

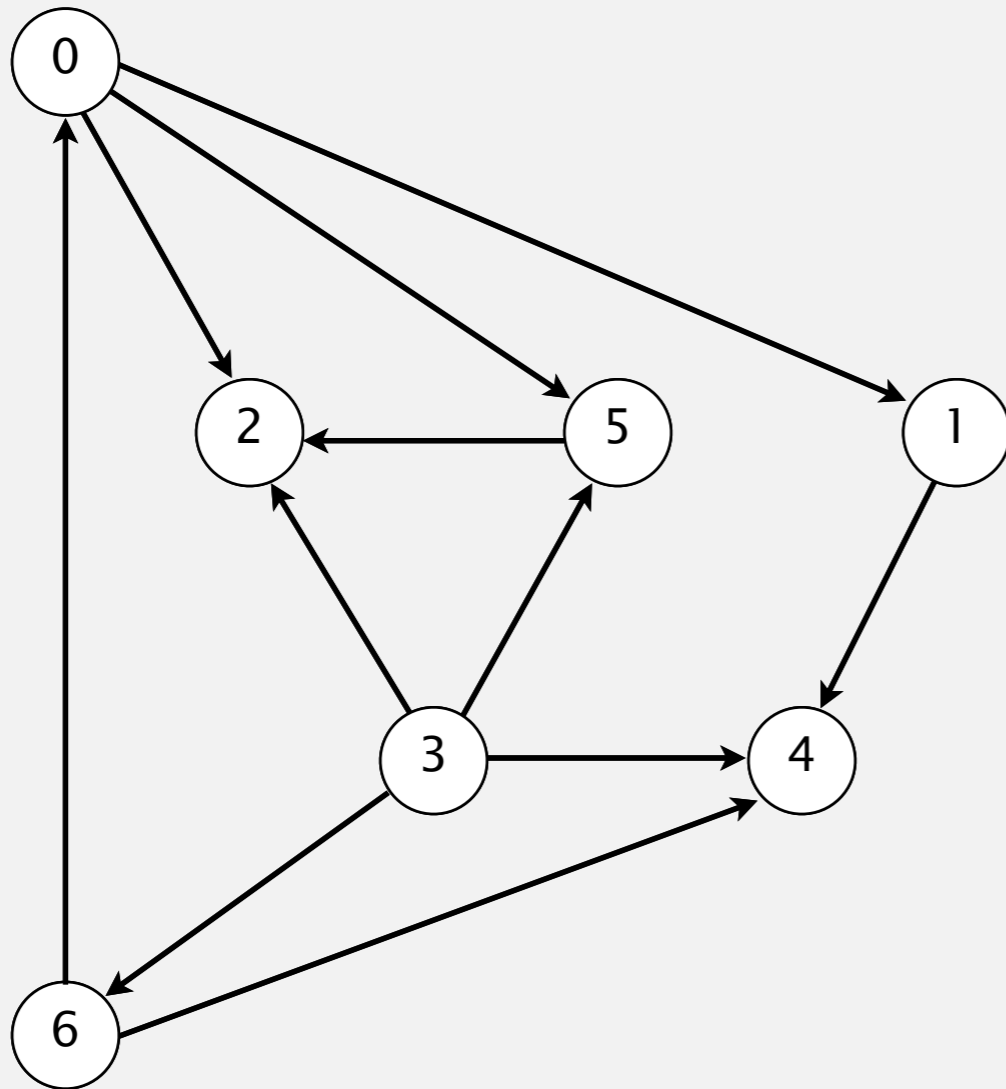


4.2 TOPOLOGICAL SORT DEMO

<http://algs4.cs.princeton.edu>

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



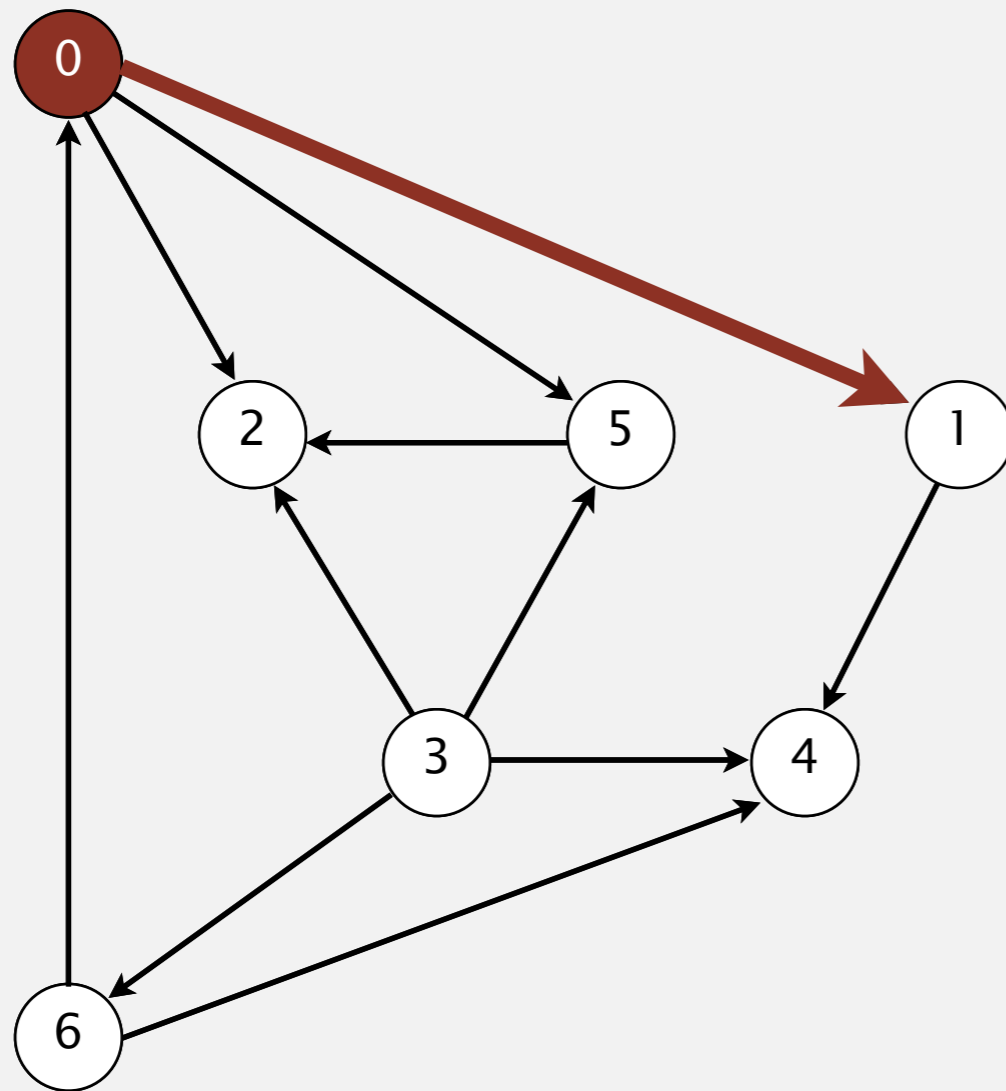
tinyDAG7.txt

```
7
11
0 5
0 2
0 1
3 6
3 5
3 4
5 2
6 4
6 0
3 2
```

a directed acyclic graph

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



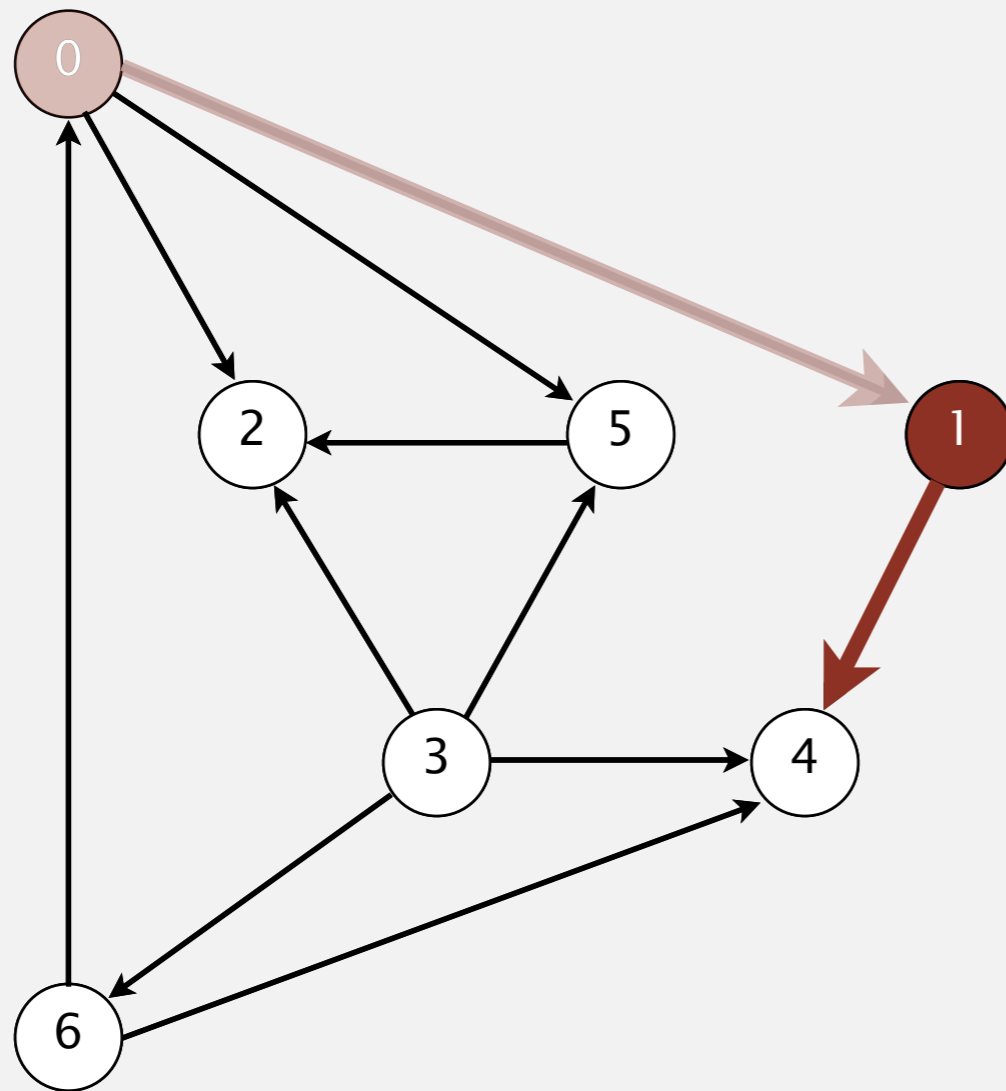
postorder

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | F |
| 2 | F |
| 3 | F |
| 4 | F |
| 5 | F |
| 6 | F |

visit 0: check 1, check 2, and check 5

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



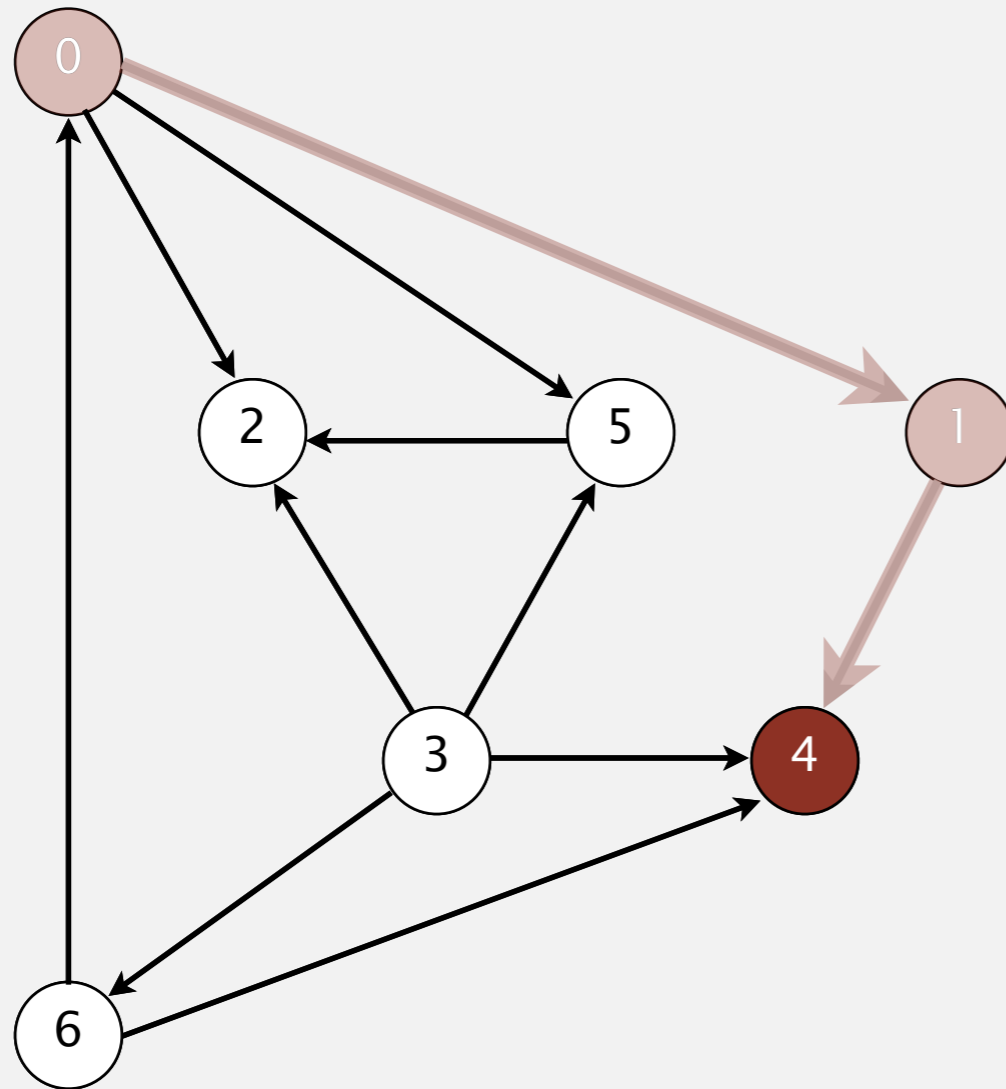
postorder

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | F |
| 3 | F |
| 4 | F |
| 5 | F |
| 6 | F |

visit 1: check 4

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



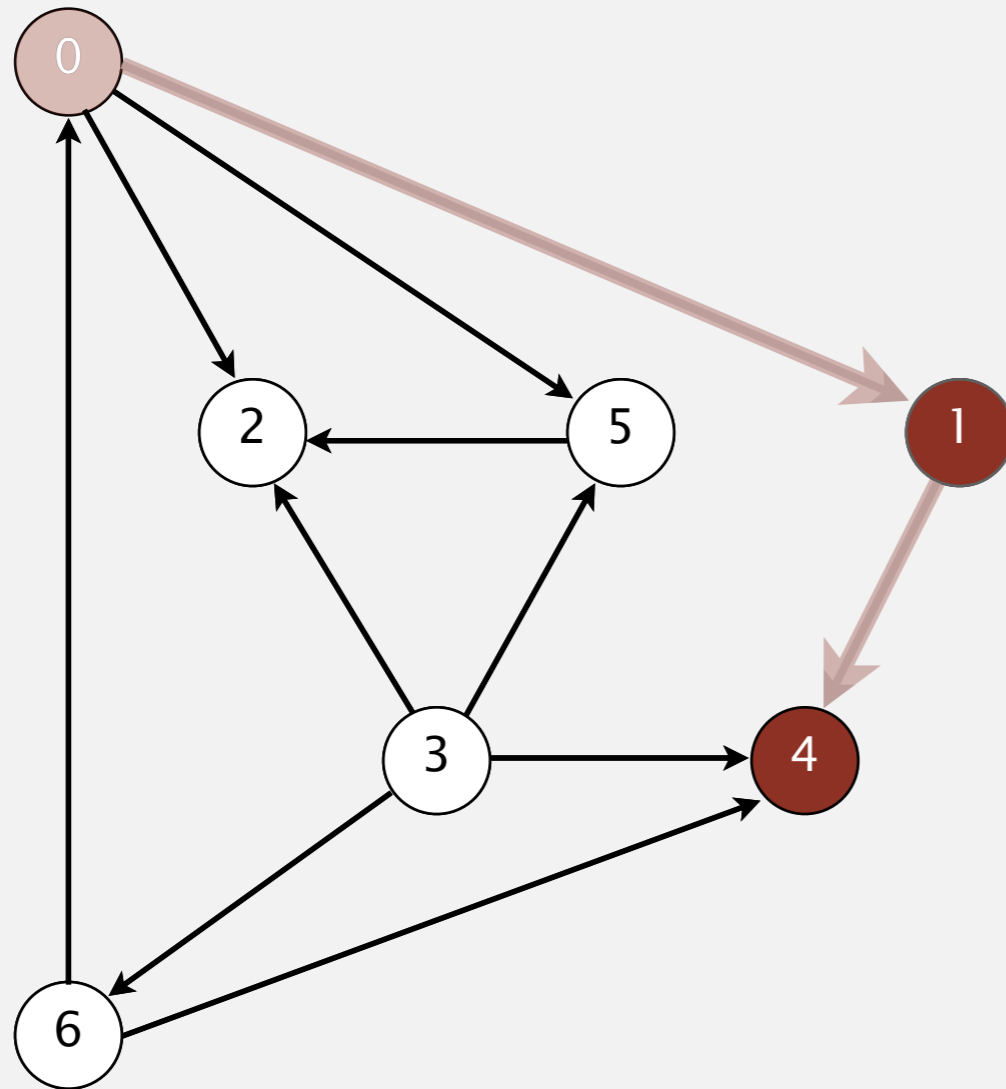
postorder

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | F |
| 3 | F |
| 4 | T |
| 5 | F |
| 6 | F |

visit 4

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

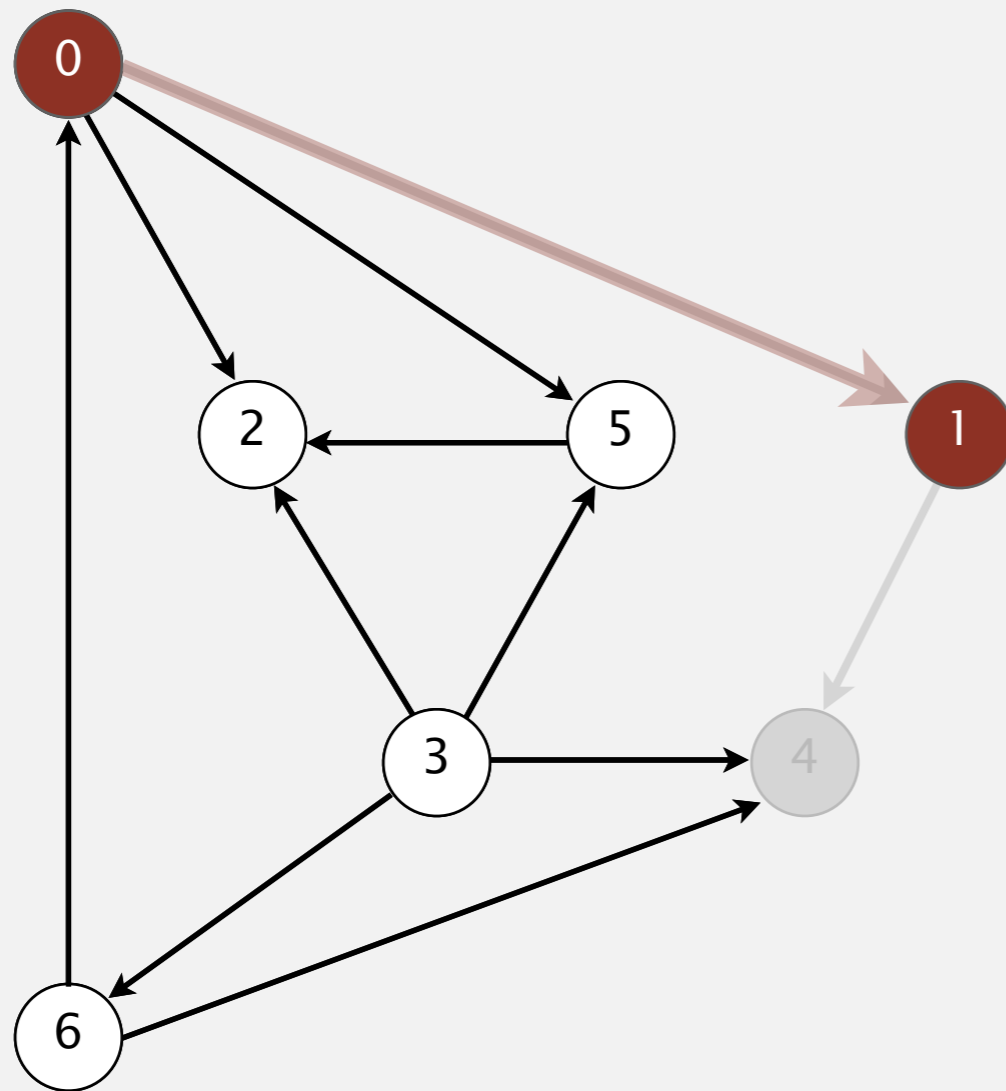
4

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | F |
| 3 | F |
| 4 | T |
| 5 | F |
| 6 | F |

4 done

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

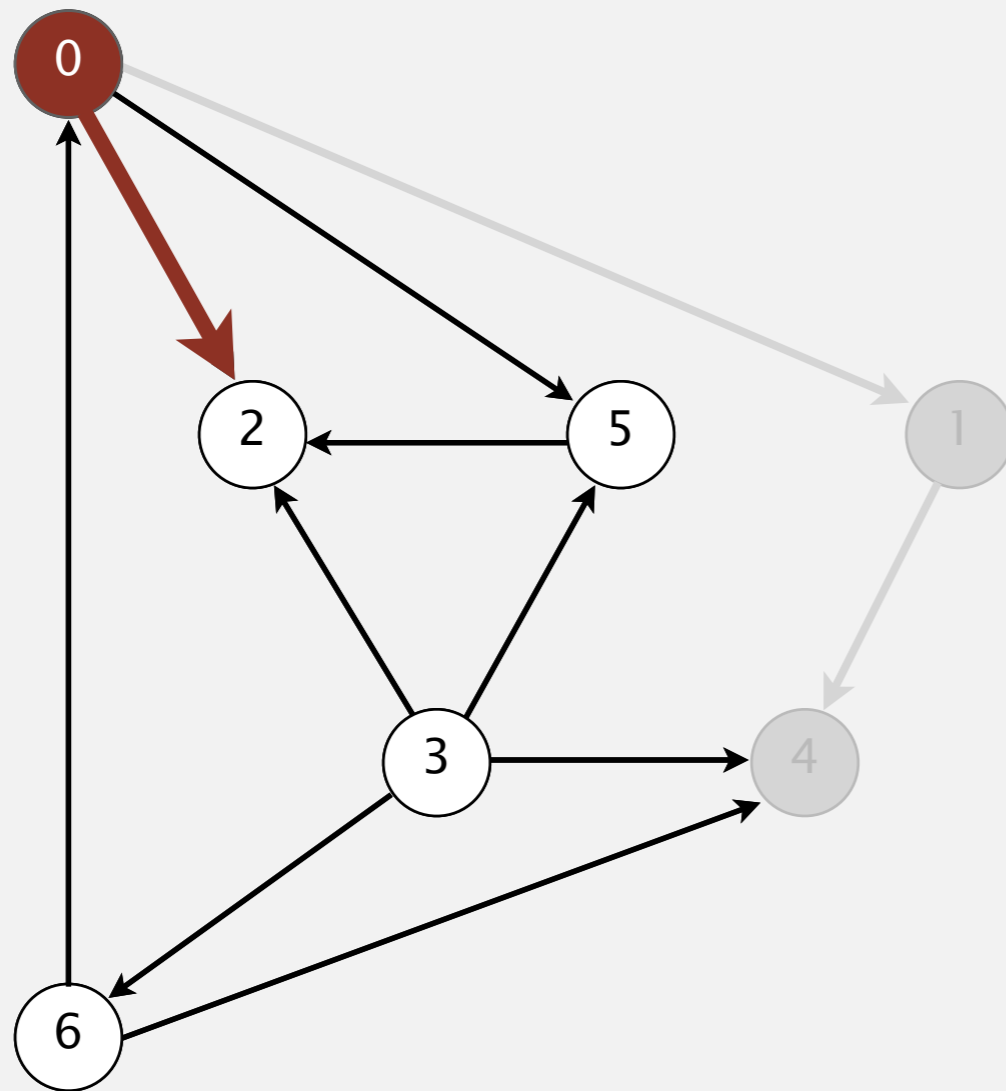
4 1

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | F |
| 3 | F |
| 4 | T |
| 5 | F |
| 6 | F |

1 done

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

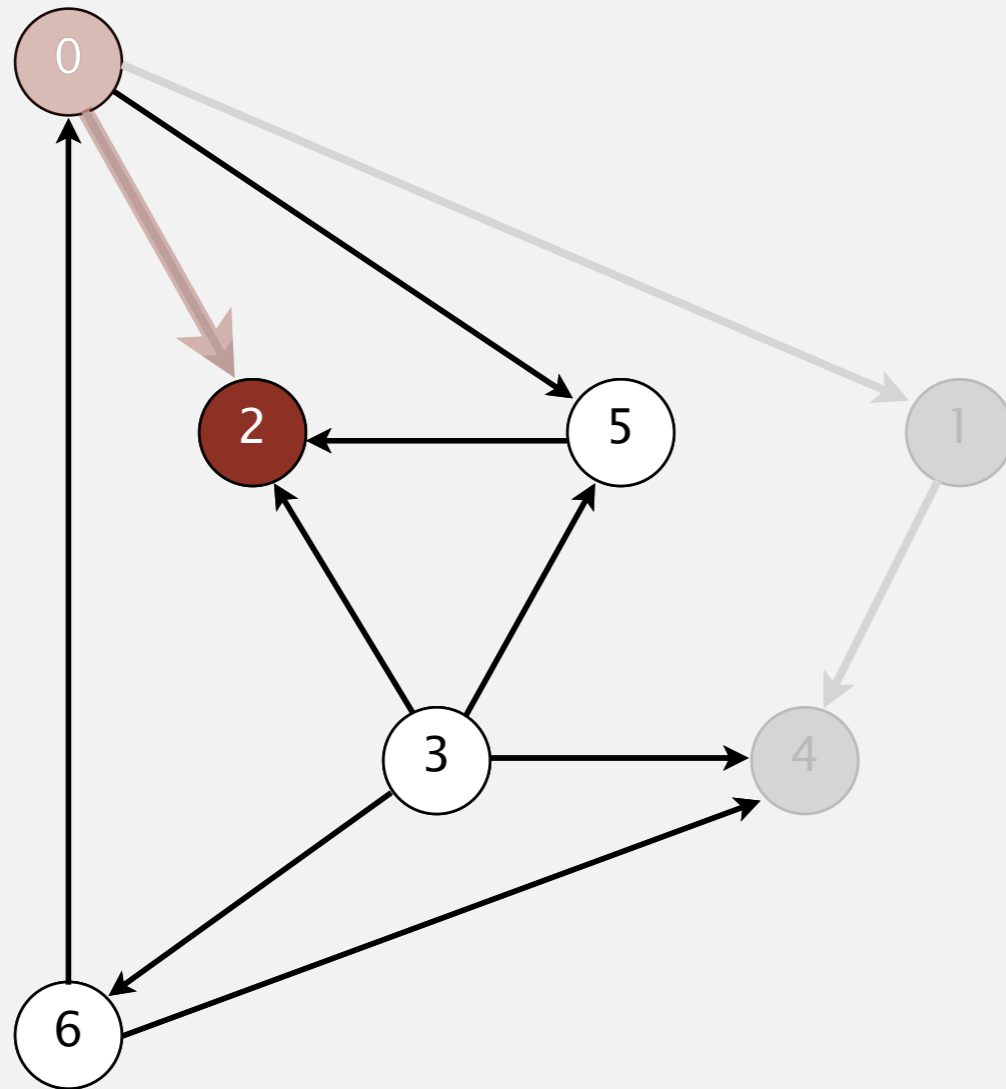
4 1

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | F |
| 3 | F |
| 4 | T |
| 5 | F |
| 6 | F |

visit 0: check 1, check 2, and check 5

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

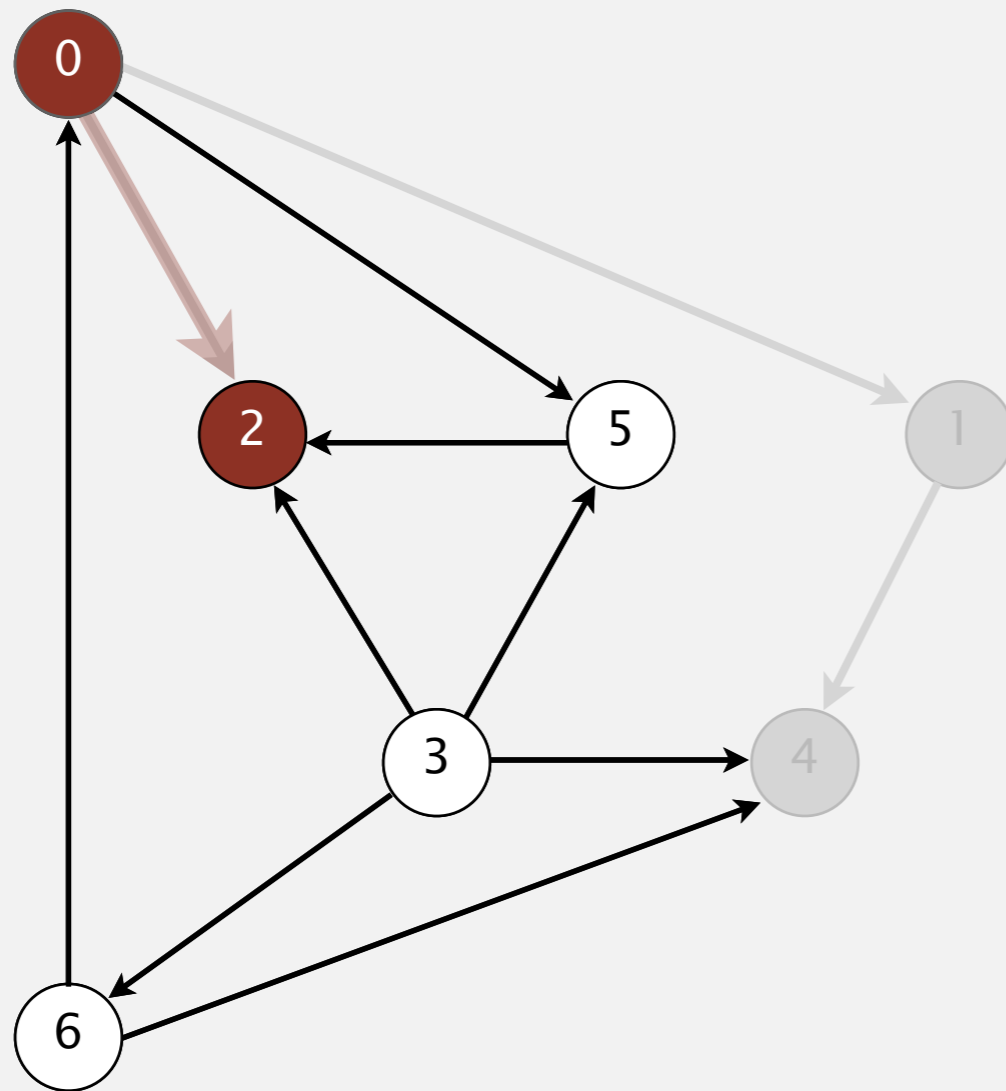
4 1

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | F |
| 4 | T |
| 5 | F |
| 6 | F |

visit 2

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

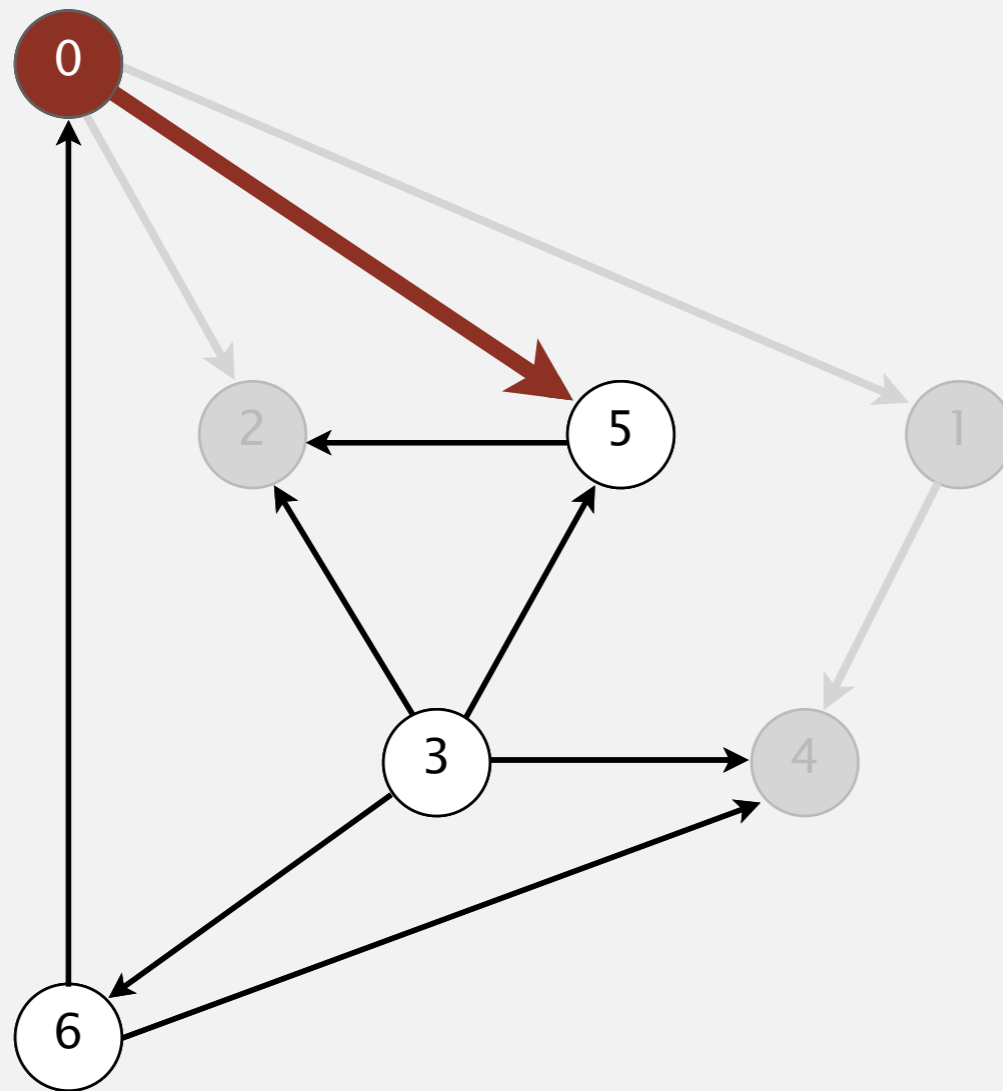
4 1 2

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | F |
| 4 | T |
| 5 | F |
| 6 | F |

2 done

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

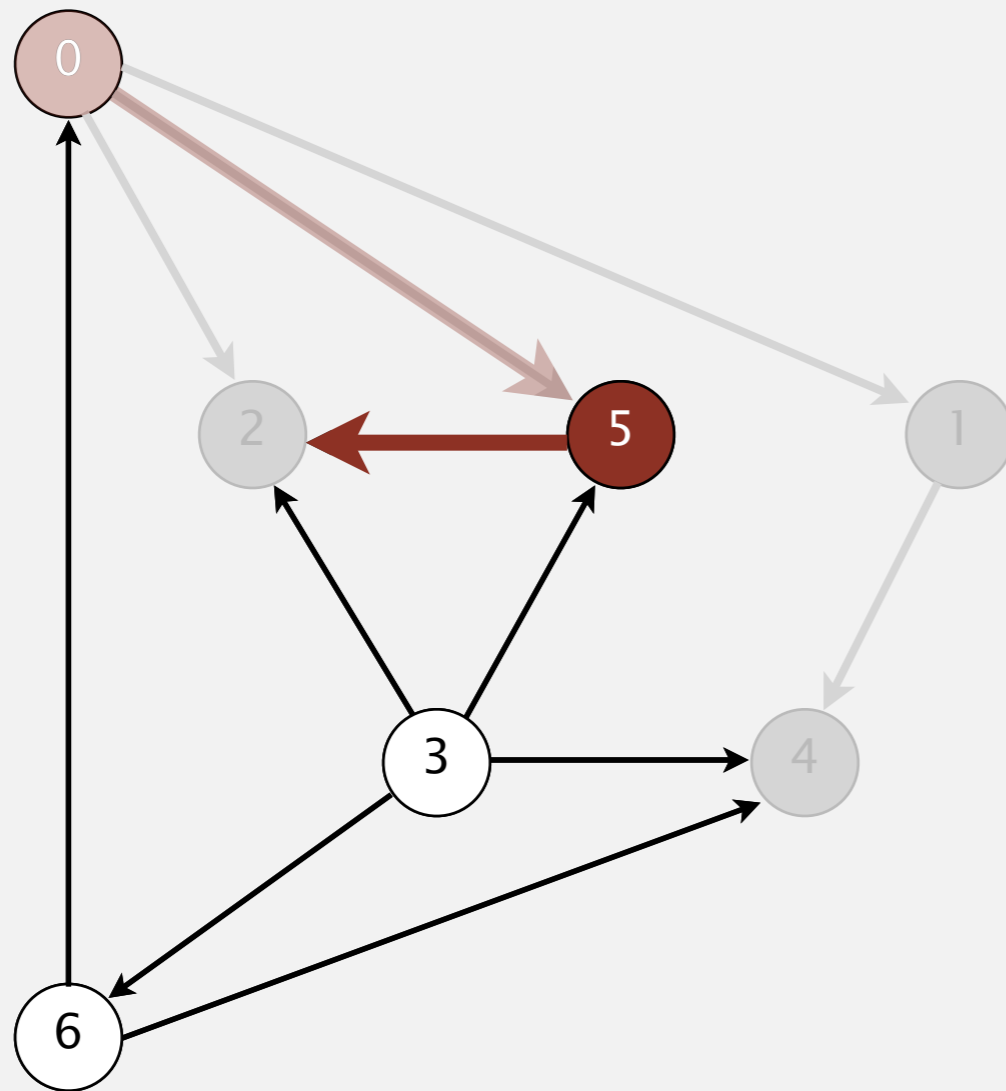
4 1 2

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | F |
| 4 | T |
| 5 | F |
| 6 | F |

visit 0: check 1, check 2, and check 5

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

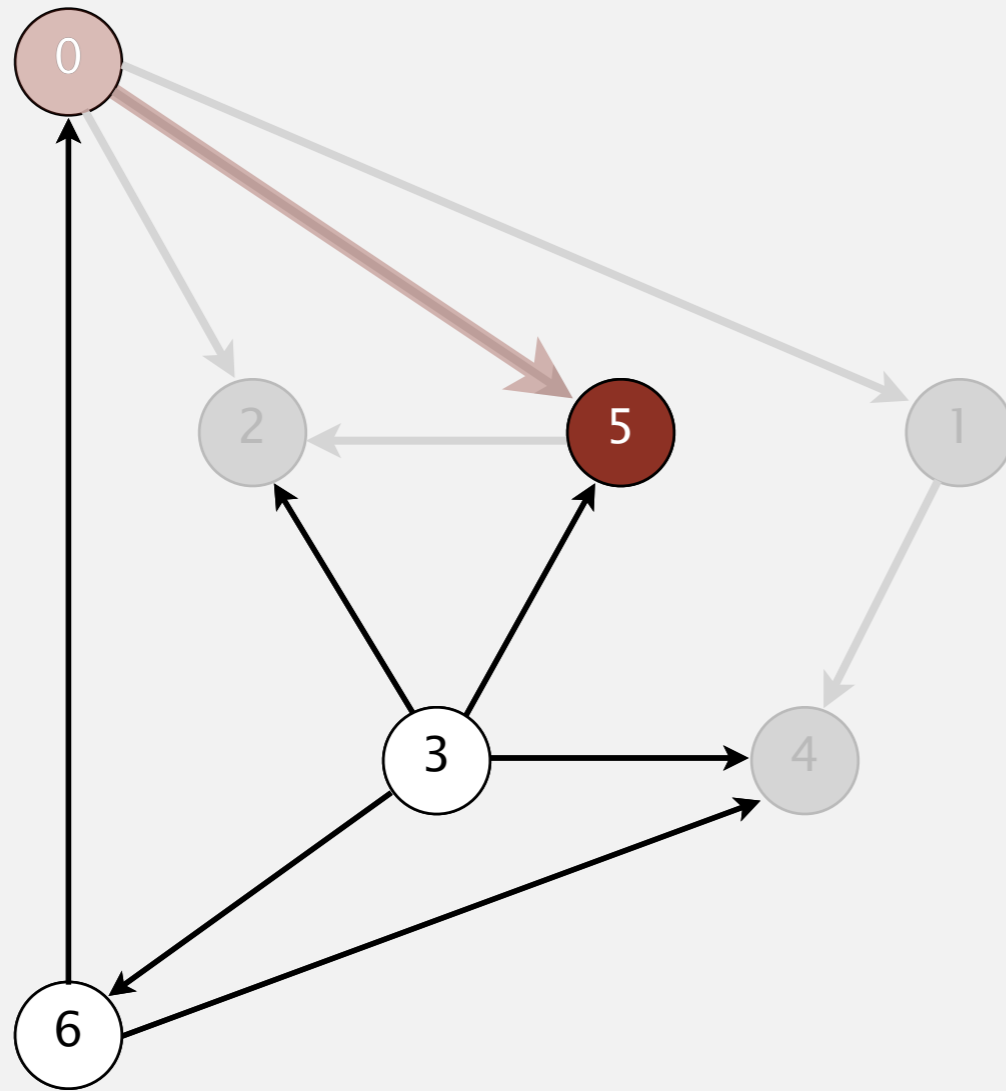
4 1 2

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | F |
| 4 | T |
| 5 | T |
| 6 | F |

visit 5: check 2

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

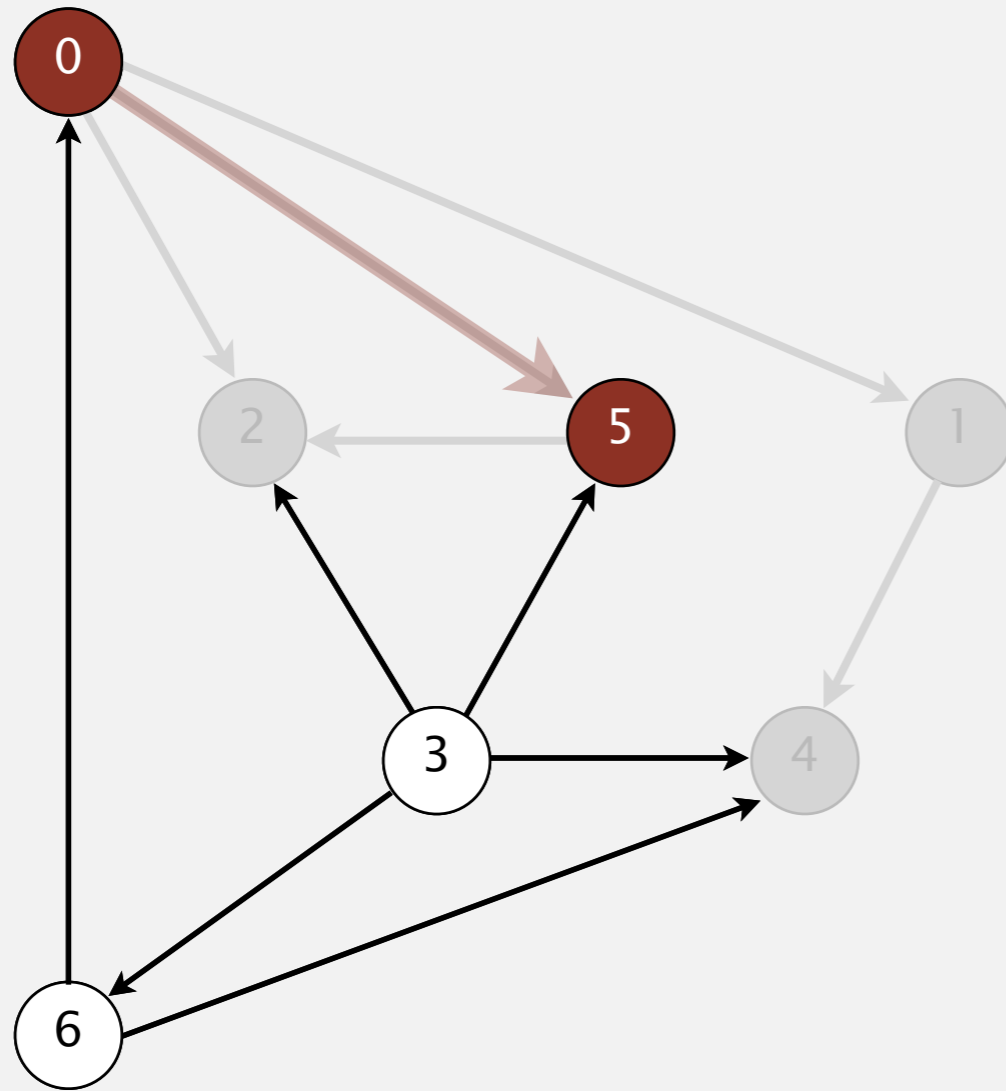
4 1 2

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | F |
| 4 | T |
| 5 | T |
| 6 | F |

visit 5

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

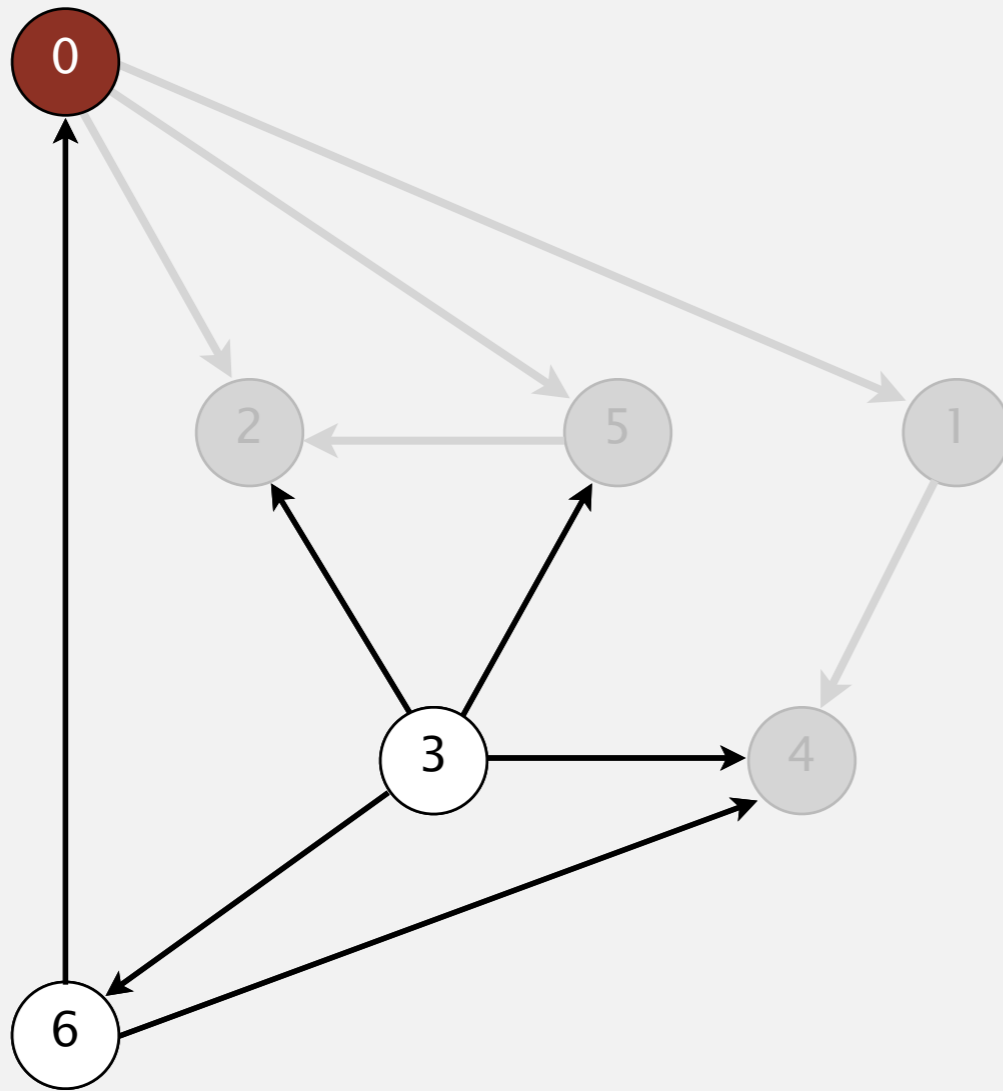
4 1 2 5

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | F |
| 4 | T |
| 5 | T |
| 6 | F |

5 done

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

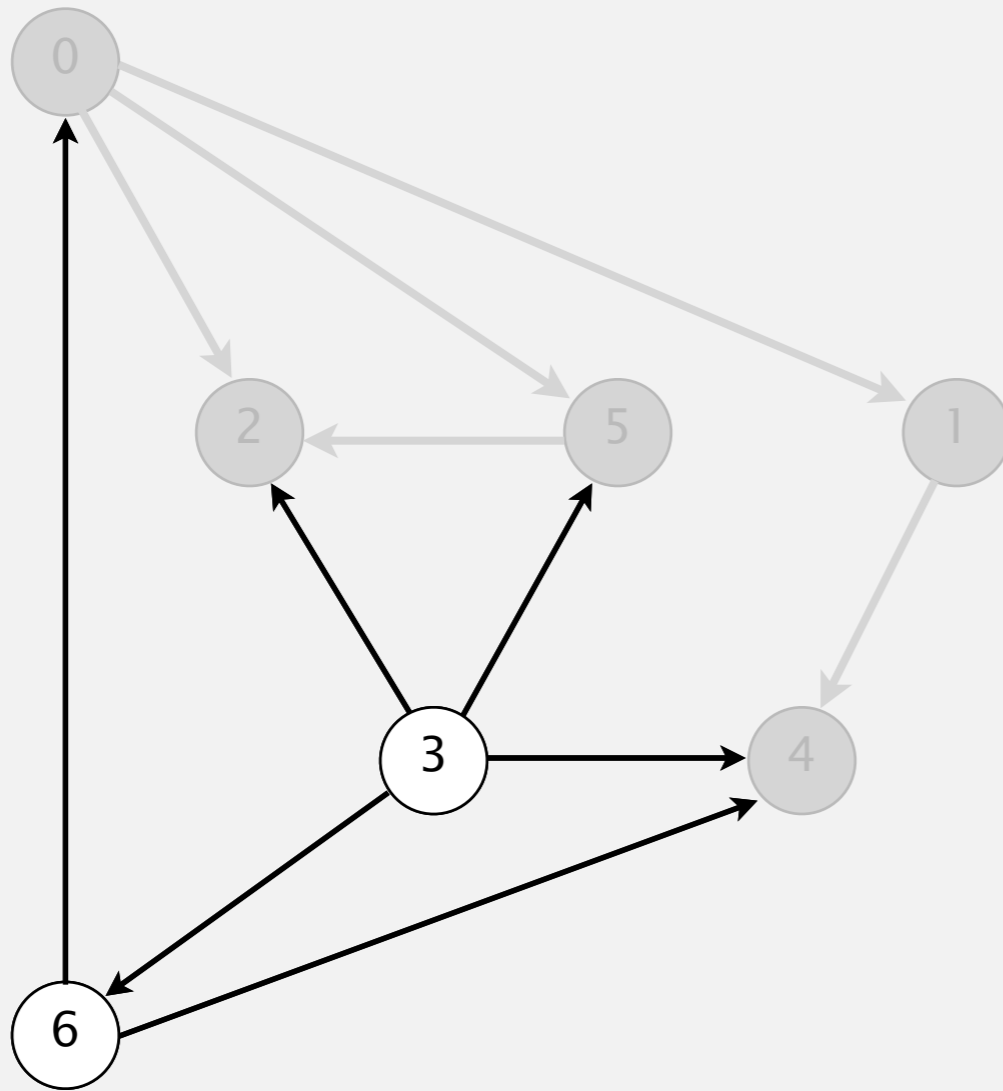
4 1 2 5 0

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | F |
| 4 | T |
| 5 | T |
| 6 | F |

0 done

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

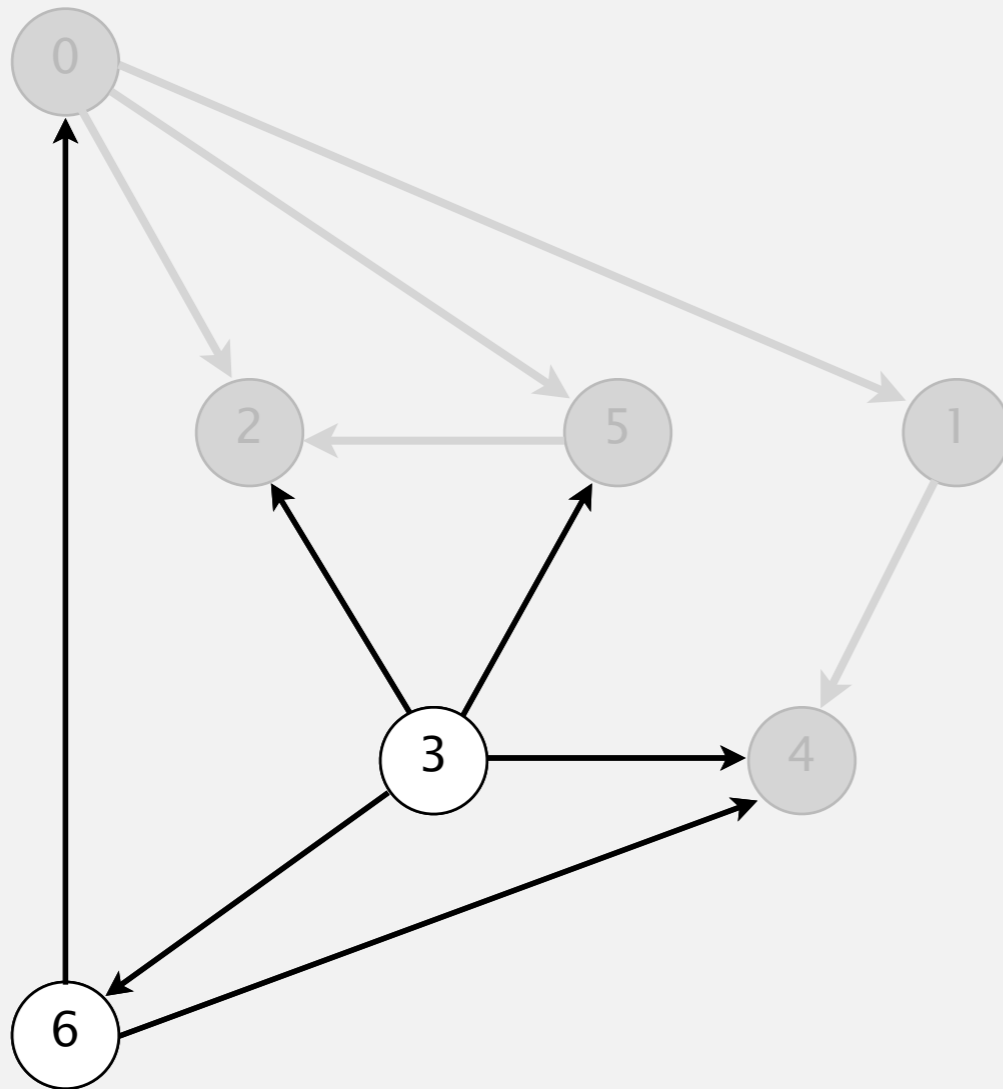
4 1 2 5 0

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | F |
| 4 | T |
| 5 | T |
| 6 | F |

check 1

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

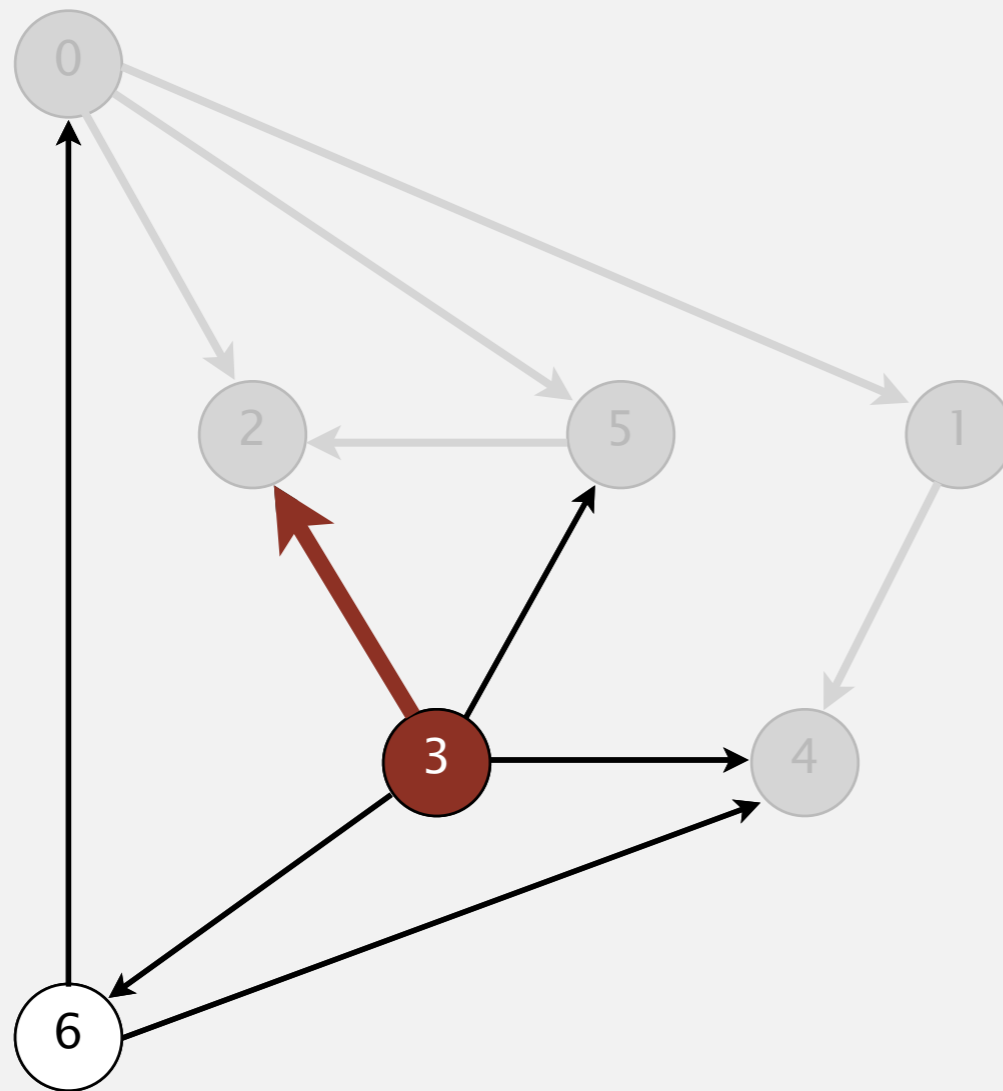
4 1 2 5 0

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | F |
| 4 | T |
| 5 | T |
| 6 | F |

check 2

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

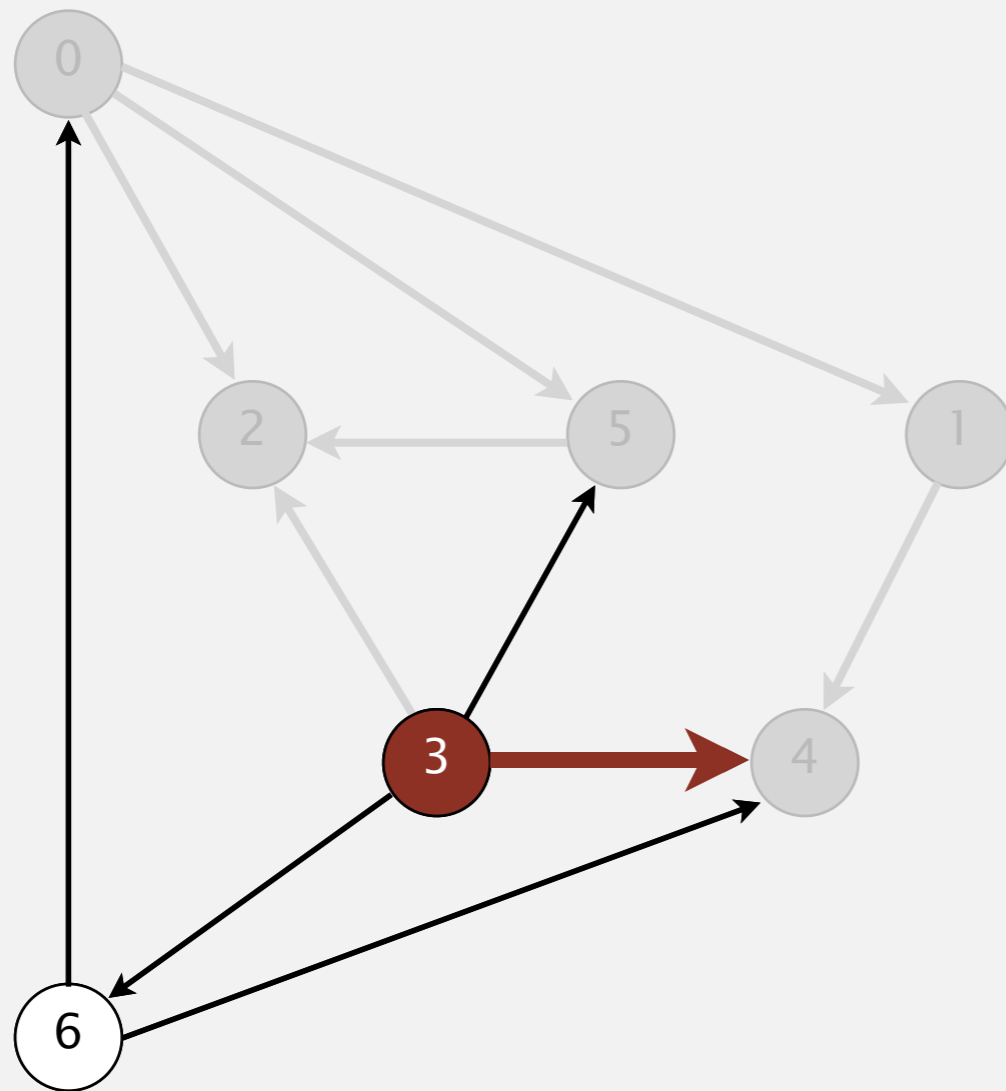
4 1 2 5 0

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | T |
| 4 | T |
| 5 | T |
| 6 | F |

visit 3: check 2, check 4, check 5, and check 6

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

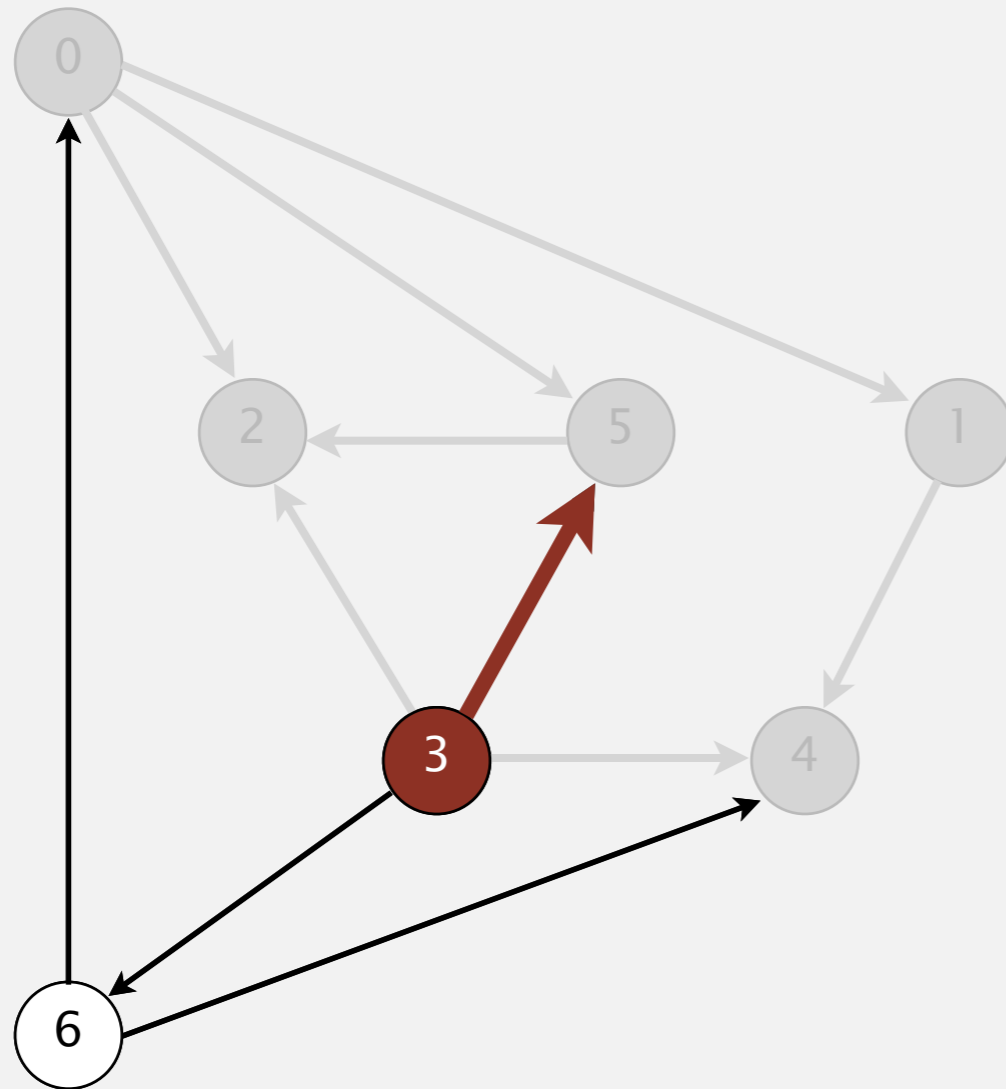
4 1 2 5 0

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | T |
| 4 | T |
| 5 | T |
| 6 | F |

visit 3: check 2, **check 4**, check 5, and check 6

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

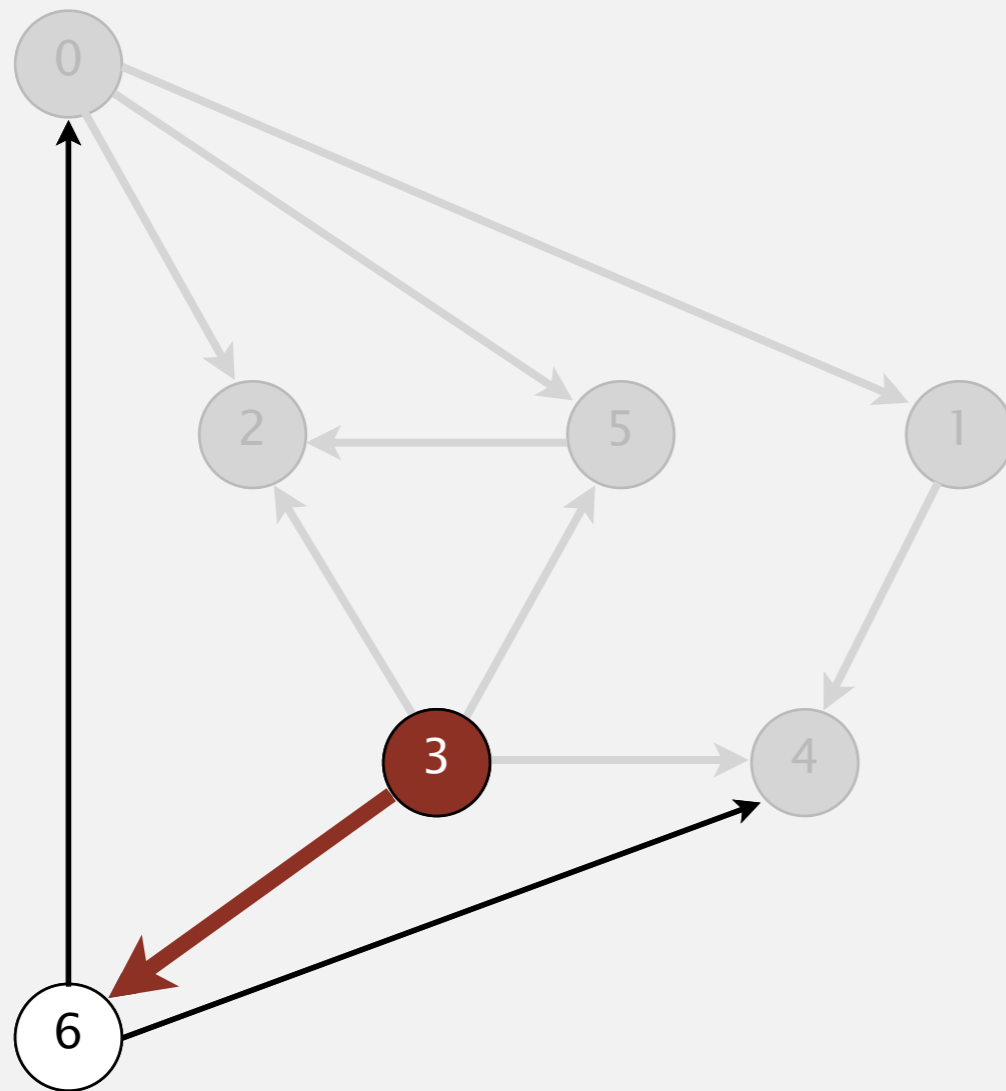
4 1 2 5 0

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | T |
| 4 | T |
| 5 | T |
| 6 | F |

visit 3: check 2, check 4, **check 5**, and check 6

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

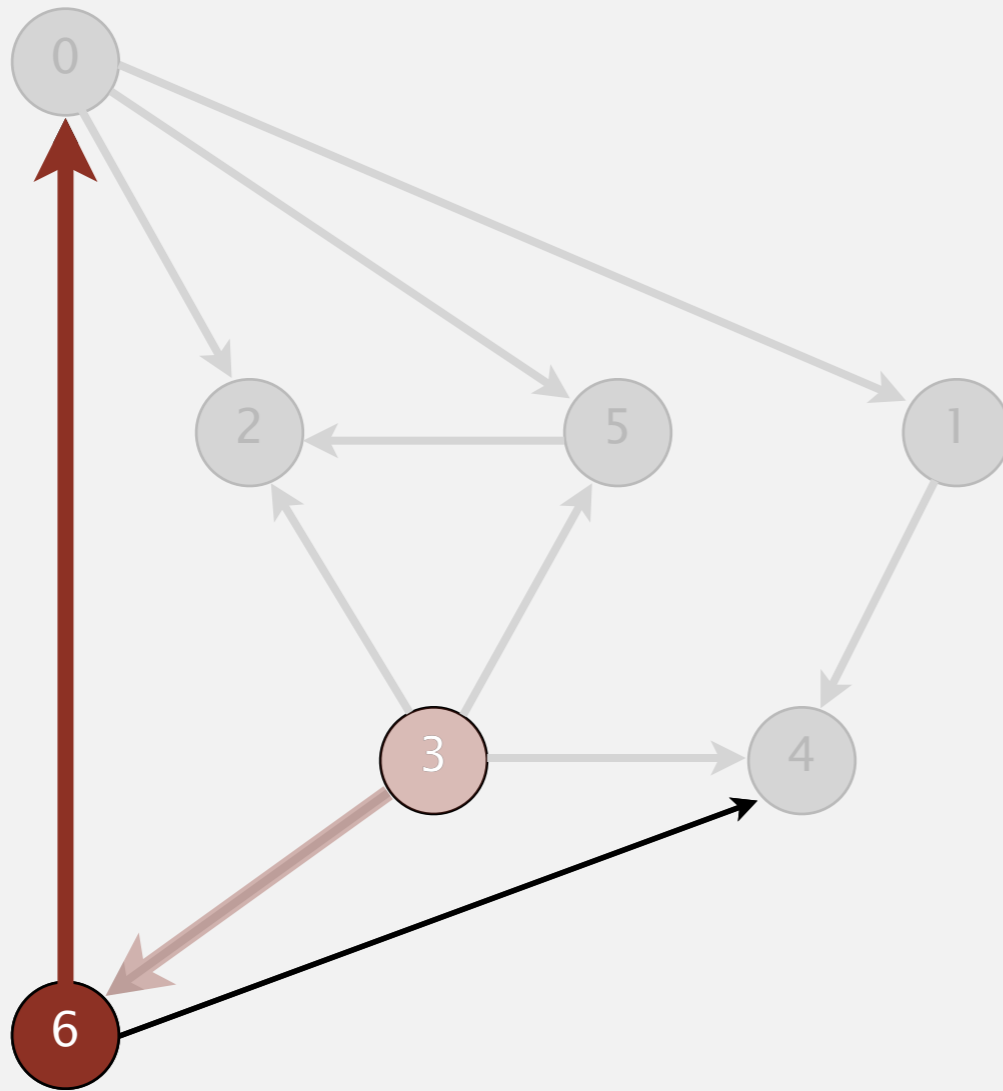
4 1 2 5 0

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | T |
| 4 | T |
| 5 | T |
| 6 | F |

visit 3: check 2, check 4, check 5, and **check 6**

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

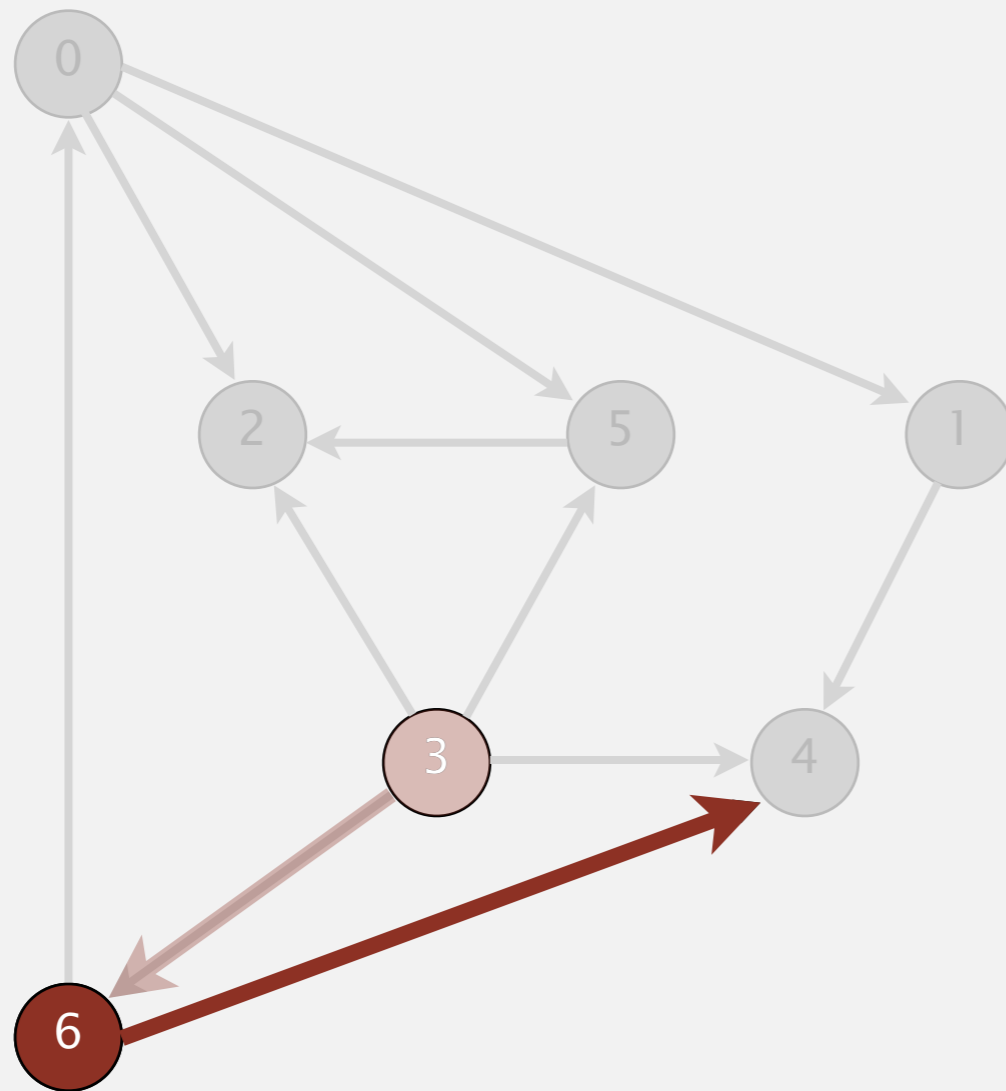
4 1 2 5 0

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | T |
| 4 | T |
| 5 | T |
| 6 | T |

visit 6: check 0 and check 4

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

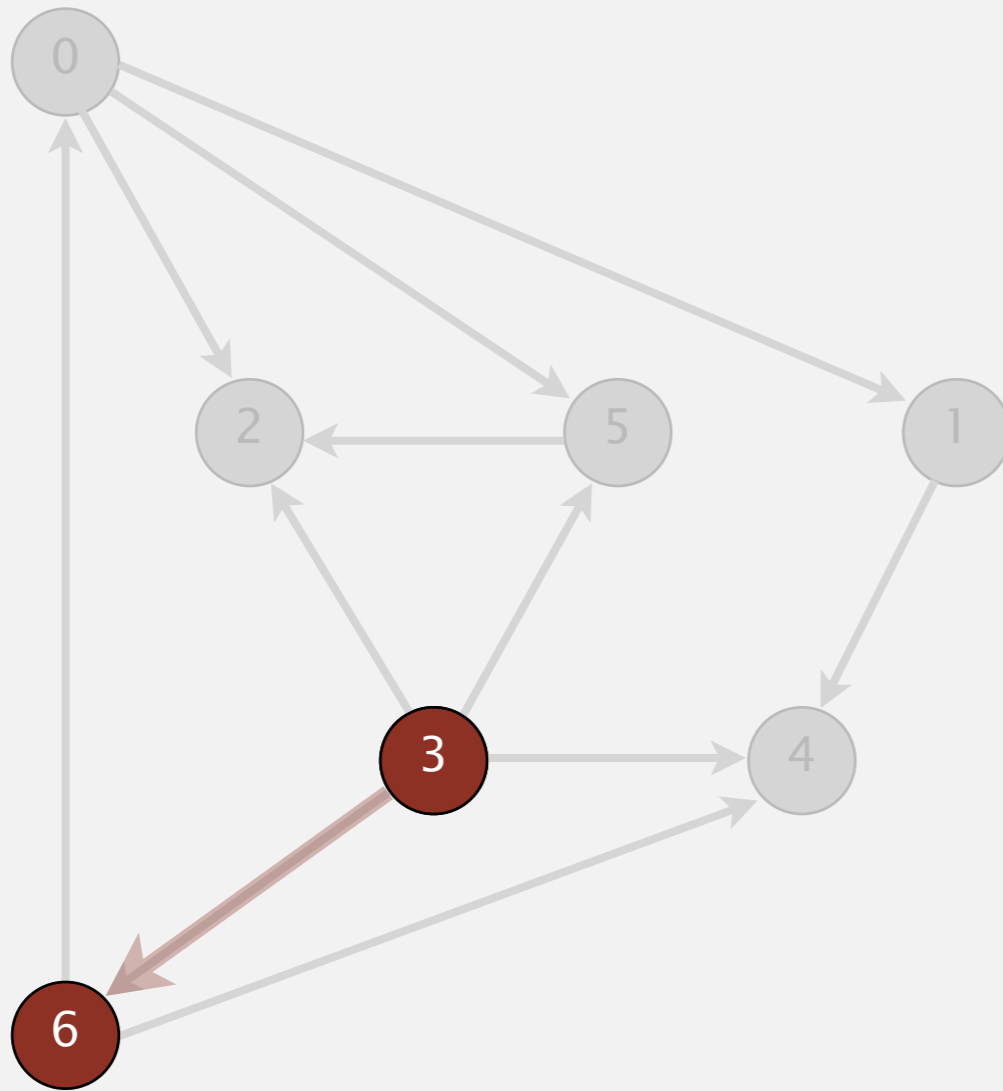
4 1 2 5 0

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | T |
| 4 | T |
| 5 | T |
| 6 | T |

visit 6: check 0 and **check 4**

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

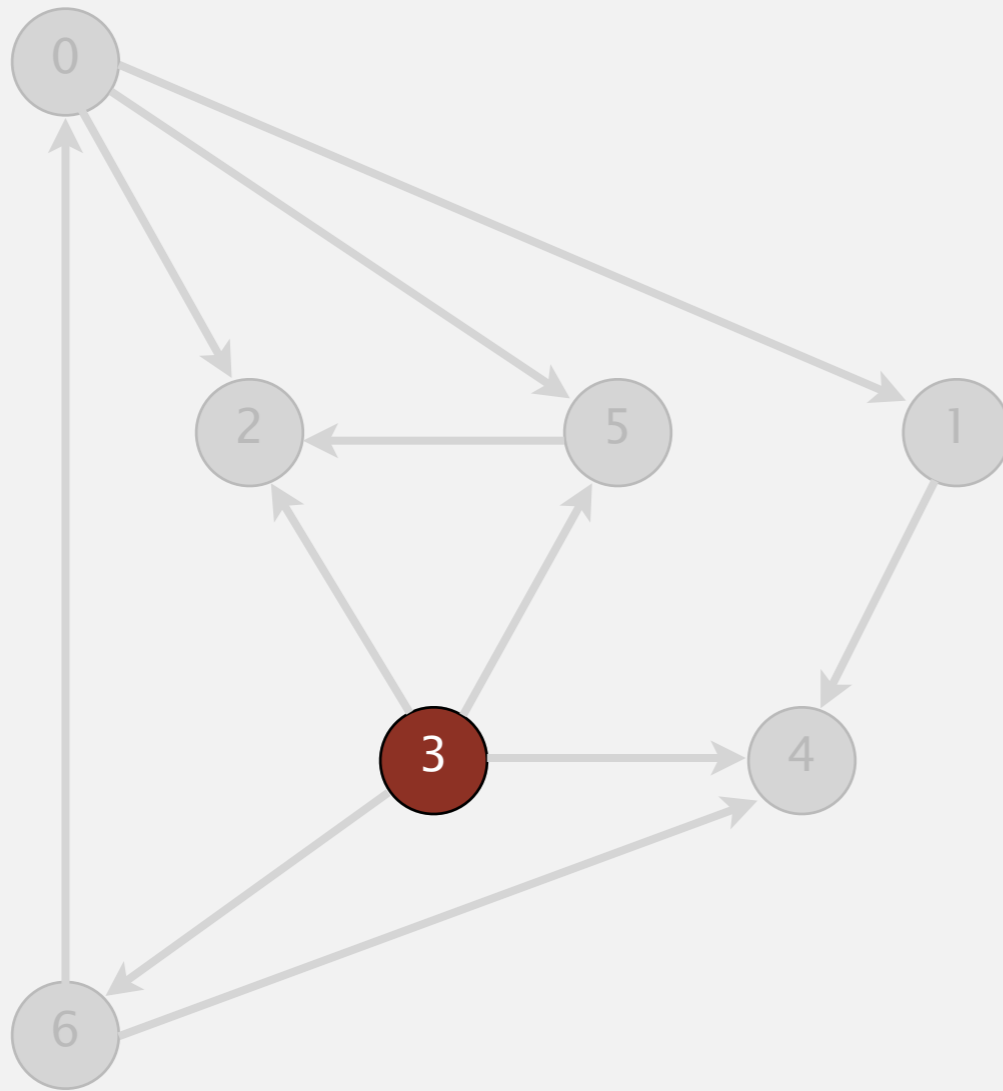
4 1 2 5 0 6

| <u>v</u> | <u>marked[]</u> |
|----------|-----------------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | T |
| 4 | T |
| 5 | T |
| 6 | T |

6 done

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

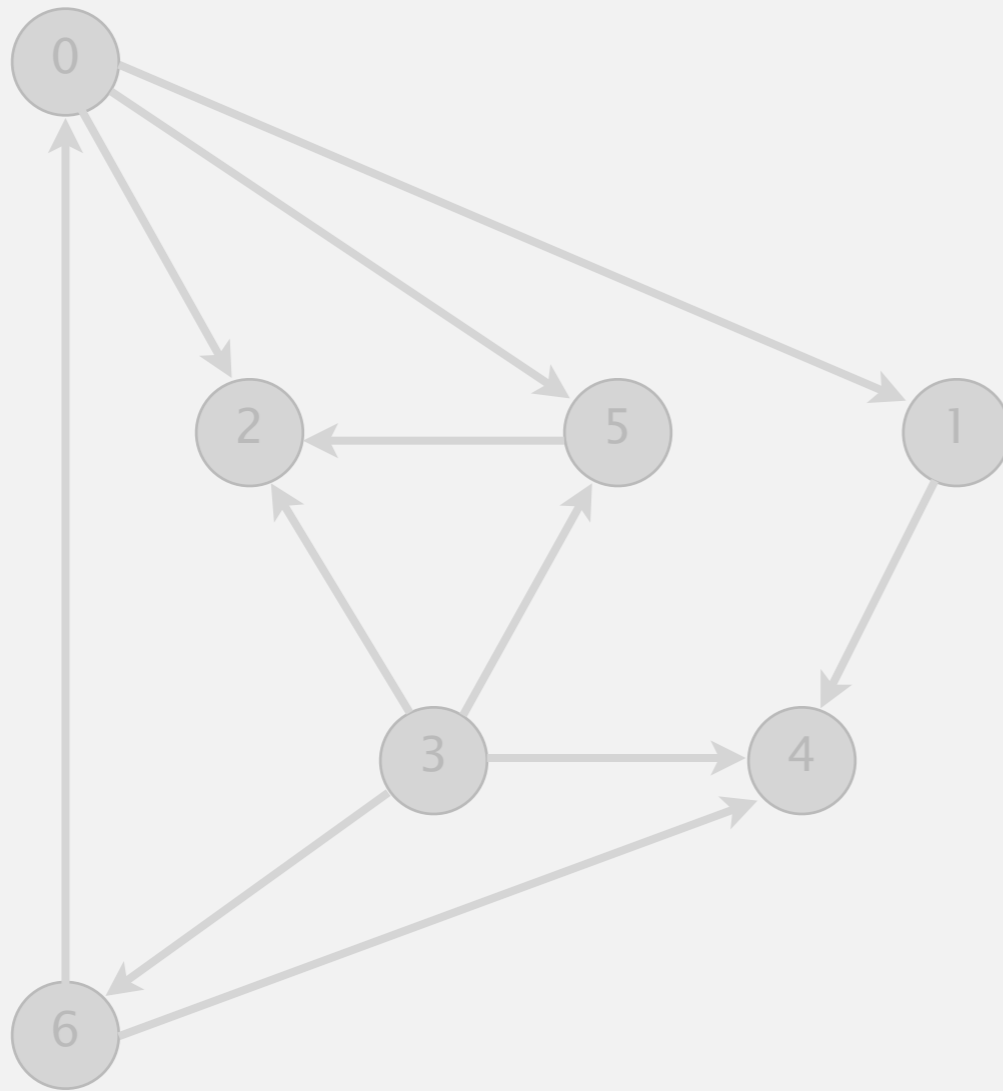
4 1 2 5 0 6 3

| v | marked[] |
|---|----------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | T |
| 4 | T |
| 5 | T |
| 6 | T |

3 done

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

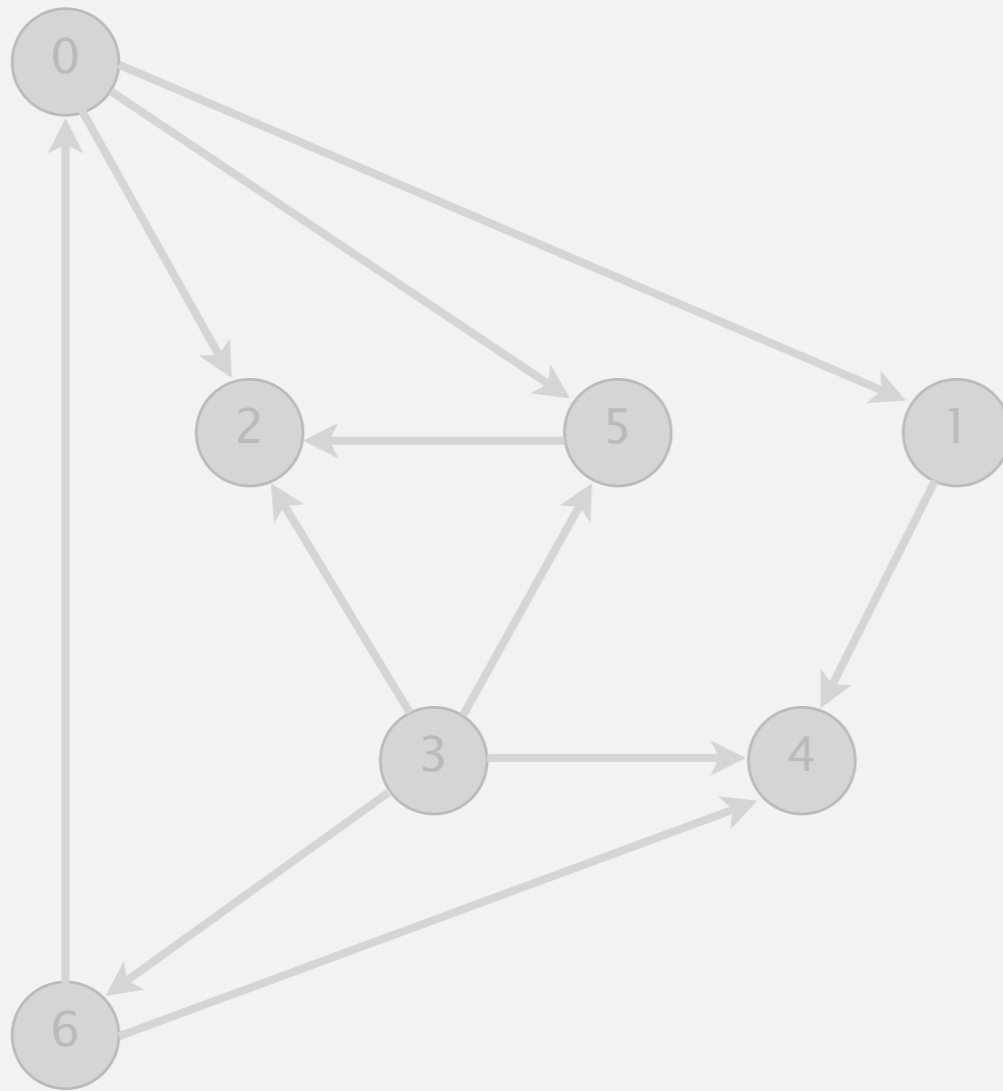
4 1 2 5 0 6 3

| v | marked[] |
|----------|-----------------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | T |
| 4 | T |
| 5 | T |
| 6 | T |

check 4

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

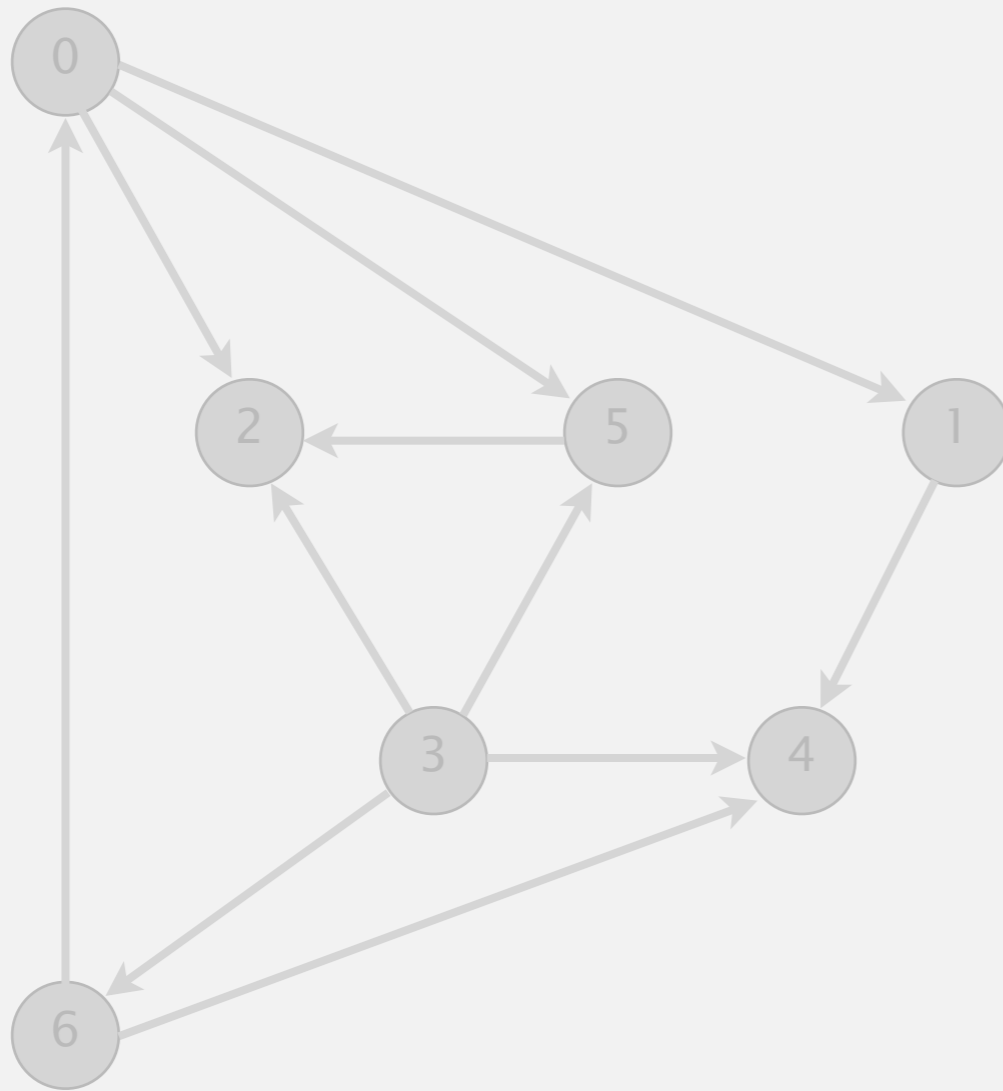
4 1 2 5 0 6 3

| <u>v</u> | <u>marked[]</u> |
|----------|-----------------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | T |
| 4 | T |
| 5 | T |
| 6 | T |

check 5

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

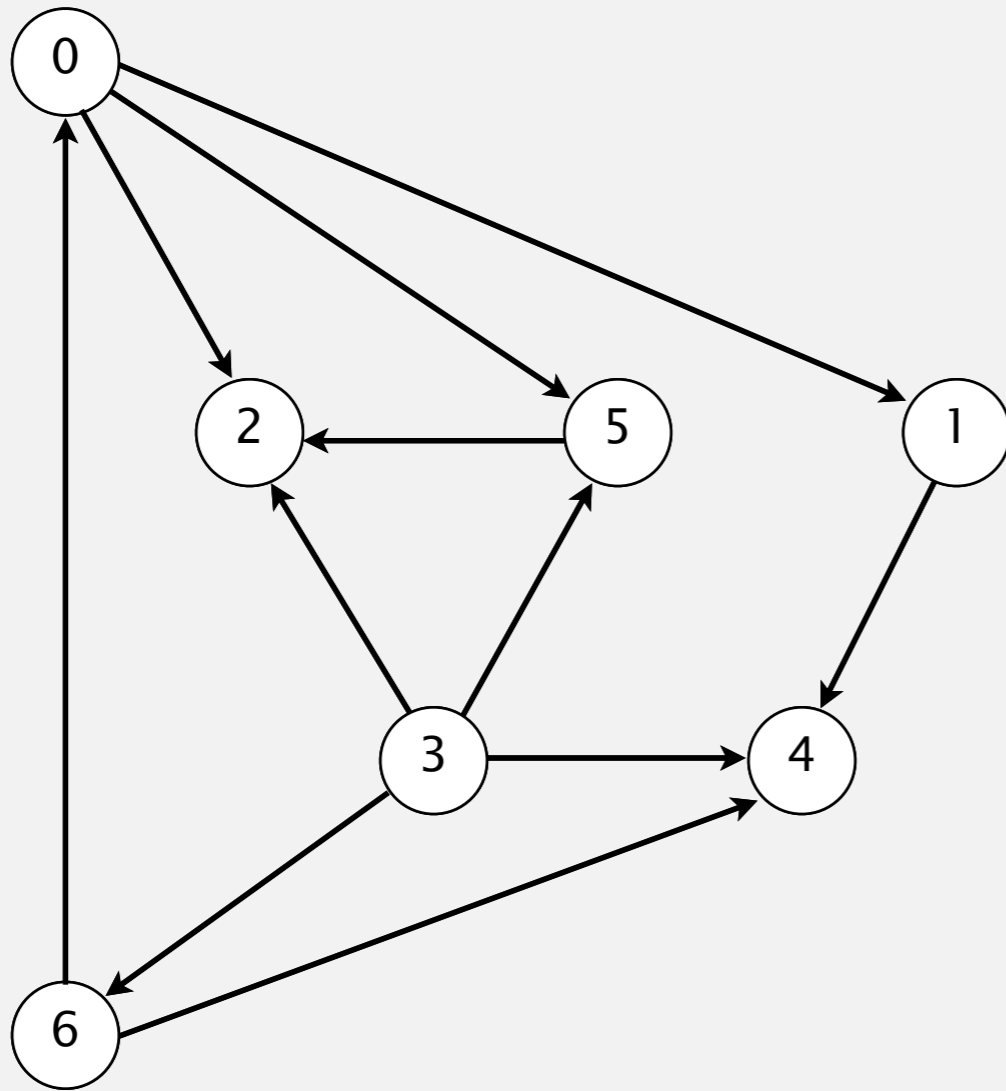
4 1 2 5 0 6 3

| v | marked[] |
|----------|-----------------|
| 0 | T |
| 1 | T |
| 2 | T |
| 3 | T |
| 4 | T |
| 5 | T |
| 6 | T |

check 6

Topological sort demo

- Run depth-first search.
- Return vertices in reverse postorder.



postorder

4 1 2 5 0 6 3

topological order

3 6 0 5 2 1 4

done