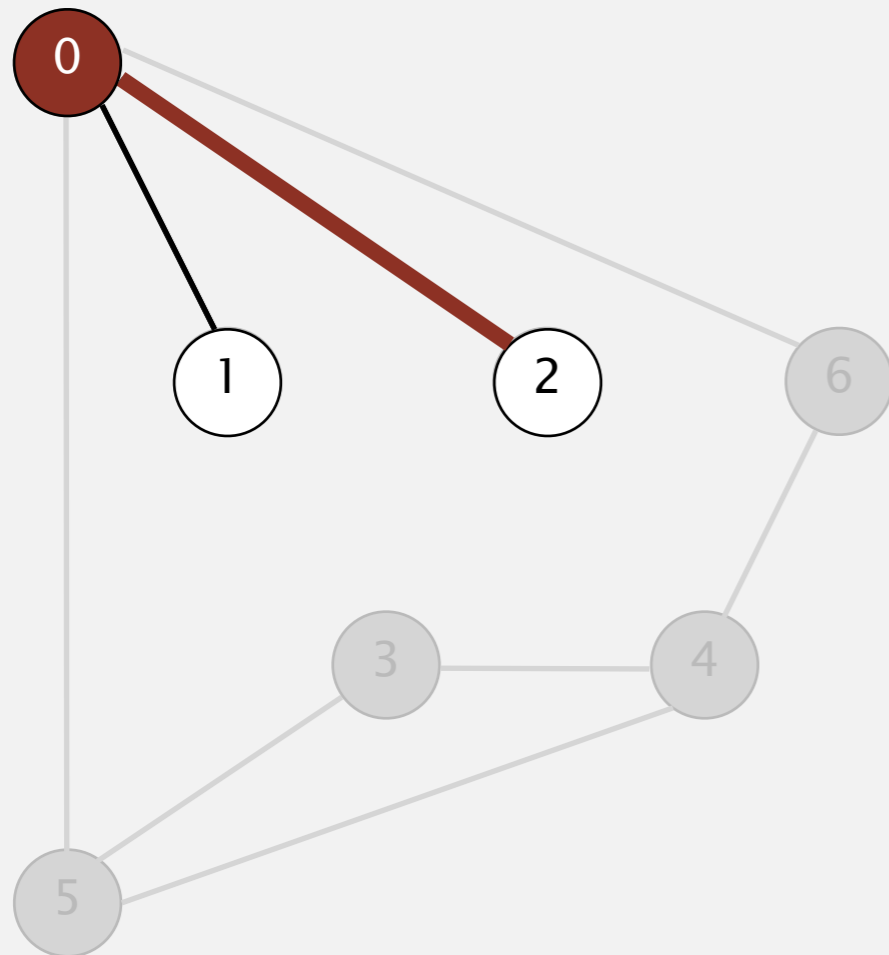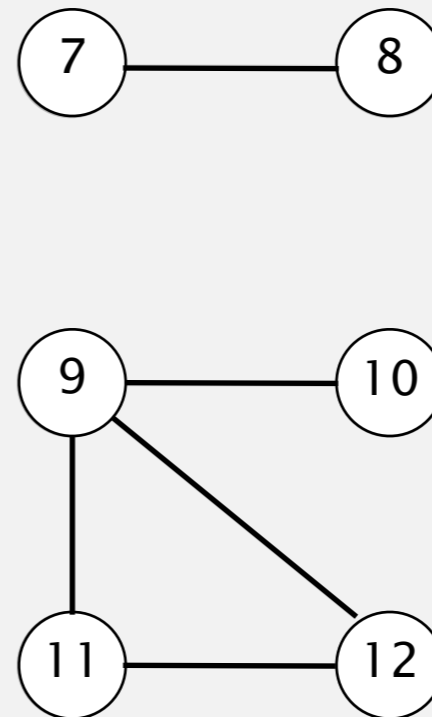- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	F	–
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 0

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.

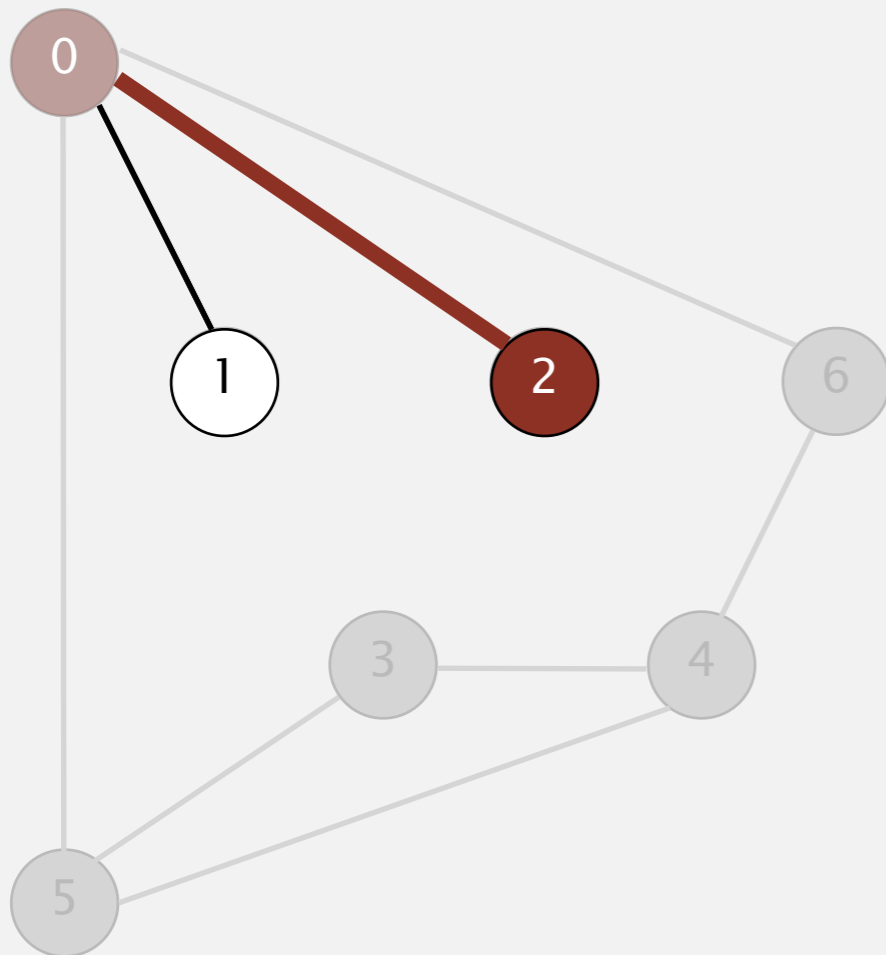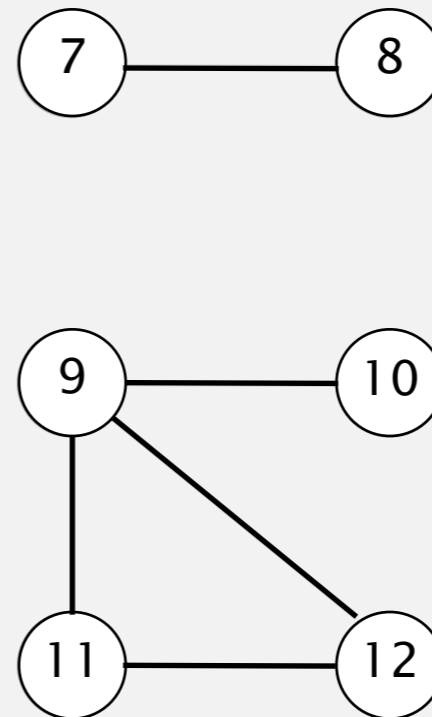- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 2

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
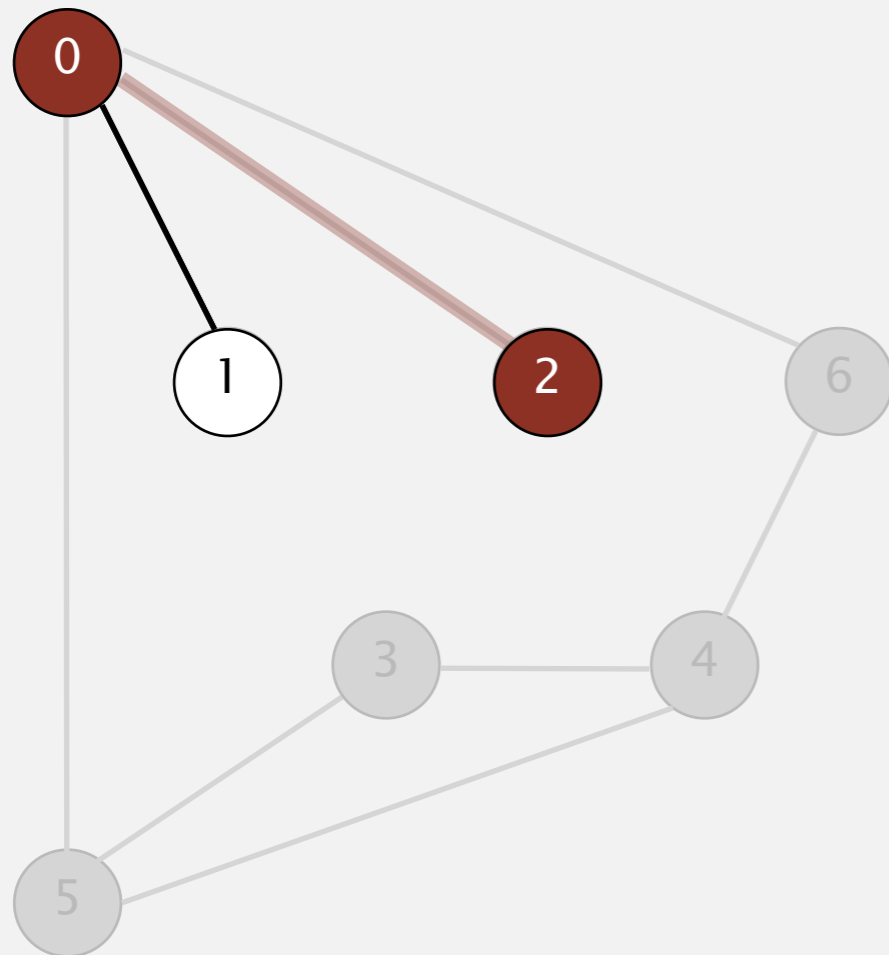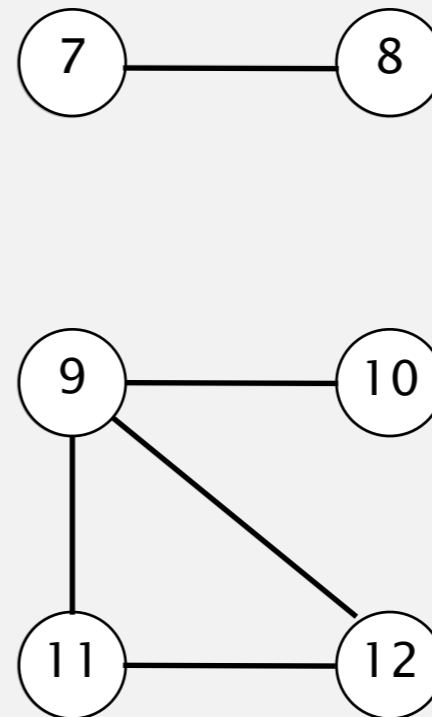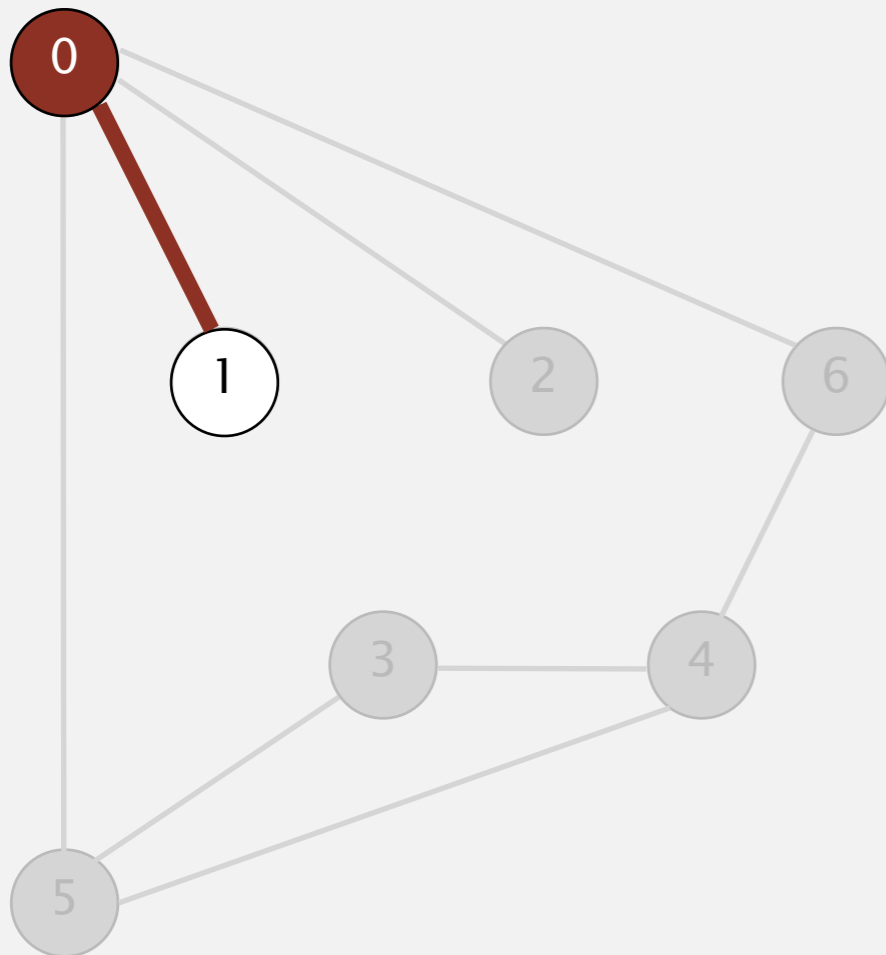
- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

2 done

To visit a vertex *v* :

- Mark vertex *v* as visited.

- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	F	–
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 0

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
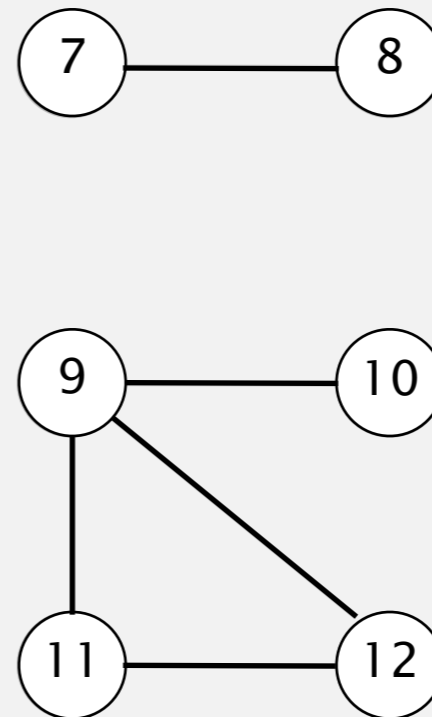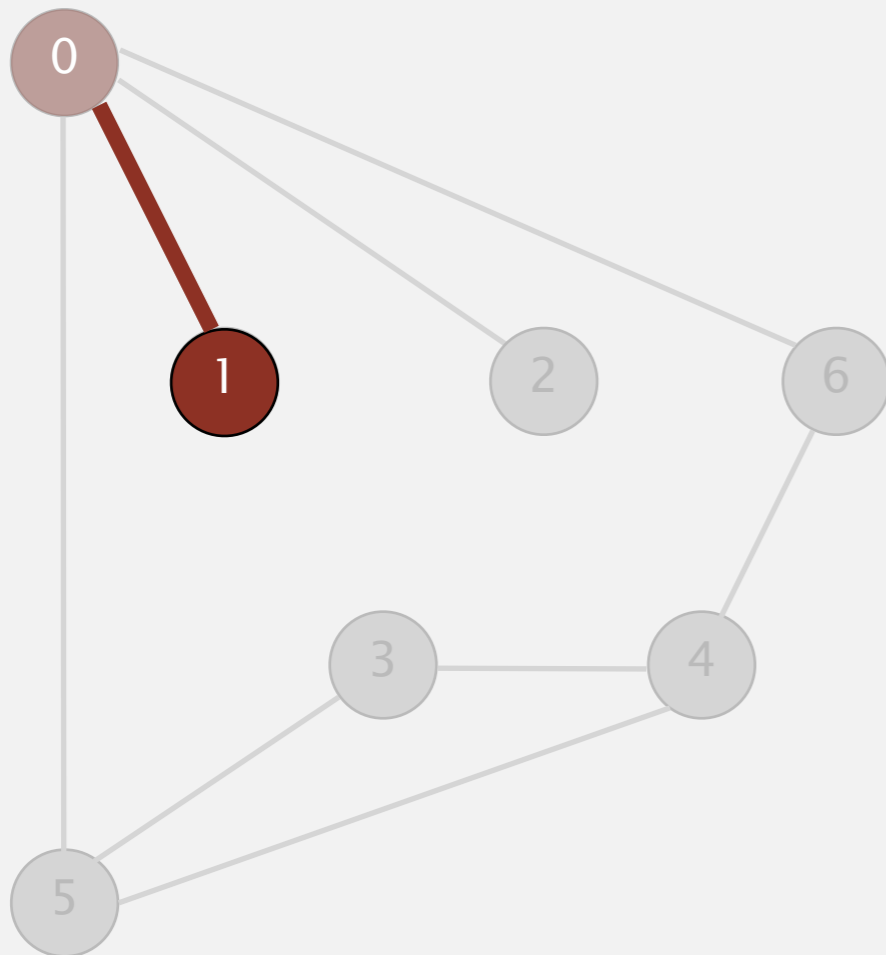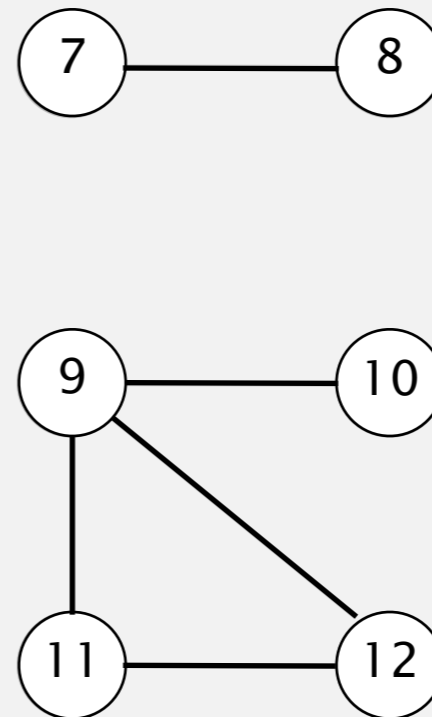- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 1

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
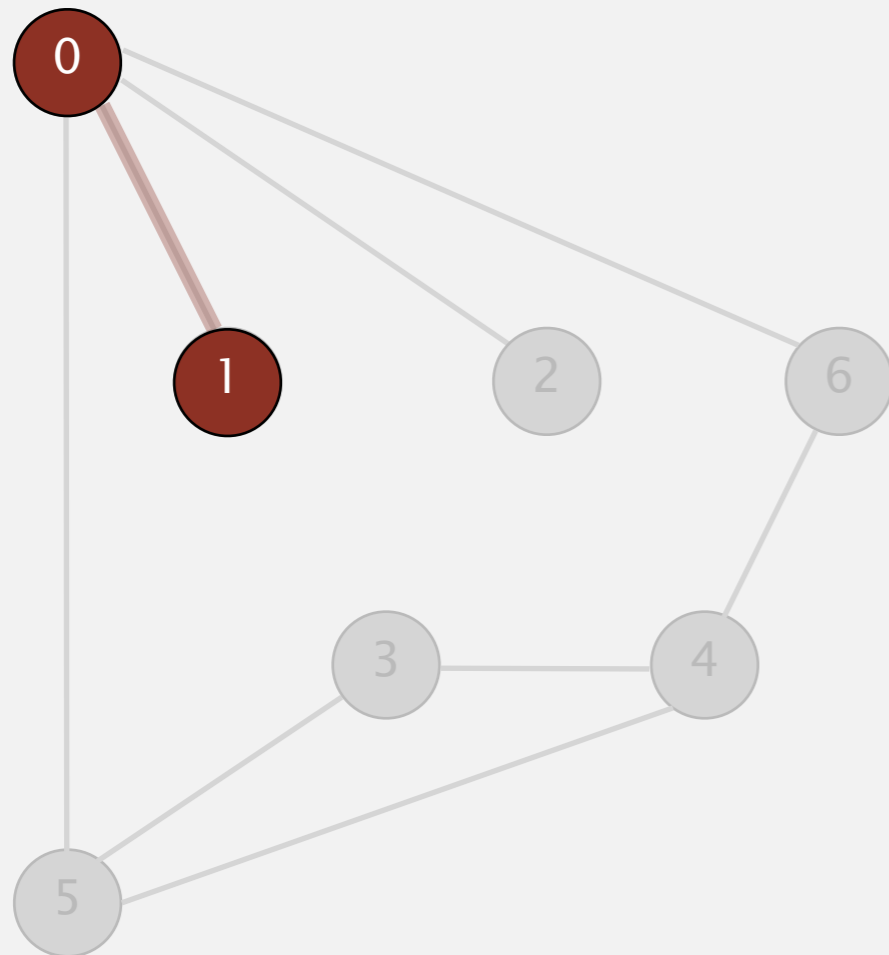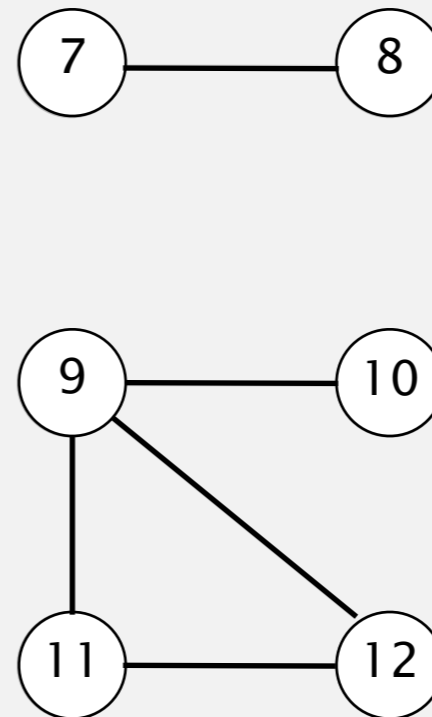
- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

1 done

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
- Recursively visit all unmarked vertices adjacent to *v*.

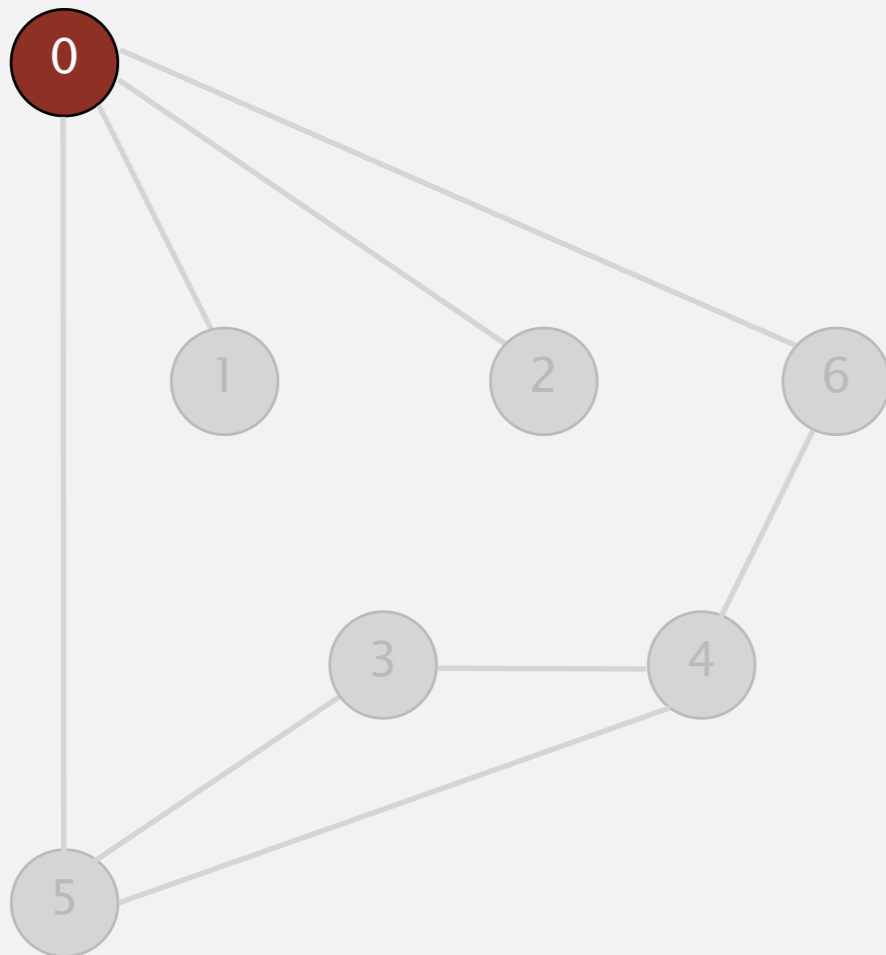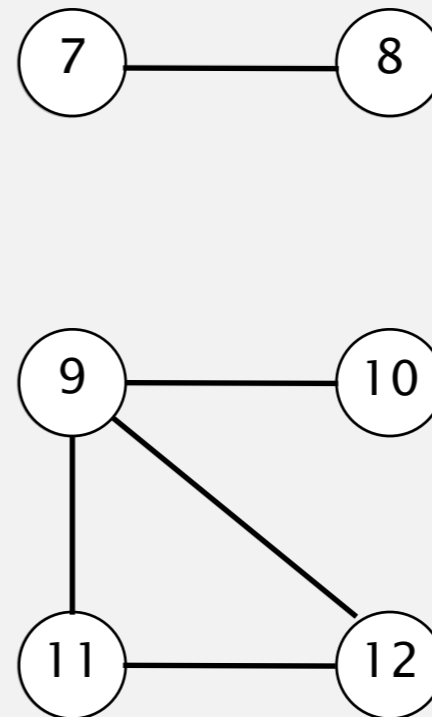| v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

0 done

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
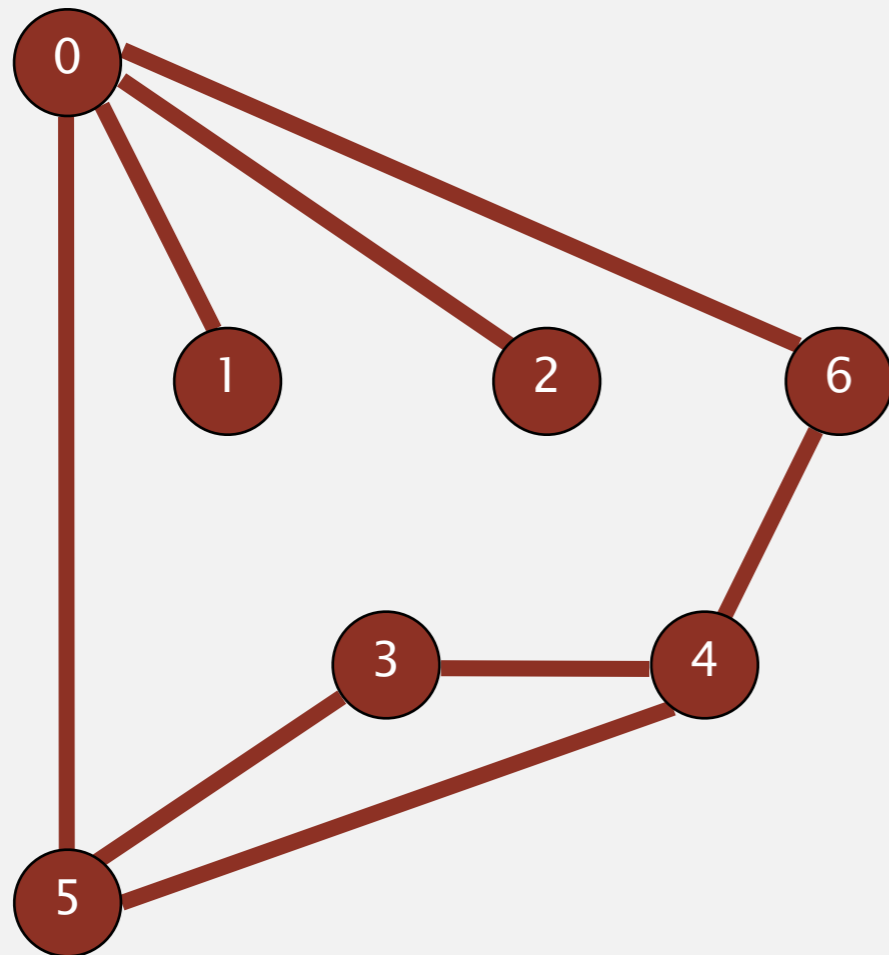
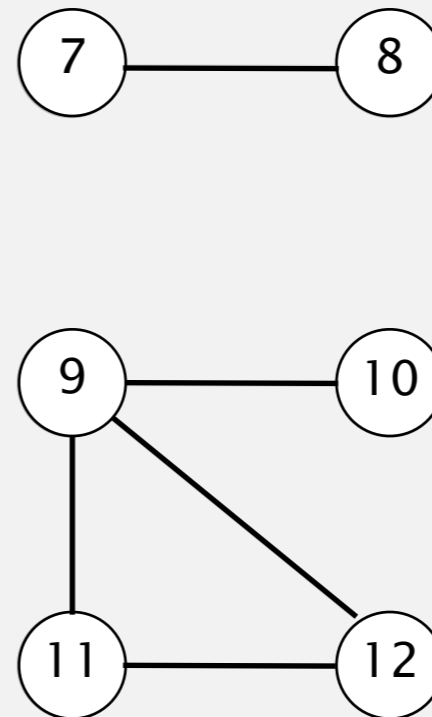- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

connected component

connected component: 0 1 2 3 4 5 6

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.

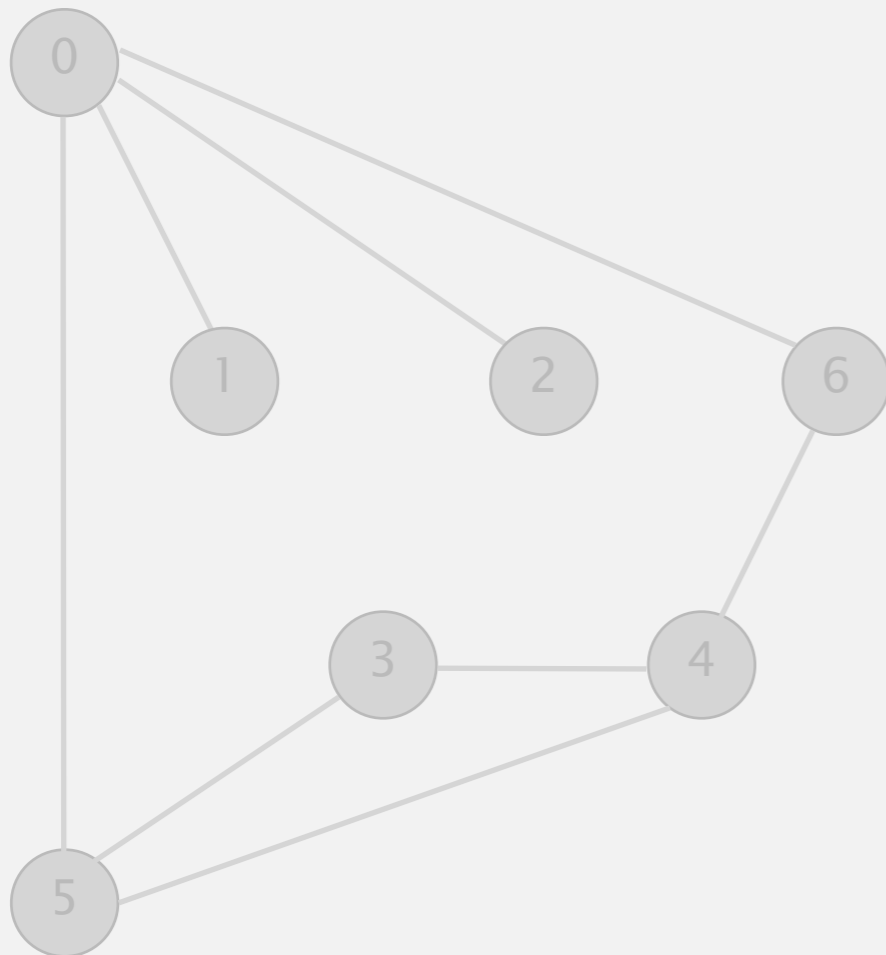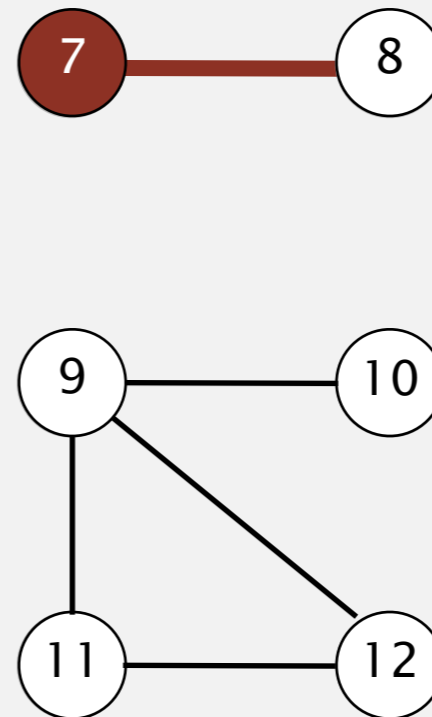- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	–
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

check 1 2 3 4 5 6

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
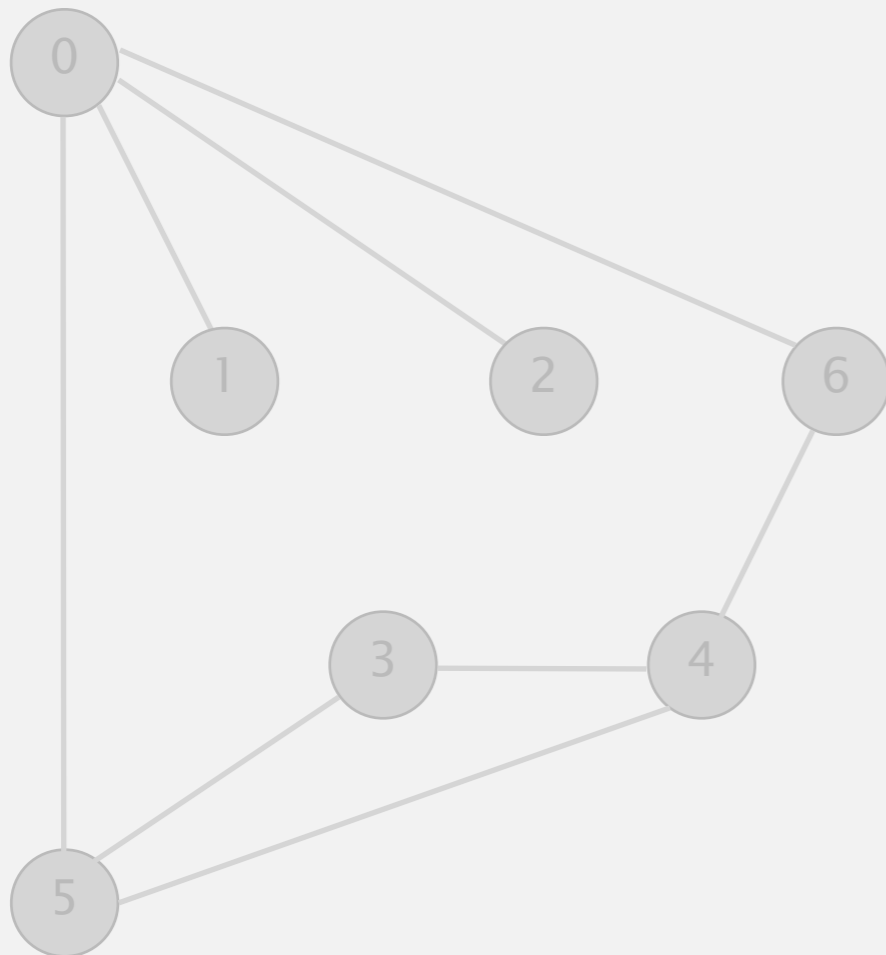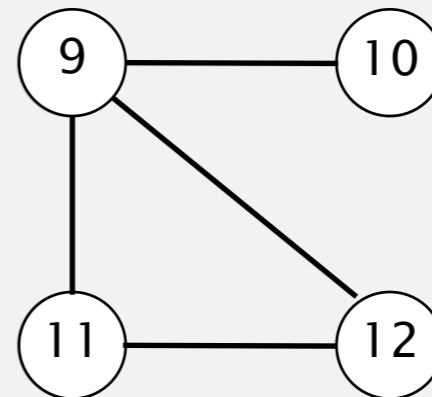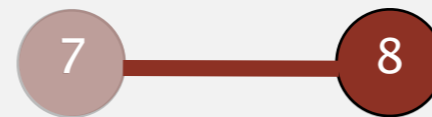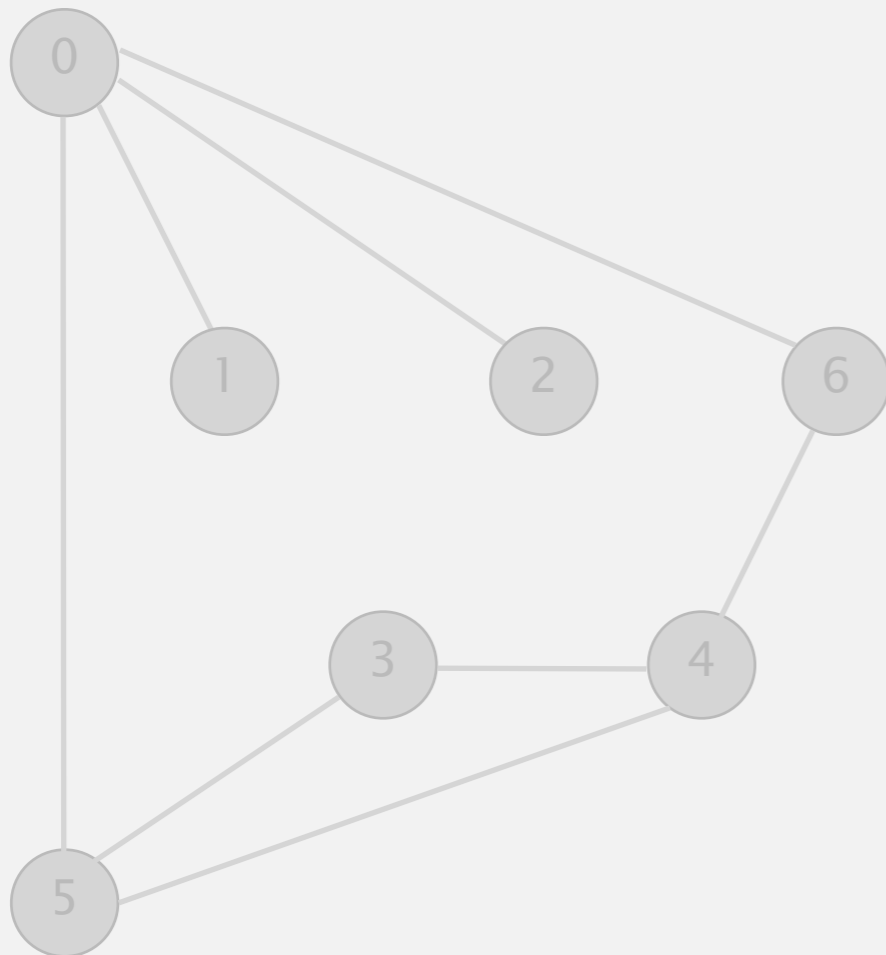- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	F	–
9	F	–
10	F	–
11	F	–
12	F	–

visit 7

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	F	–
10	F	–
11	F	–
12	F	–

visit 8

Connected components demo

To visit a vertex v :

- Mark vertex v as visited.
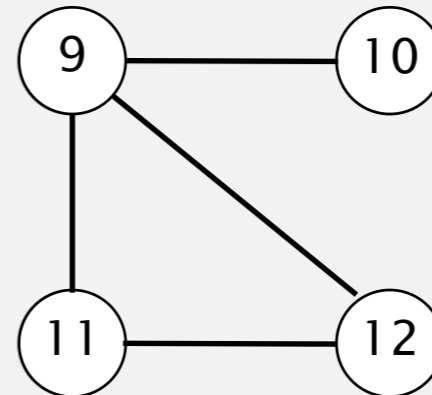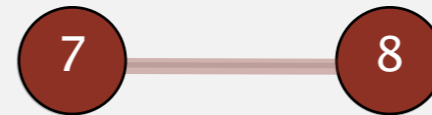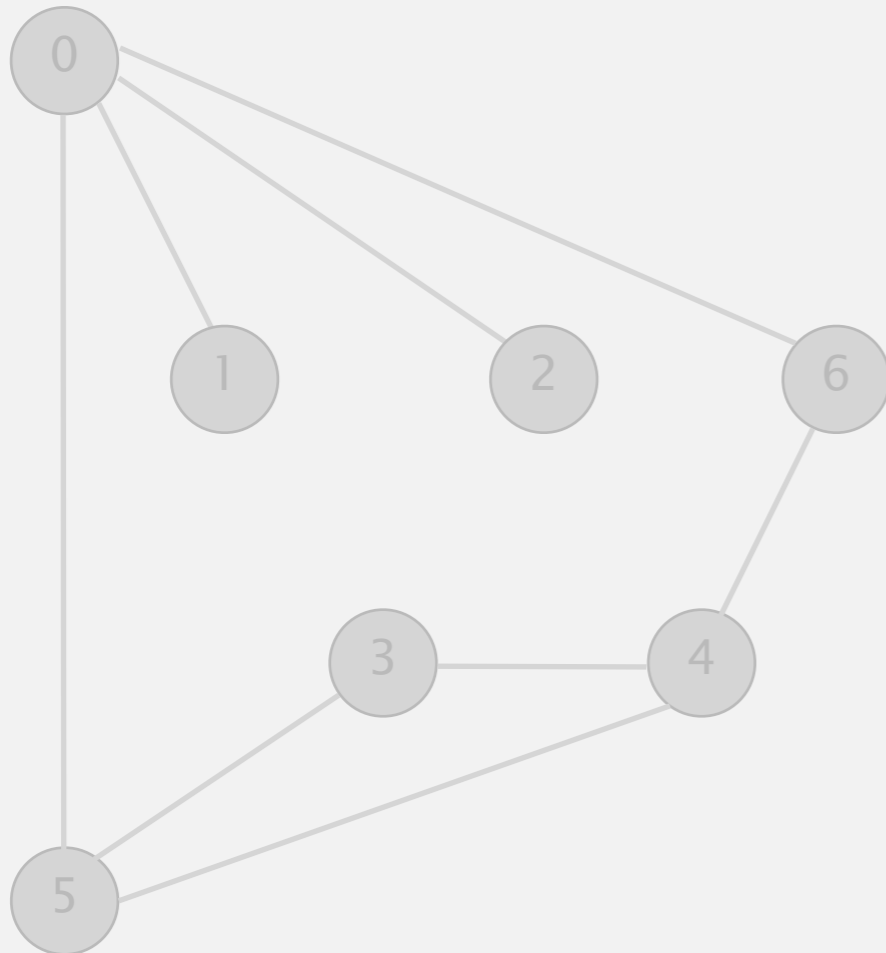- Recursively visit all unmarked vertices adjacent to v.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	F	–
10	F	–
11	F	–
12	F	–

8 done

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
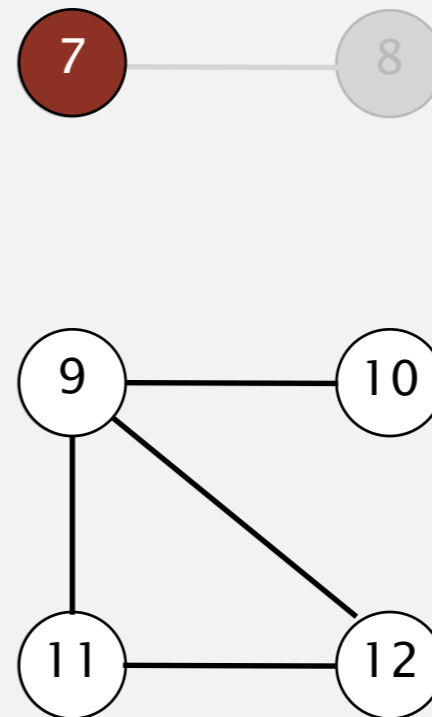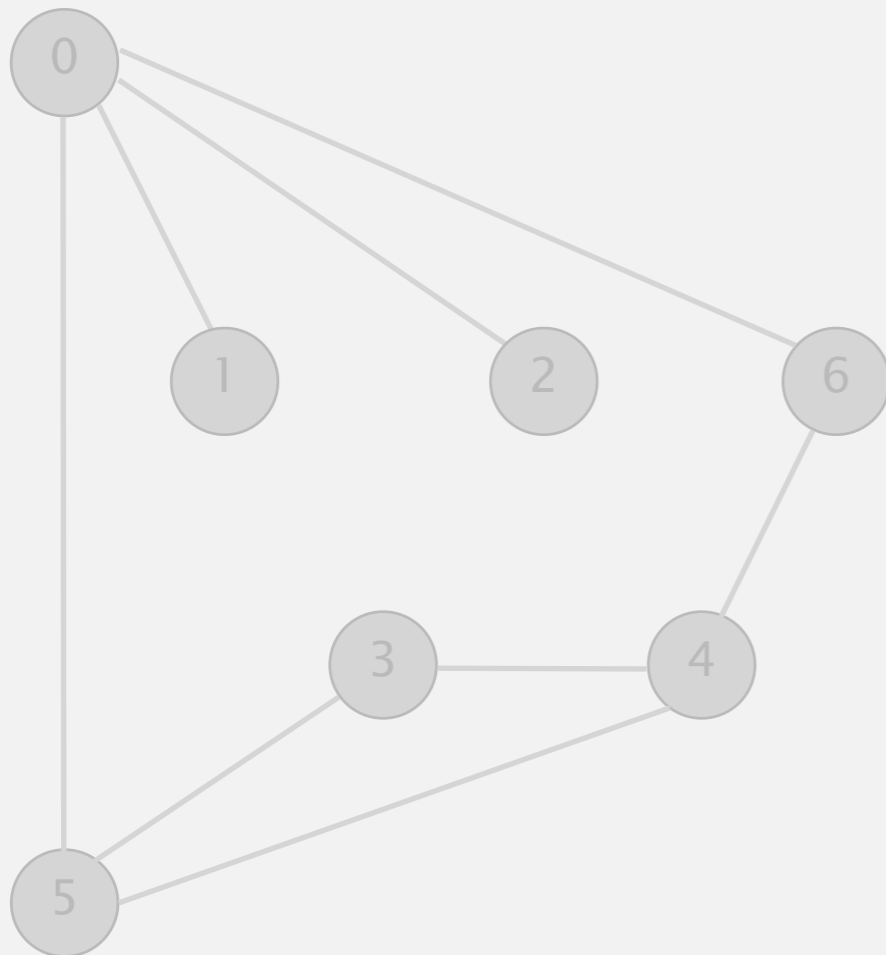- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	F	–
10	F	–
11	F	–
12	F	–

7 done

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
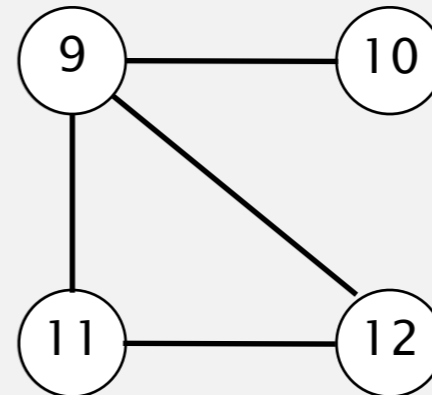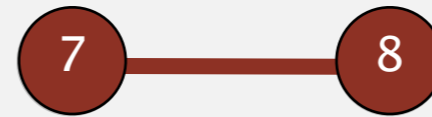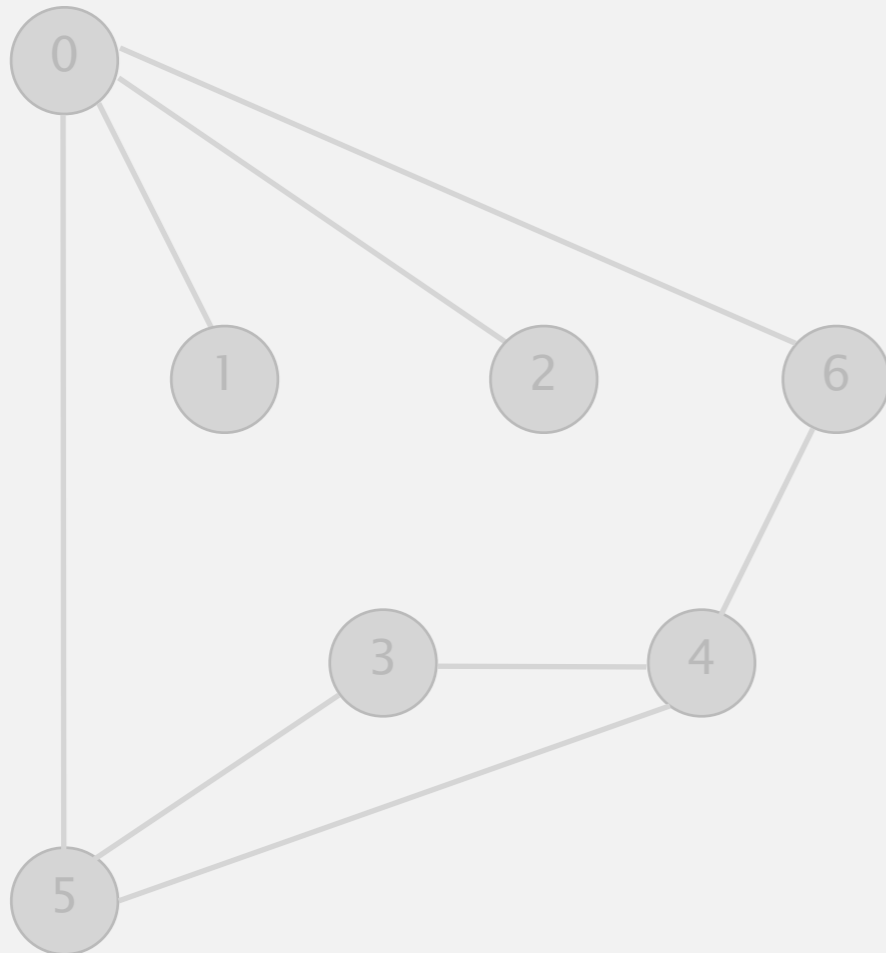- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	F	–
10	F	–
11	F	–
12	F	–

connected component: 7 8

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
- Recursively visit all unmarked vertices adjacent to *v*.

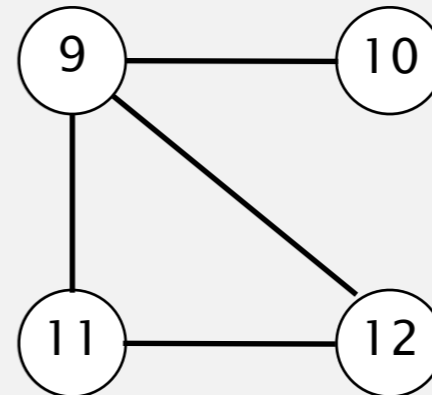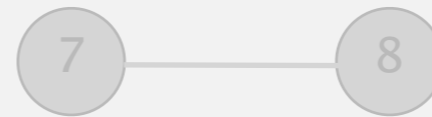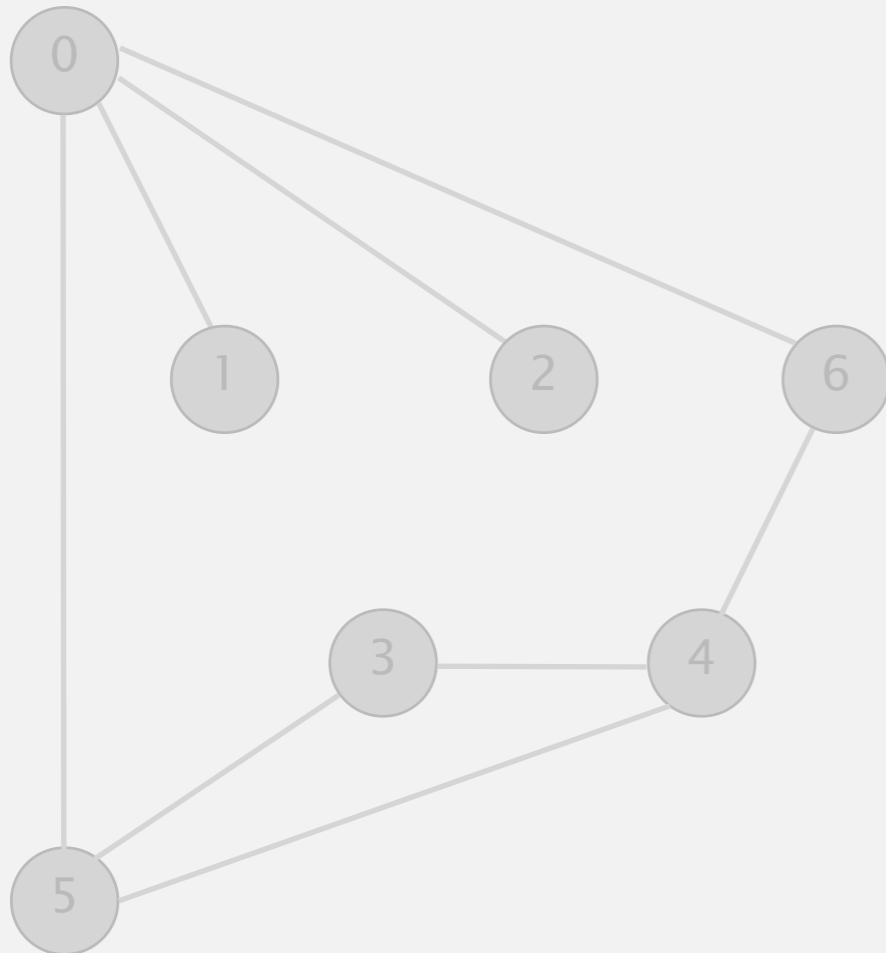| v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	F	–
10	F	–
11	F	–
12	F	–

check 8

To visit a vertex *v* :

- Mark vertex *v* as visited.
- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	–
11	F	–
12	F	–

visit 9

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
- Recursively visit all unmarked vertices adjacent to *v*.

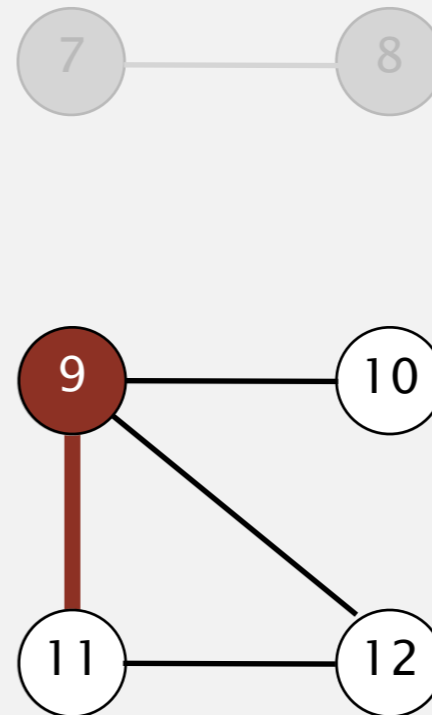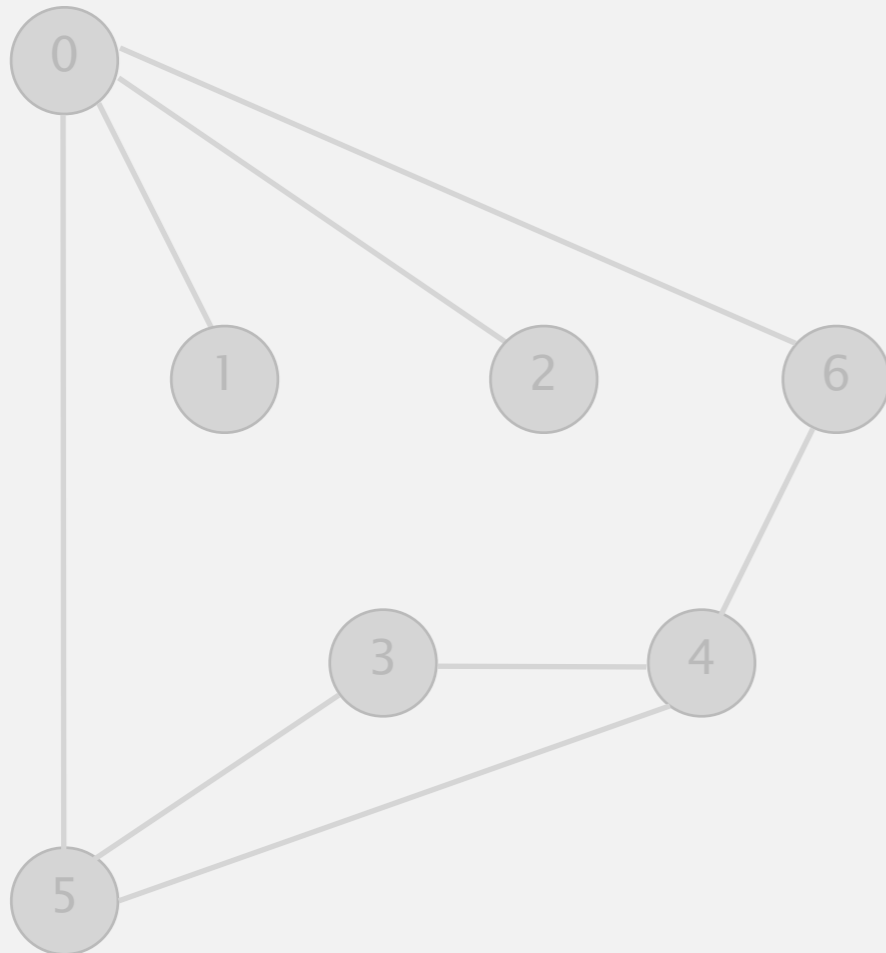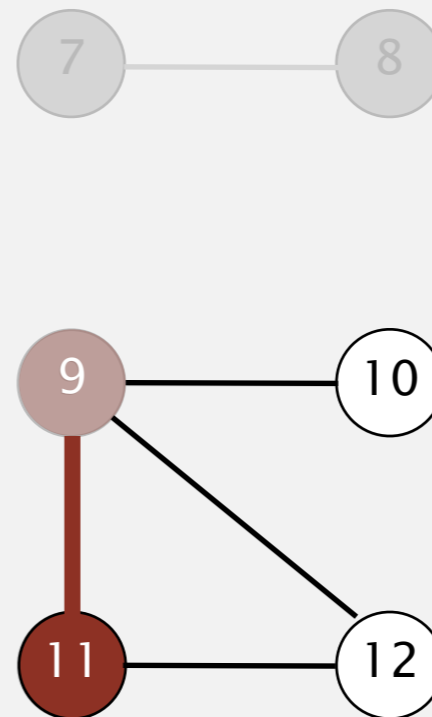

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	–
11	T	2
12	F	–

visit 11

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.

- Recursively visit all unmarked vertices adjacent to *v*.

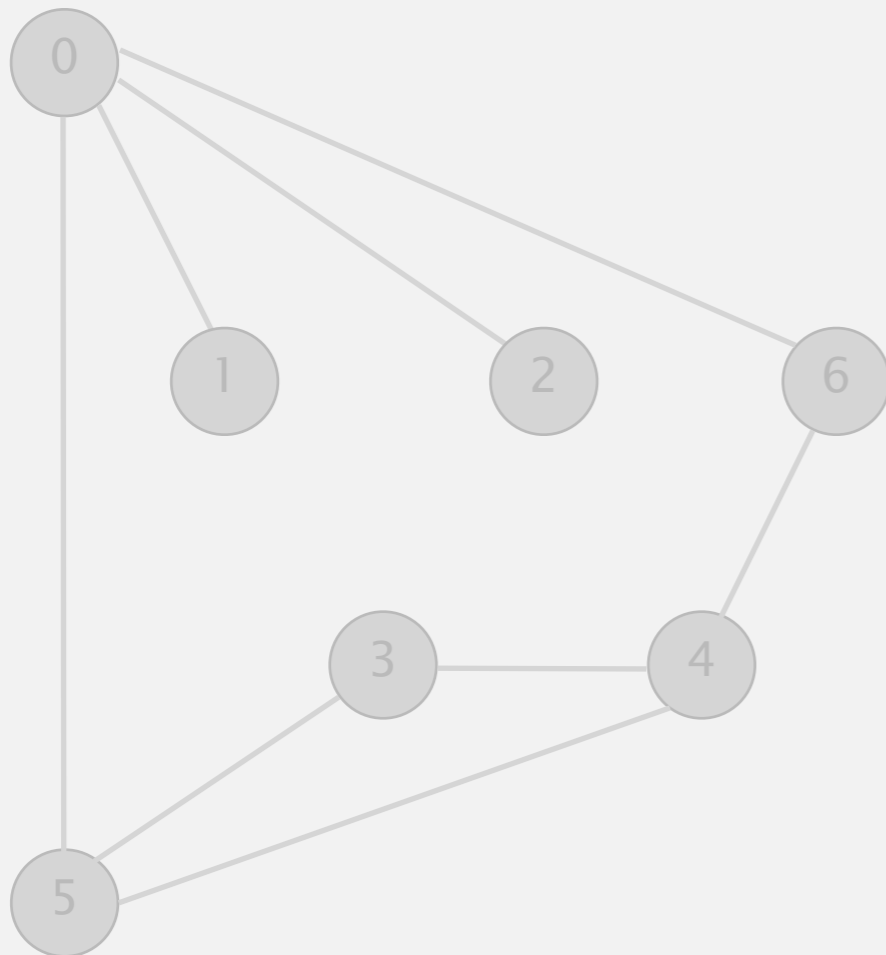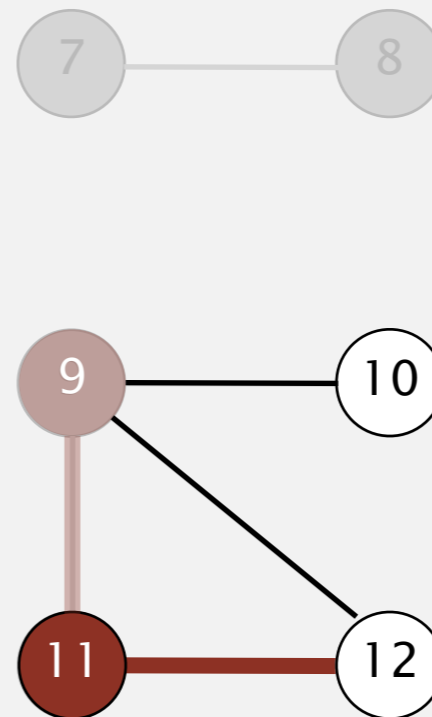| v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	–
11	T	2
12	F	–

visit 11

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
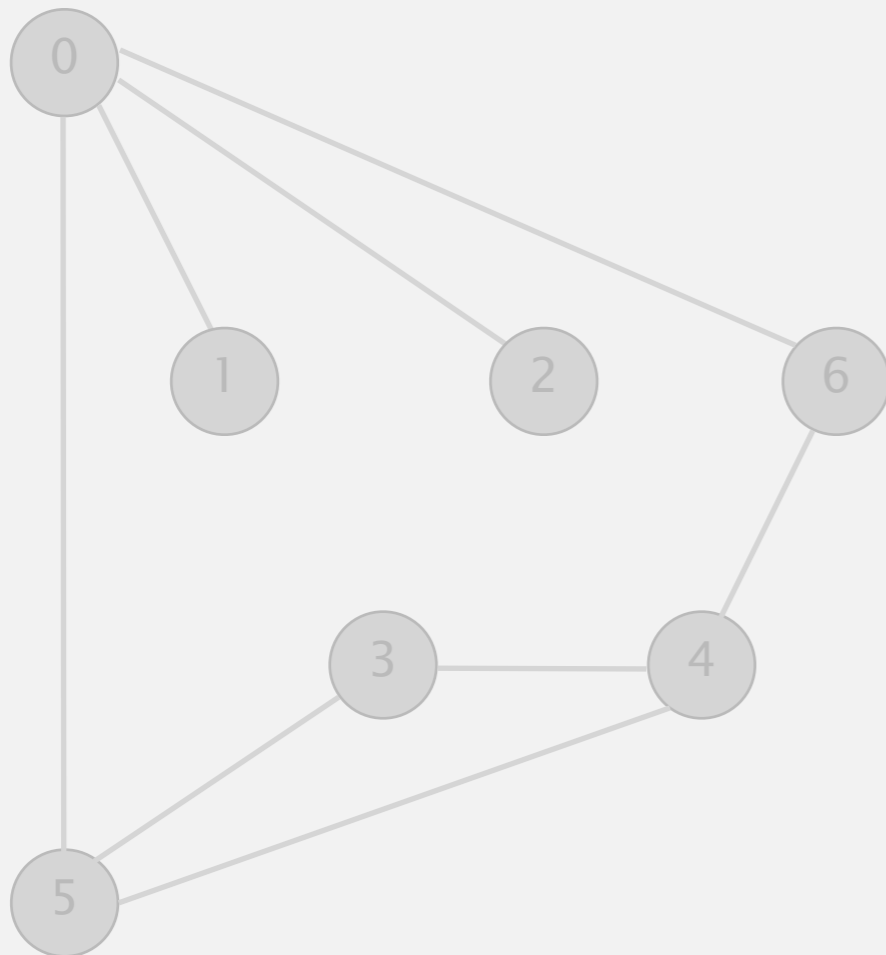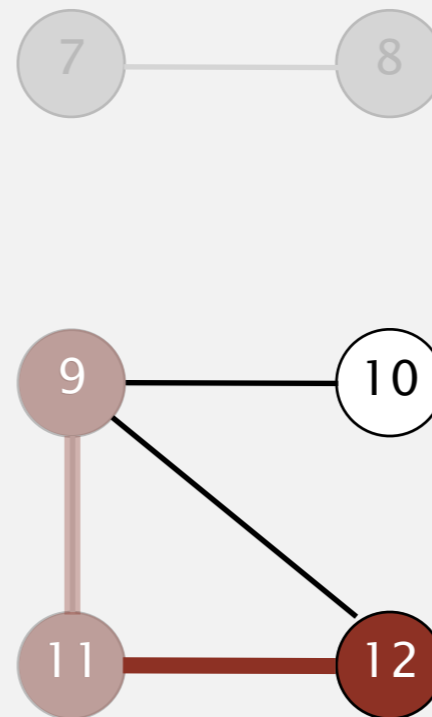- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	–
11	T	2
12	T	2

visit 12

Connected components demo

To visit a vertex v :

- Mark vertex v as visited.
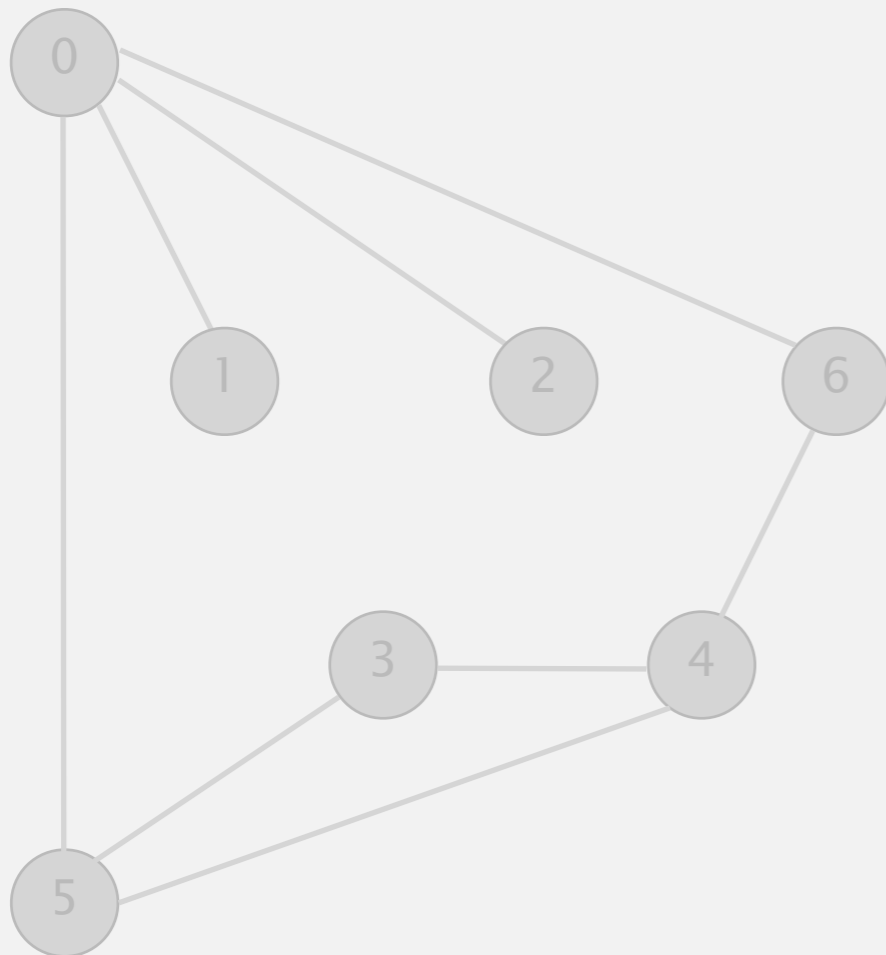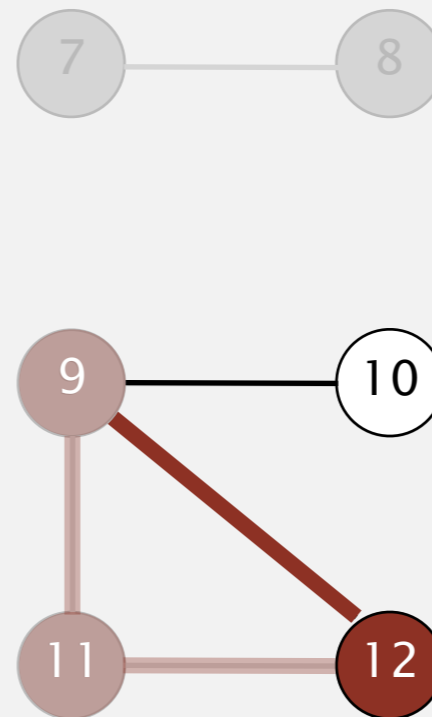- Recursively visit all unmarked vertices adjacent to v.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	–
11	T	2
12	T	2

visit 12

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
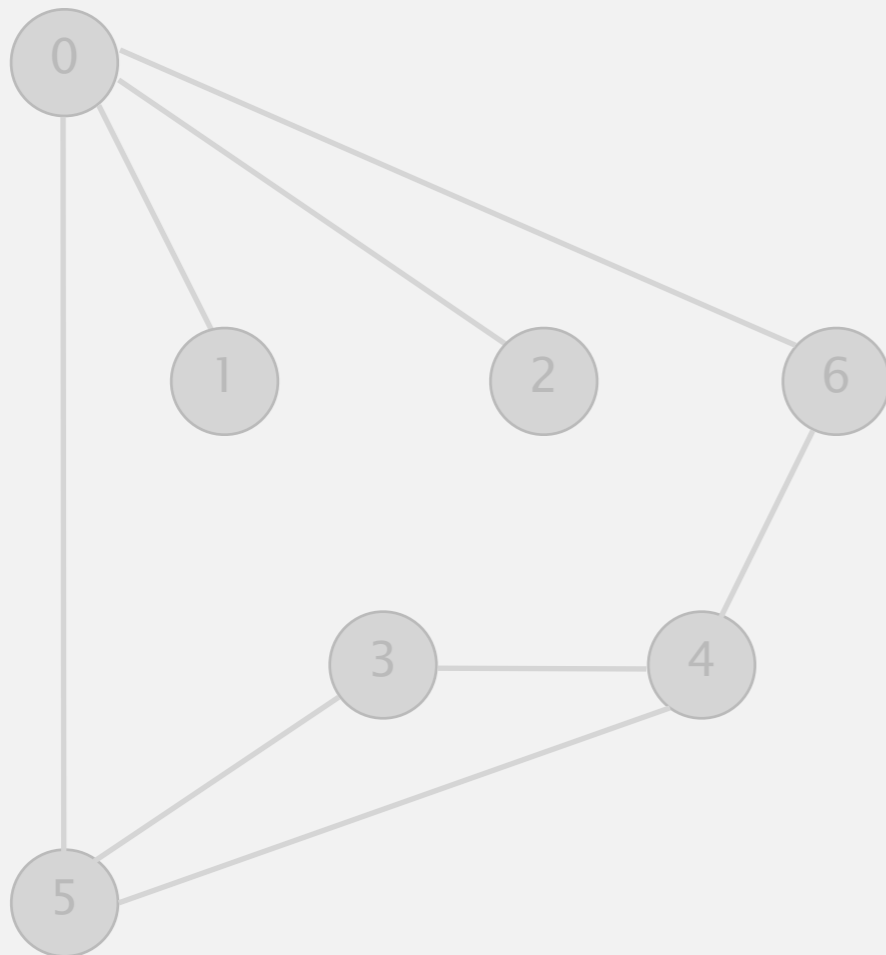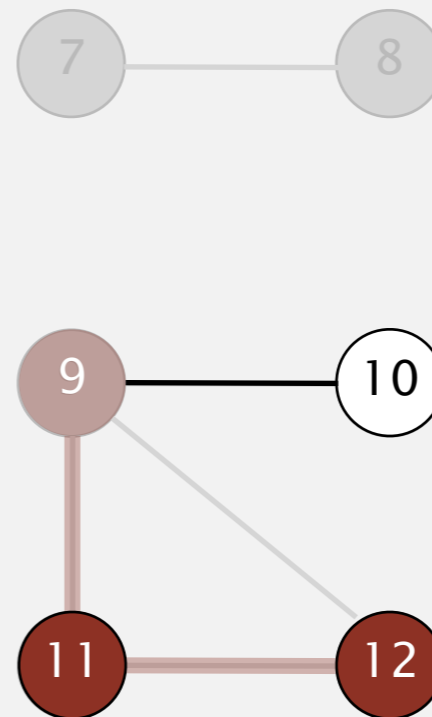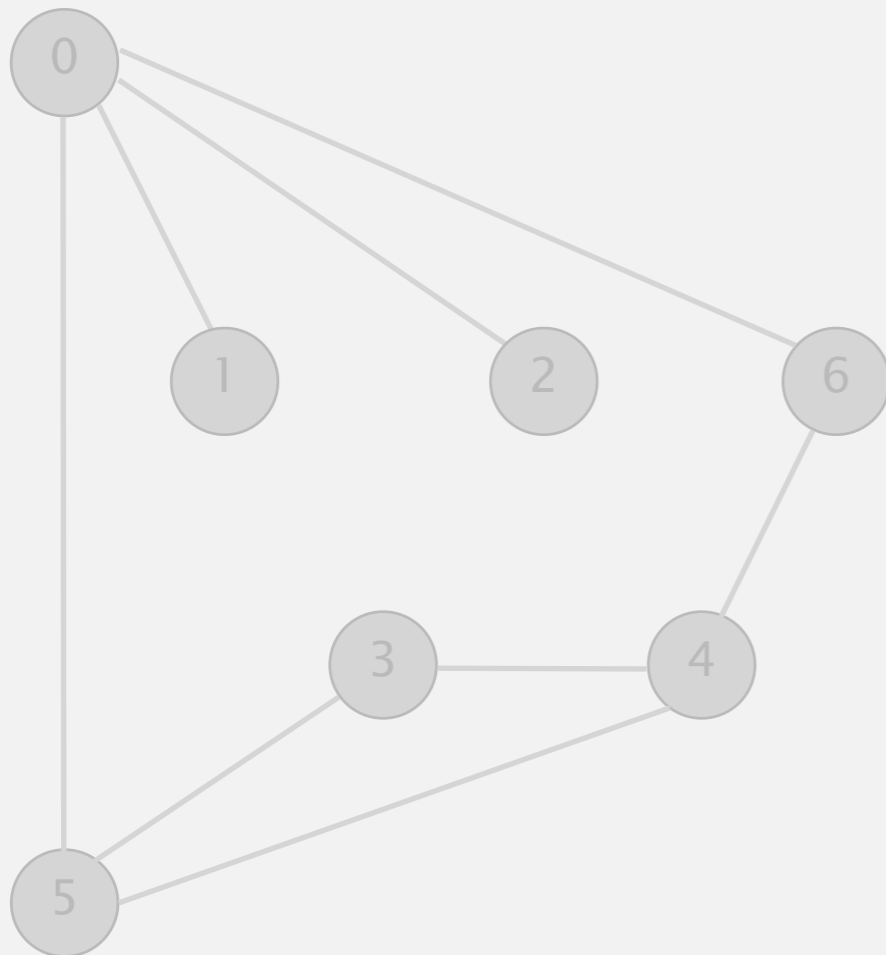- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	–
11	T	2
12	T	2

12 done

Connected components demo

To visit a vertex v :

- Mark vertex v as visited.
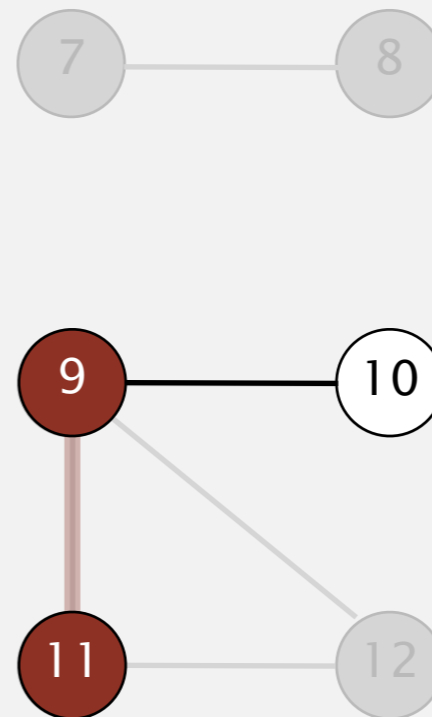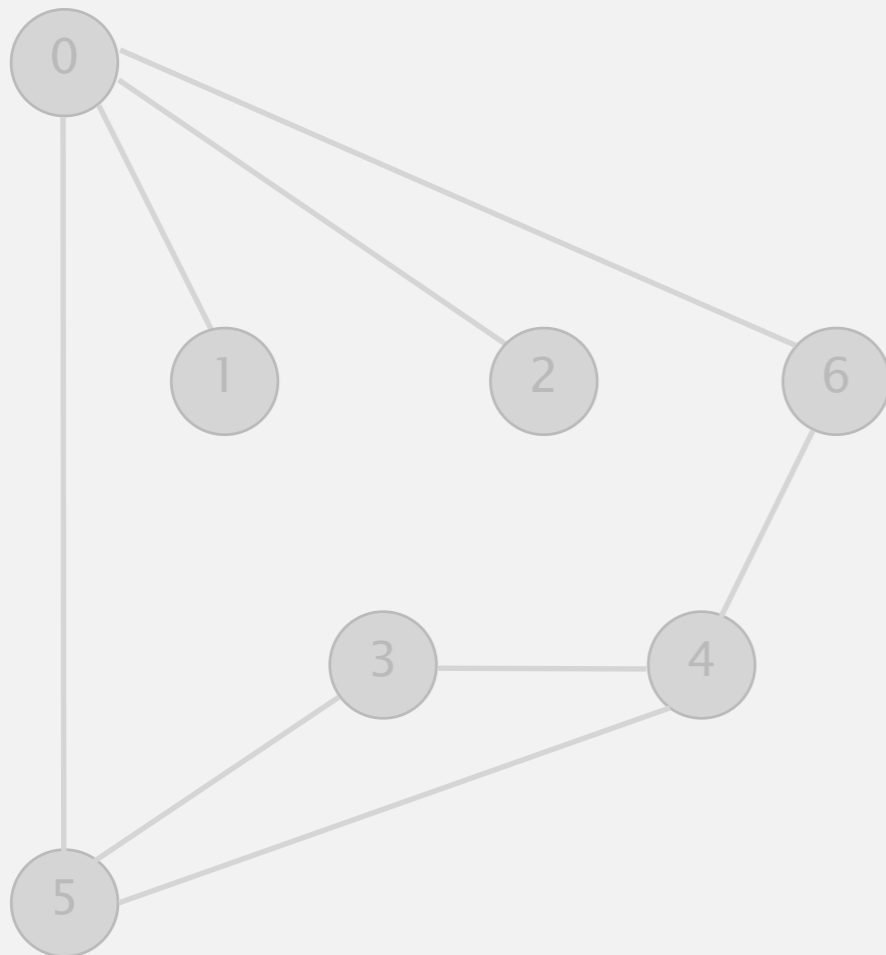- Recursively visit all unmarked vertices adjacent to v.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	–
11	T	2
12	T	2

11 done

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.

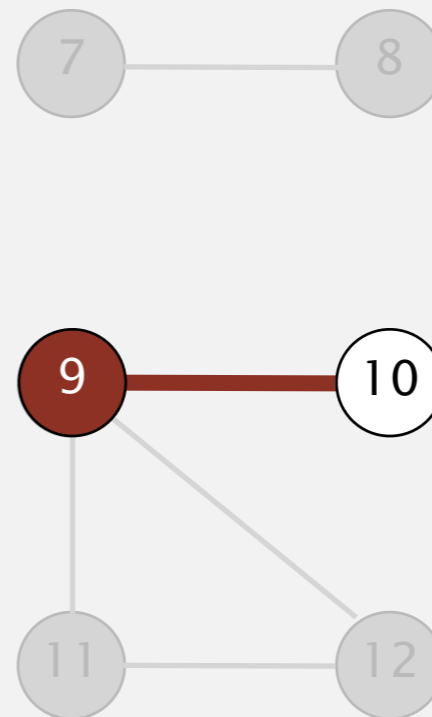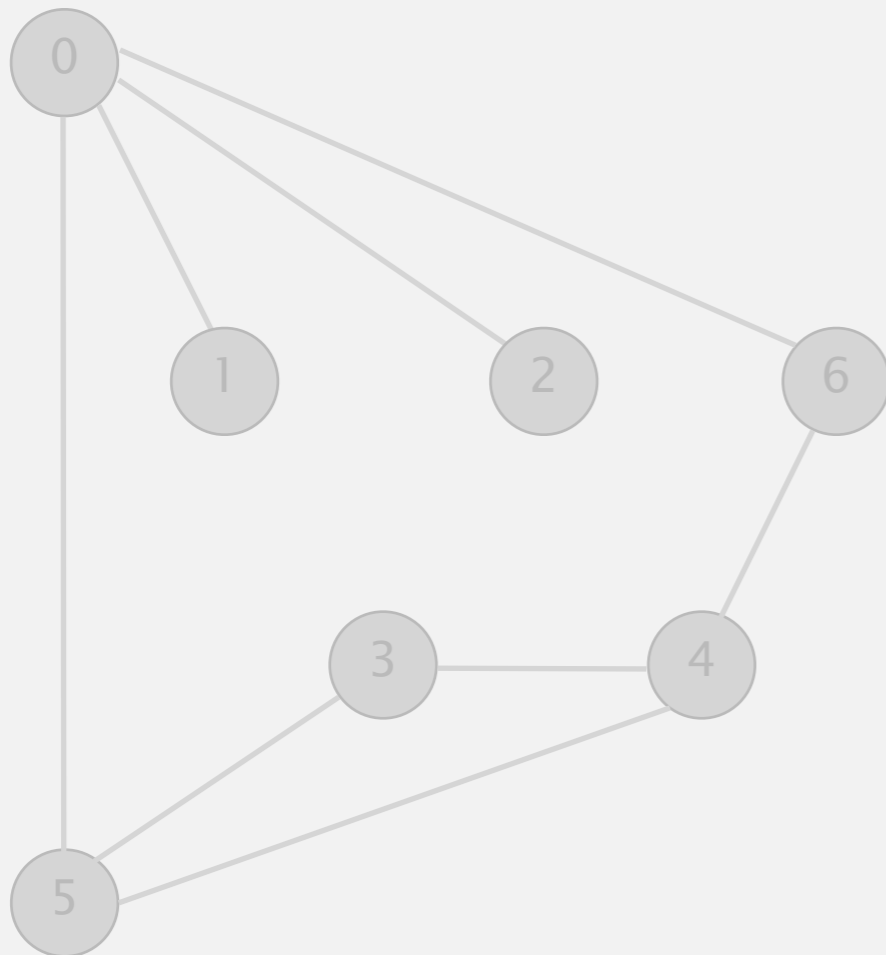- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	–
11	T	2
12	T	2

visit 9

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
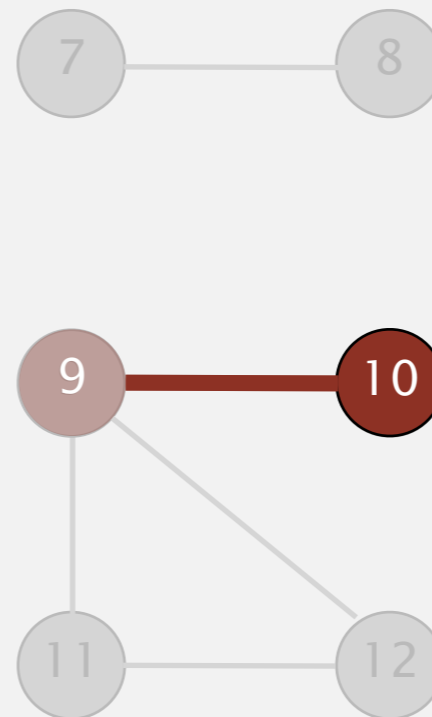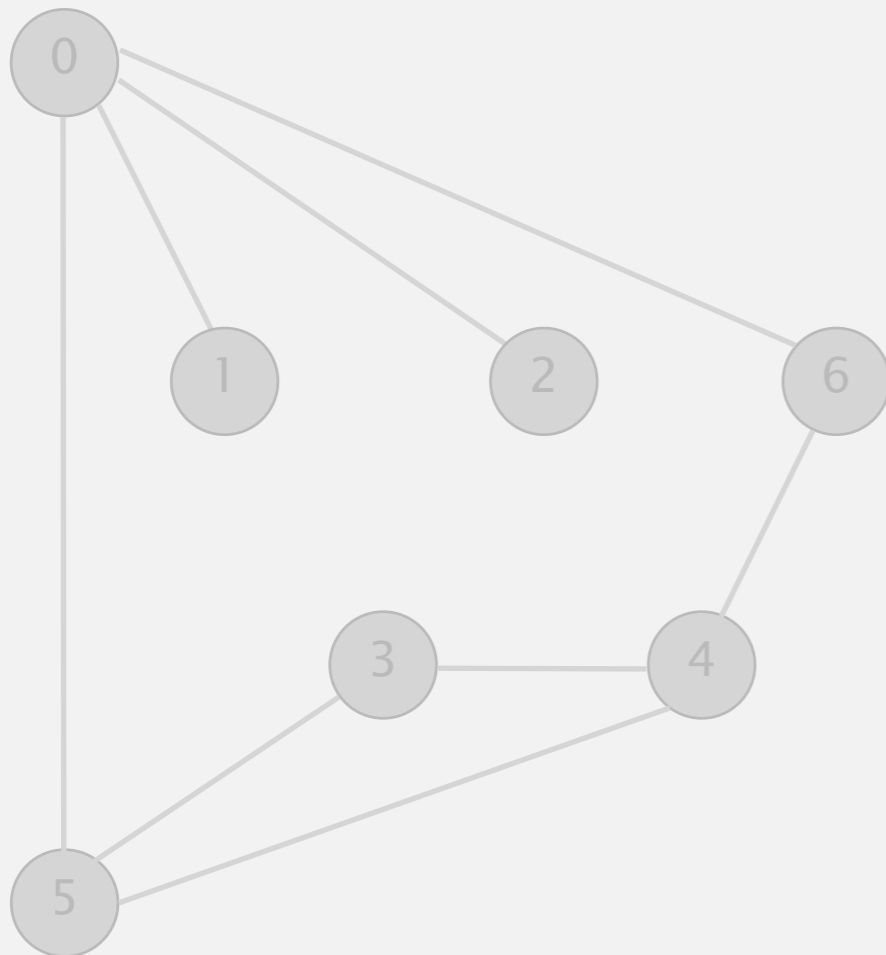
- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	T	2
11	T	2
12	T	2

visit 10

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.

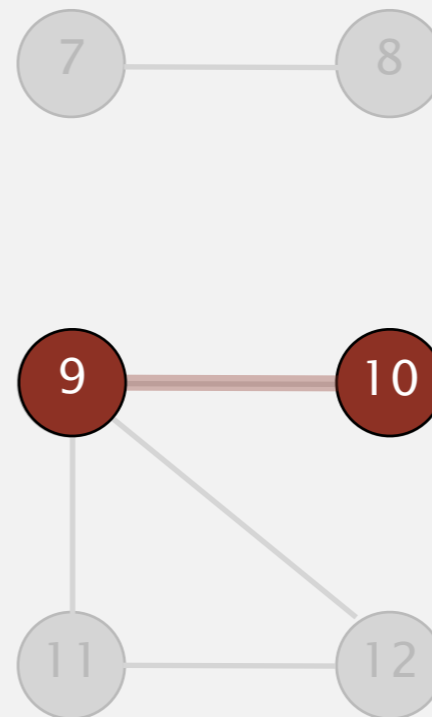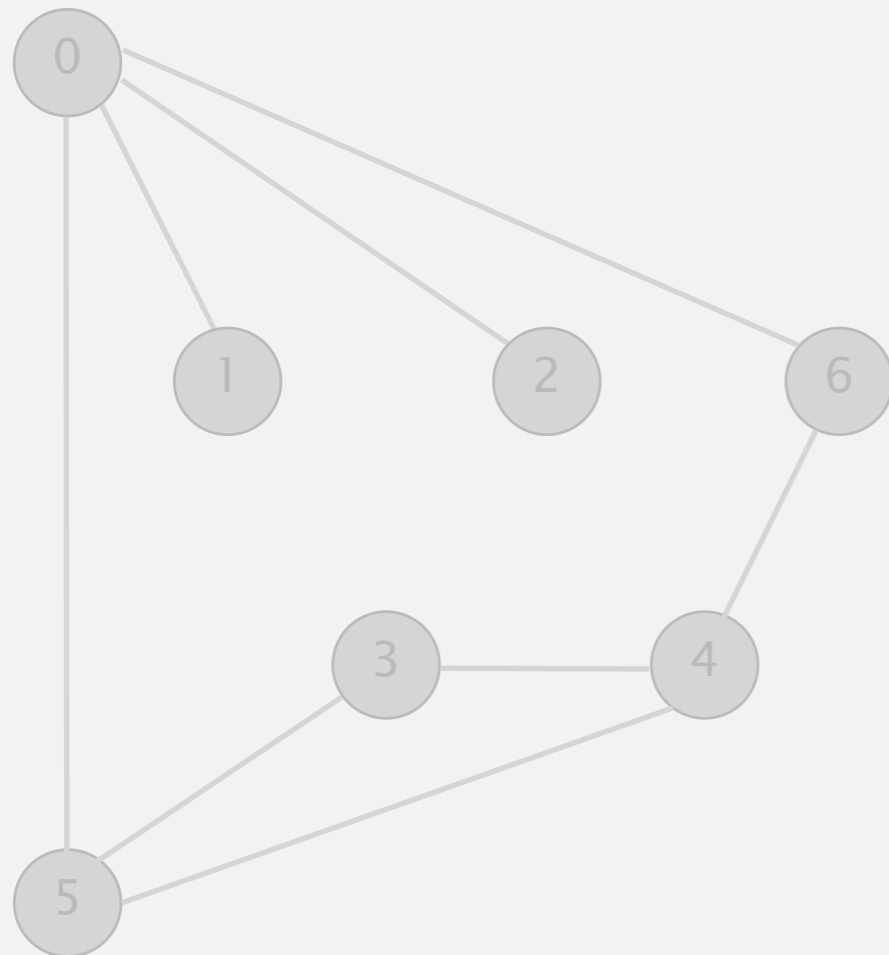- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	T	2
11	T	2
12	T	2

10 done

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
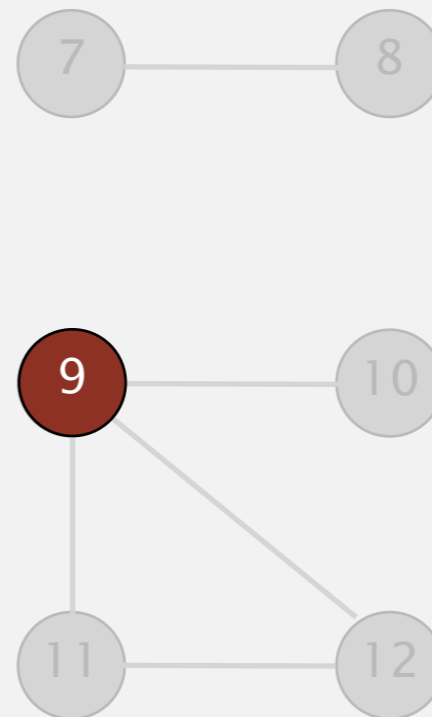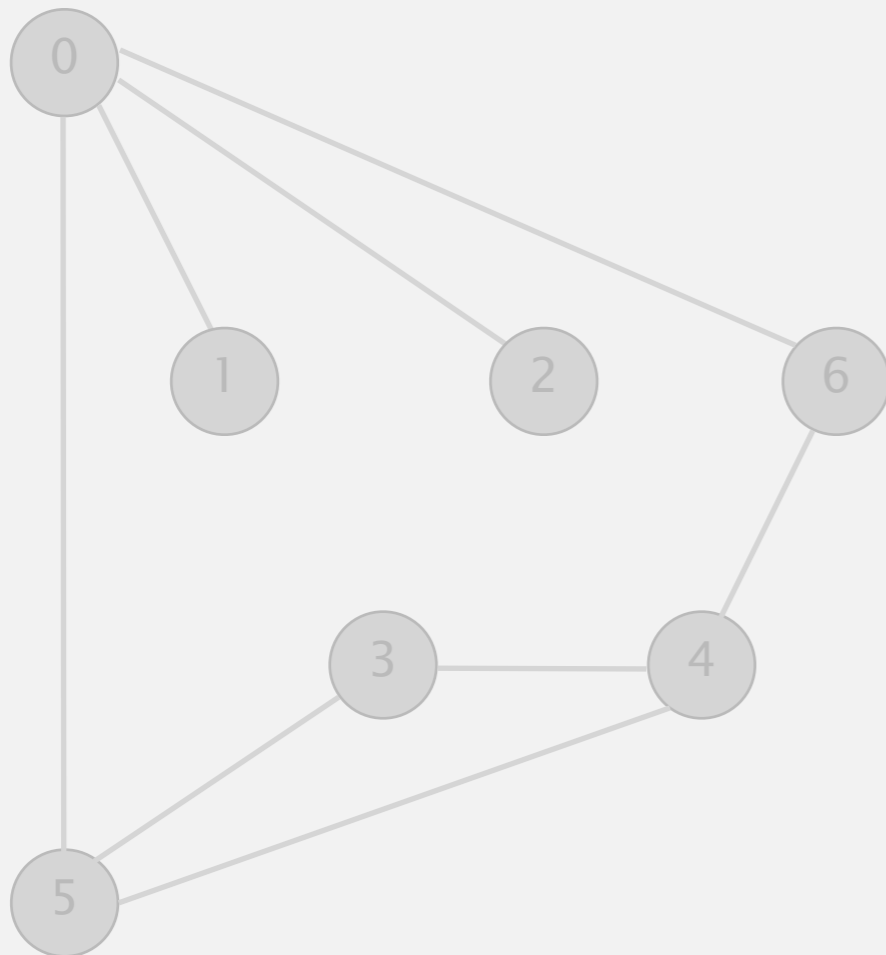- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	T	2
11	T	2
12	T	2

9 done

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
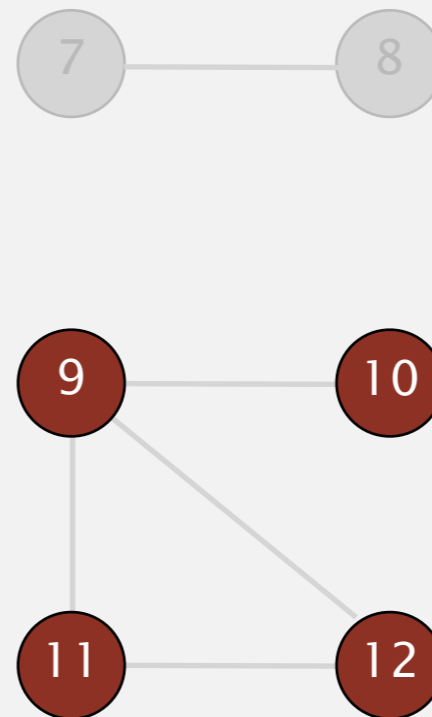
- Recursively visit all unmarked vertices adjacent to *v*.
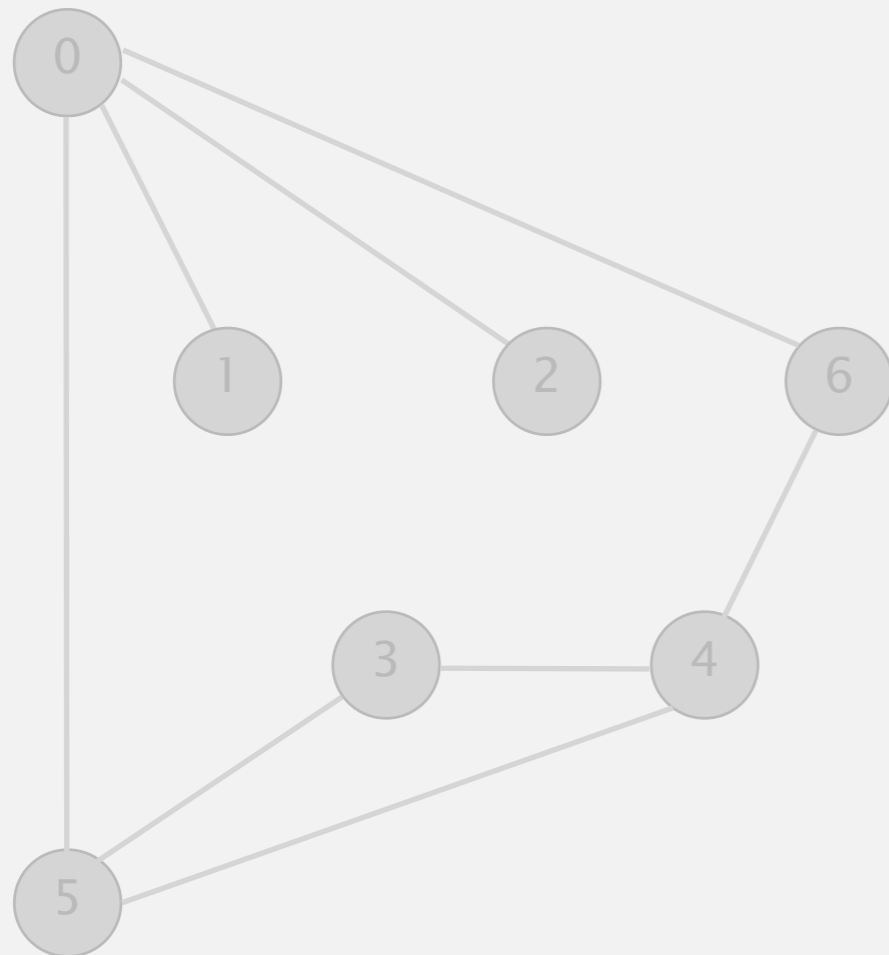

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	T	2
11	T	2
12	T	2

connected component: 9 10 11 12

Connected components demo

To visit a vertex *v* :

- Mark vertex *v* as visited.
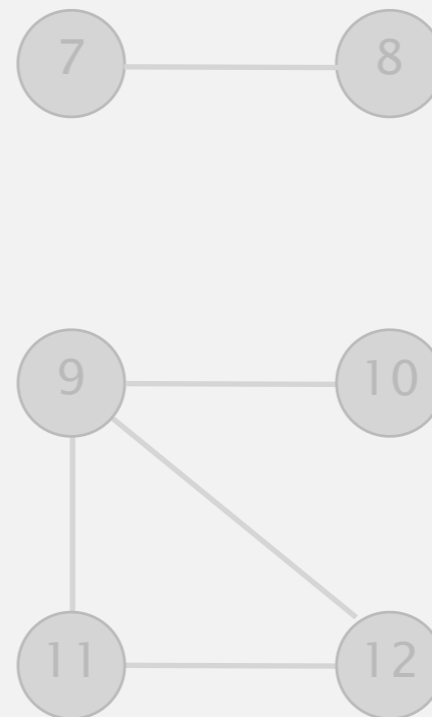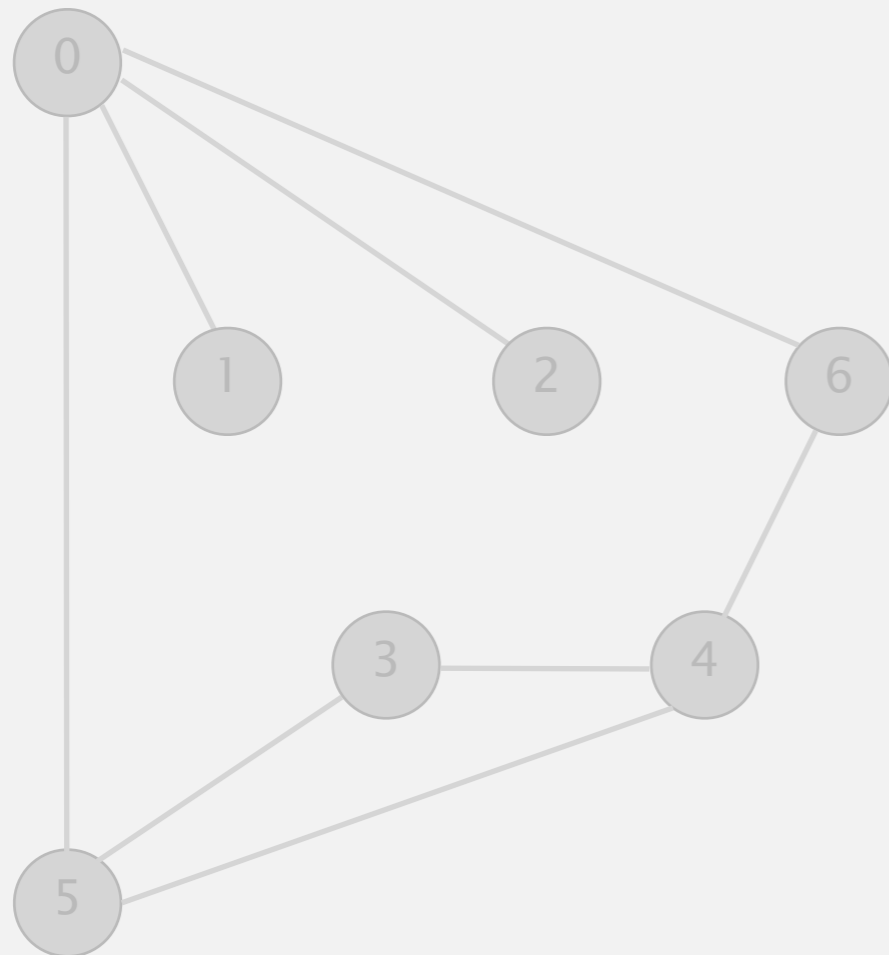- Recursively visit all unmarked vertices adjacent to *v*.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	T	2
11	T	2
12	T	2

check 10 11 12

Connected components demo

To visit a vertex v :

- Mark vertex v as visited.
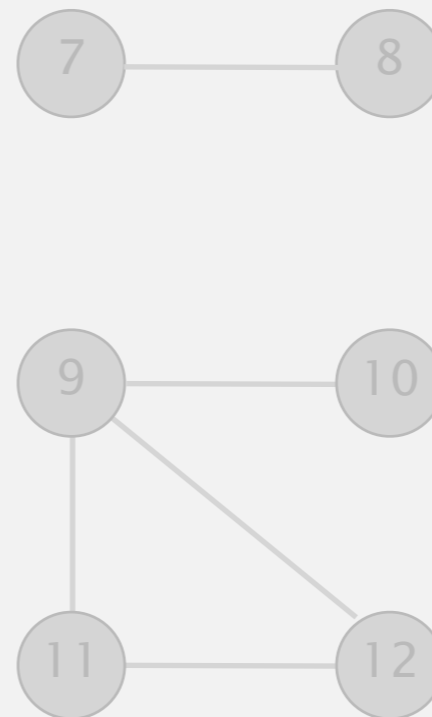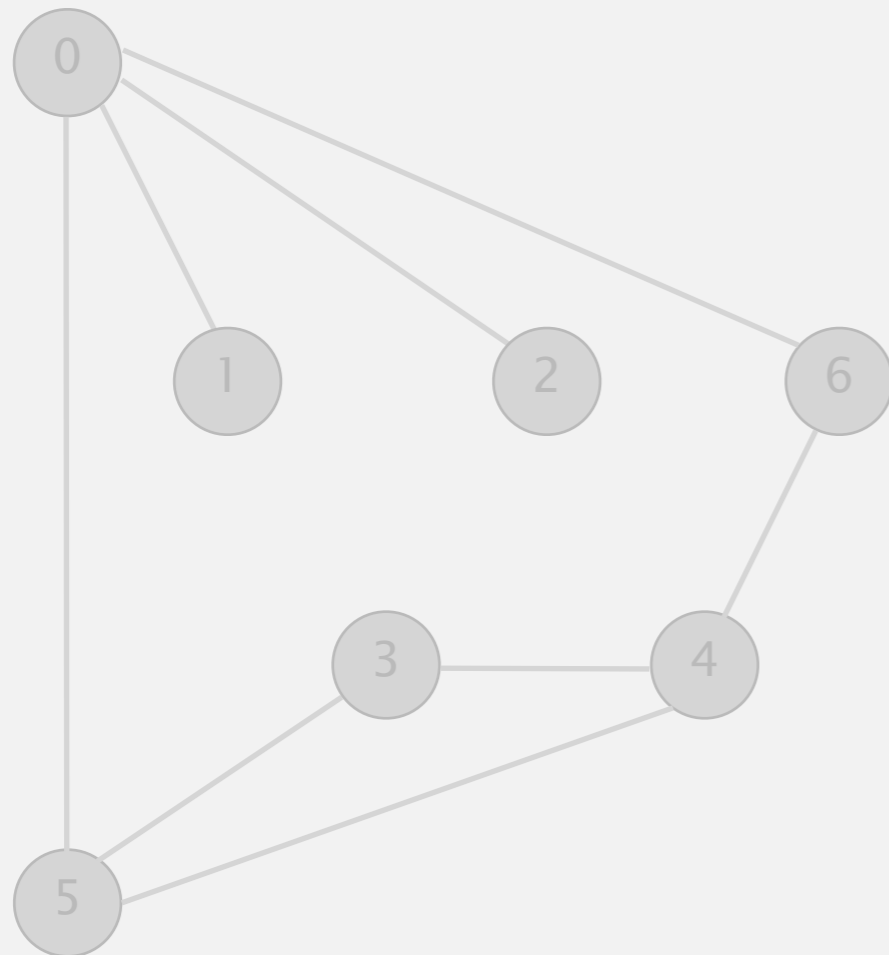- Recursively visit all unmarked vertices adjacent to v.

v	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	T	2
11	T	2
12	T	2

done